New Insight into Customer Value Analysis using Data Mining Techniques

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ABSTRACT

Recency, Frequency, Monetary model (RFM) has been widely used to analyze the customers' value in traditional market using three purchasing behavior attributes. This is considered one dimensional view of customers' value that is based on profit and purchasing criteria and ignores other useful attributes. Online customers have additional attributes that when captured and analyzed can give more details about customers' value other than provided by traditional RFM model. This gives companies better vision of their customers, and therefore serve them effectively, resulting in strong and long relationship with them. New Behavioral RFM1 Model (BRFM) is proposed in this paper to provide online retailers with a new customers' insight that reflects their web behavior beside their profitability. Three web behavioral attributes, represented in Recency of Session (Rs), Frequency of Session (Fs), and Number of clicks (NoC) are added to the traditional RFM attributes for customer value segmentation in online market using K-means clustering algorithm. The effectiveness of BRFM model is compared against the traditional RFM using Dunn index and Davies- Bouldin measures. Results show that the BRFM model enhances the clustering accuracy and reveals new customers' clusters disregarded by the traditional RFM model.

Keywords

Customer value analysis; Recency, Frequency, Monetary Model; K-means clustering algorithm; Dunn Index (DI); Davies Bouldin (DB)

1. INTRODUCTION

Customers are the heart of business success. Business cannot survive and get profit without maintaining loyal and satisfied customers and keep long term relationship with them [1]. Therefore, enterprises have adopted the Customer Relationship Management (CRM) strategy for managing their relationship with customers, learning more about customers' behaviors and values, and maintain profitable and strong relationship with them [2]. CRM's success lies in using the data mining techniques to extract useful patterns that improve the enterprises understanding of their customers [3,4].

Analyzing customers' value is a critical concept of CRM. It helps in assessing the loyalty and importance level of each customer to the enterprise, and develops more personalized relationship with them to maximize their current and future value [5]. The RFM model, which stands for Recency, Frequency, and Monetary, is the most commonly used model for the customer value analysis based on three purchasing attributes represented in Recency of purchasing (R), "Last purchasing time in specific period", Frequency of purchasing (F)," number of purchases in specific period", and the Monetary value of purchases (M), "total amount of purchasing in specific period." [6].

Analyzing Customers value based on the profit and the purchasing criteria is considered as one-dimensional view that does not guarantee customers' retention and loyalty to the enterprise. Profitable customers may turn to other competitors if they are provided with good offers, especially with the convenience of shopping online, where customers can easily shop in multiple online stores, get all information about available products, and make comparisons about prices. Furthermore, less profitable customers may be more valuable in the future if the company get richer understanding about their behavior and targets them better.

The World Wide Web, as a leading channel for conducting businesses, contains a huge amount of data about customer navigation patterns [7]. This behavioral data can be used beside the RFM purchasing attributes to provide online retailers with a rich customers' insight that reflects their interests, stickiness, intention to future purchase and loyalty besides reflecting their profitability.

In this paper, three web behavioral attributes, represented in Recency of session (Rs) (Number of days since last time the customer visit the website), Frequency of session (Fs) (Number of visits done by customer within a specific time frame, and the Number of Clicks (NoC) (Number of requested pages by customer over a specific time frame), are added to RFM purchasing attributes for analyzing the customer value in online retailing. Then k-means clustering algorithm is used to cluster customers using BRFM model into different clusters. These new clusters don't only identify customer purchasing behavior but also reflect their intention to future purchase, their loyalty, interesting, stickiness to company's products which are reflected in how recently they visited the website, their number of site visits and their number of clicks that may indicate how they navigate in the web site. These attributes identify new categories of customers that are not shown using traditional RFM as will be shown in section 3.4. one of these categories are customers that are not profitable to the company but may still interested in the company's products. Companies may get benefit of this information and try to address those customers with more effective promotions and marketing campaigns according to their web behavior and

¹ Behavioral RFM (BRFM): is three web behavioral attributes represented in Recency of session (Rs), Frequency of session (Fs), and Number of clicks are added to RFM model.

their purchasing characteristics to encourage them make purchases. As a result, companies' revenue is increased by assigning suitable resources to right customers, and guarantee customer loyalty and retention.

Finally, the different clusters resulted from RFM and BRFM model are compared and examples of customers' movement from cluster to cluster based on the new BRFM model are also shown. And then the accuracy of BRFM resulted clusters is compared against the traditional RFM using Dunn index and Davies Bouldin measures.

The rest of this paper is organized as follows. Section 2 presents an overview of the related works concerning customer value analysis using data mining techniques. Section 3 describes the Behavioral RFM model. Section 4 evaluates the effectiveness of BRFM model using Dunn Index and Davies Bouldin measures, and then results are discussed in section 5. Finally, Section 6 concludes this study and suggests some areas for the future work.

2. RELATED WORK

Customer value is an important metric to measure the loyalty and importance level of each customer to the enterprise. RFM (Recency, Frequency, and Monetary) model, proposed by [6], is the most widely used model for customer value analysis. Many researchers have employed the RFM model with different data mining techniques for customer value segmentation in Brick and Mortar (physical market) and in online retailing as follows:

2.1 Customer Value Analysis in Brick and Mortar (Physical Market)

There are many studies in literature that are concerned with analyzing the customer value in physical market using RFM model and different data mining techniques as follow. [8], used RFM model and K-means clustering algorithm to segment customers of electronic company in Taiwan into five loyalty clusters. The customer lifetime value (CLV) of resulted clusters is calculated based on the distance between the center of cluster and zero point. Then, RFM attributes (input attributes) and the resulted loyalty clusters (decision attribute) are joined into rough sets theory (the LEM2 algorithm) to enhance classification accuracy. Similar to previous study, authors in [9] segment customers of a grocery store using RFM and K-means clustering algorithms based on their value into five clusters. The study used the C5 classification algorithms on the obtained K-means clusters for predicting the loyalty of future customers based on demographic attributes. Paper [10] proposes an extension of RFM model by applying it on database containing customer transactions and three customer types (Silver, Gold, and Platinum). Customers are segmented using K-means algorithm into five groups of loyalty three repeated times according to the customers types to find customer loyalty in each type of customer.

Some authors used Weighted RFM (WRFM) instead of RFM for customer value segmentation. WRFM proposed by [11] where different weights are assigned to R, F, and M depends on characteristics of the industry. Authors in [12] and [13], use the WRFM and K-means for customer value segmentation and the customer lifetime value (CLV) of each cluster is calculated as the sum of normalized RFM multiplied by their weights. Other researchers try to develop RFM model and add some parameters to these three attributes. LRFM model and K-means are used by [14] and [15] to carry out customer value segmentation, L refer to the interval is between the first and last exchange with a customer. These studies used L because it is supposed that customers with longer relationship are more loyal. Authors in [16] perform RFM, WRFM, and LRFM with K-means algorithm for customer value segmentation to find the golden customer by getting the top ten sold products and determine which customer belong to the golden segment in RFM, WRFM, or/and LRFM purchases one or more of these top products.

2.2 Customer Value Analysis in Online Retailing

Paper [17] used the RFM model and K-means to segment customers of online retail business into five meaningful groups, then the study compares the resulted five clusters in term of their profitability based on the average RFM and the number of customers in each cluster. Authors in [18] used RFM attributes to define the profitable customers of small sized online shopping mall. Then three classification models are applied to classify customers into VIP or non-VIP. Finally, the study applied sequential patterns and association rules algorithms into the transactions of VIP customers only to get rules and patterns. RFM and k-means++ were used in [19] to segment customers of online sports store in Turkey into eight clusters. Then, the C4.5 classification model is used to predict the future customer value using RFM values and some demographic attributes as input attributes and the resulted clusters value as class attribute. Finally, association rule mining was applied for product recommendation. Paper [20] used weighted RFM and Kmeans to segment customer of electronic flower retailing company into eight clusters. Research [21] segment customers of online mobile sales website in terms of their lifetime value using WRFM model and self-organizing map. Customer lifetime value in each cluster is calculated based and clusters are categorized based on the resulted life time value in customer value pyramid.

It can be concluded that the majority of previously stated researches handled the customer value issue in brick and mortar market and in online market in term of customer profitability and purchasing behavior, which is considered as a one-dimensional view of customers' value. This dimensional view only focuses on the profit comes from customers spend and their purchasing attitude, that does not guarantee company to get loyal customers (i.e. keep long term relationship with them). A company need to gain a new and richer insight for customers' value, which reflects how customers are interested in the company, their stickiness to company and their intention to future purchase, besides the purchasing and profit criteria. Based on this insight, company can develop and target customers with more effective marketing strategies that maximize their future value and keep long term and profitable relationship with them.

Table 1 summarizes the previous researches that are concerned with customer value analysis in physical and online market based on the used criteria as follow:

 Table 1. classification of customer value analysis studies

 based on the used criteria

Criteria References	RFM	WRFM	LRFM	Case Study						
Customer value analysis in physical traditional market (Brick & mortar)										
Cheng and Chen [8]		Electronic company								
Qiasi et al.	✓			Grocery						

[9]				store
Bunnak et al.	./			Commercial
[10]	v			store
Liu and Shih				Hardware
		\checkmark		retailing
[12]				company
Khaiyand et				Health and
al [13]		\checkmark		Beauty
ai. [15]				Company
Li, D et.al.			\checkmark	Textile
[14]				business
Parvaneh et			\checkmark	B2B
al. [15]				
Mesforoush			,	SME
and Tarokh	✓	\checkmark	\checkmark	Company
[16]				company
Cust	tomer valu	e analysis oi	1-line retai	ling
Chen et al.	1			Online retail
[17]	•			business
Shim at al				Online
	✓			shopping
[10]				mall
Birant [10]	1			Online sport
Dirant [17]	•			store
Tabaei and				Electronic
Fathian [20]		\checkmark		flower
Taunan [20]				retailing
Ansari and				Online
i mbari ana				Omme
Ghalamkari		\checkmark		mobile sales

3. BEHAVIORAL RFM MODEL (BRFM)

This section introduces and explains the proposed Behavioral RFM (BRFM) model for analyzing the customers' value based on their web behavior and their purchasing patterns. Three web behavioral attributes represented in Recency of session (Rs), Frequency of session (Fs), and Number of clicks (NoC) are added to the purchasing based RFM model for customer value segmentation in on-line market.

It is supposed that more recent and frequent user session and more number of clicks reflect how far customers are interesting to know about the company's products and are intended to make future purchase, which means more customer loyalty and value. Figure 1 shows the proposed Behavioral RFM Model, where customers' transaction data and web log data are preprocessed to get the Behavioral RFM (BRFM) attributes to be included in K-means clustering algorithm for customer value segmentation. Then the customer lifetime value (CLV) is calculated and ranks are assigned, then the resulted BRFM clusters are analyzed to understand their characteristics.

3.1 Data Pre-processing

Data in transaction data set and web log files are in unsuitable format for customer segmentation. It needs to be cleaned, and BRFM related attributes are to be extracted. Then the extracted data will be transformed into an appropriate format for the K-means clustering algorithm. The preprocessing steps of the transaction data and web log files are explained as follow:

3.1.1 Transaction Data Pre-processing

In this step, the transaction data set is cleaned and the related attributes to RFM model are selected. Then the selected attributes are transformed based on the actual value of RFM, as recommended in [22] for more clustering accuracy, into three attributes which are Recency (Rp): number of days since last purchasing date, Frequency (Fp): the number of purchases done by customer within a specific time frame, and Monetary (M): the total amount of sales by a customer over the wholetime frame.



Fig 1. The Behavioral RFM Model (BRFM).

3.1.2 Web Log Data Pre-processing

In this step, the web log files are cleaned by removing the records with failed HTTP status codes and records of graphics and videos, and the relevant user sessions are identified by considering specific run out time between requests which is commonly over than 30 minutes [23, 24]. Then, the web behavioral attributes in BRFM model are to be extracted from these files. These attributes are: the Recency of session (Rs) which is the number of days since last session, the Frequency of session (Fs) which is the number of sessions done by a specific user within a specific time frame, and the Number of Clicks (NoC) which is the number of requested pages by a specific user over a specific time frame. The extracted web log attributes are then combined with RFM attributes resulted from the transaction data preprocessing step to be ready for customer segmentation step. Table 2 provides an example of the preprocessed BRFM attributes.

Table 2. Preprocessed BRFM Attributes

User Name	R _P	F _P	Μ	Rs	Fs	NoC
Cassandra Brandow	79	2	2538	29	6	463
Denny Ordway	109	2	6696	48	6	455
Jonathan Doherty	20	5	11212	20	8	447
Arthur Prichep	77	4	9262	49	7	427

3.2 BRFM Customer Segmentation

After the preprocessing step, data is ready and suitable to be used for customer segmentation into different value segments based on their web behavior and purchasing patterns. K- means clustering algorithm is used for customer value segmentation using the Behavioral RFM attributes (Recency of purchasing (R_P), Frequency of purchasing (F_P), Monetary (M), Recency of session (Rs), Frequency of session (Fs), and Number of clicks (NoC).

In traditional RFM model, customers are segmented into eight clusters[12,19,20]. This is because there are eight possible combinations of patterns resulted from assigning one of the (upward \uparrow or downward) pattern to each one of the three RFM attributes. This assignment is based on a comparison between the average value of the RFM in clusters and the overall average value of RFM in the data set. The

characteristics of each cluster is described according to the pattern (\uparrow or \downarrow) assigned to each R, F, and M attribute.

In the proposed BRFM, customers are also segmented into 8 clusters as RFM model in order to evaluate the impact of adding the web behavioral attributes to RFM on the clustering accuracy when the same clustering algorithm and same number of clusters are used.

Table 3 shows the eight customer segments resulted from using the BRFM attributes, each cluster is shown with the corresponding number of customers, the average value of Rp, Fp, M, Rs, Fs, NoC attributes, and the associate BRFM patterns that is assigned.

Cluster#	Number of				Attributes			- Dottoma
Cluster#	Customers	R _P	F _P	Μ	R _s	Fs	NoC	Patterns
1	20 (13%)	73.85	1.95	3755.75	71.3	1.6	103.65	$\downarrow\downarrow\downarrow\downarrow\downarrow\downarrow\downarrow\downarrow\downarrow$
2	24 (15%)	78.21	3.13	6566.08	34.0833	5.25	369.17	↓↑↑↑↑↑
3	11 (7%)	27.64	7	14502.27	13.9091	7.64	436.09	<u> </u>
4	21 (14%)	24.71	2.10	2732.43	23.4286	2.10	162.14	↑↓↓↑↓↓
5	22 (14%)	29.77	2.59	4312.55	14.8636	4.36	292.55	$\uparrow \downarrow \downarrow \uparrow \uparrow \uparrow$
6	20 (13%)	128.35	1.65	3840.15	128.35	1.7	129.35	$\downarrow\downarrow\downarrow\downarrow\downarrow\downarrow\downarrow\downarrow\downarrow$
7	14 (9%)	20.21	3.57	21774.36	19	2.5	138.5	$\uparrow\uparrow\uparrow\uparrow\downarrow\downarrow$
8	23 (15%)	126.09	2	5500.96	42.8261	4.17	278.87	$\downarrow\downarrow\downarrow\uparrow\uparrow\uparrow\uparrow$
Full Data	(155)	68.271	2.729	6791.2839	45.3806	3.529	235.5548	

 Table 3. Eight Resulted Clusters Using BRFM

For Recency attributes (Rp and Rs), if the average value of Recency of cluster is lower than the overall average value of Recency in the data set, it is considered as high Recency of purchase or visit and cluster will take upward (\uparrow) Recency pattern. When the average value of Recency exceeds the average of total Recency values in the data set, cluster will take downward (\downarrow) Recency pattern. That because the negative relationship between the Recency (of purchase or session) and the customer value (i.e. small numbers of days since last purchase or session date means more recent behavior and consequently high customer value, and high number of days since last purchase or session date means low recency and low customer value).

For the Frequency attributes (F_P and F_s), Monetary attribute (M), and Number of user clicks attribute NoC), they have positive effect on the customer value. High frequency of purchasing and user session, high spends, and a lot of user clicks means high customers' value and loyalty. So, if the average value of Frequency (F_P and F_s), Monetary (M), and Number of clicks (NoC) of cluster exceed the total average of Frequency (F_P and F_s), the Monetary (M), and Number of clicks (NoC) in the data set, then it considered a high F_P , F_s , M, and NoC, and upward (\uparrow) pattern is assigned to these attributes in a cluster. In the opposite case, downward (\downarrow) pattern is assigned for these attributes.

3.3 CLV Ranking

In this subsection, the customer life time value (CLV) of each BRFM cluster is calculated and ranks are assigned. CLV ranking is important to understand the different clusters' value and to clarify the high loyal segment of customers and less loyal ones.

Papers [12] and [13] calculate the CLV of clusters as the total average normalized value of RFM attributes multiplied by their weights, as follow:

 $CLV_{ci} = NR_{ci} * WR_{ci} + NF_{ci} * WF_{ci} + NM_{ci} * WM_{ci}$ (1) Where CLV_{ci} is the customer life time value of cluster *ci*. NR_{ci} . NF_{ci} , and NM_{ci} are the normalized value of RFM of cluster ci. WRci, WFci, and WMci are the relative weights of RFM attributes.

The CLV of each BRFM cluster is calculated as the sum of average normalized value of Rp, Fp, M, Rs, Fs, and NoC attributes as follows, considering that all BRFM attributes have the same relative importance (i.e. WRP, WFP, WM, WRS, WFS, WNoC = 1).

$$CLV_{ci} = NR_{P_{ci}} + NF_{P_{ci}} + NM_{ci} + NR_{S_{ci}} + NF_{S_{ci}} + NNoC_{ci}$$
(2)

Where CLVci is the customer life time value of cluster ci. NRpci, NFpci, and NMpci are the normalized value of Recency of purchasing, Frequency of purchasing, and Monetary of cluster ci, NRsci refers to the normalized value Recency of session attribute in cluster ci, NFsci is the normalized Frequency of session attribute in cluster ci, and NNoCci is the normalized value of NoC attribute of cluster ci.

The normalized value of BRFM attributes in each resulted cluster is calculated based on the Min-Max normalization method [25] as follow:

$$v'_{A} = \frac{v_{A} - min_{A}}{max_{A} - min_{A}} (new_{max_{A}} - new_{min_{A}}) + new_{min_{A}}$$
(3)

Where V'_A is the normalized value of A, V_A is the original value of attribute A, min_A and max_A is the minimum and maximum value of A, new_max_A and new_min_A are the new maximum and minimum value of A, and they are 0 and 1.

The normalization is done to map the value of BRFM attributes to have the same scale range from 0 to 1. From previous equation, the normalized value of BRFM attributes in resulted clusters is calculated as follow:

$$NR_{p_i} = \frac{R_{p_{max}} - R_{p_i}}{R_{p_{max}} - R_{p_{min}}}$$
(4)

$$NF_{p_i} = \frac{F_{p_i} - F_{p_{\min}}}{F_{p_{\max}} - F_{p_{\min}}}$$
(5)

$$NM_{i} = \frac{M_{i} - M_{min}}{M_{max} - M_{Min}}$$
(6)

$$NR_{s_i} = \frac{R_{s_{max}} - R_{s_i}}{R_{s_{max}} - R_{s_{min}}}$$
(7)

$$NF_{s_i} = \frac{F_{s_i} - F_{s_{min}}}{F_{s_{max}} - F_{s_{min}}}$$
(8)

$$NNoC_{i} = \frac{NoC_{i} - NoC_{min}}{NoC_{max} - NoC_{min}}$$
(9)

Where $NRp_{ib} NFp_{ib} NM_i$, $NRs_{ib} NFs_{ib}$ and NMs_i are normalized Recency and Frequency of purchasing, normalized Monetary, normalized Recency and Frequency of session, and normalized Number of clicks of cluster *i*. $Rp_{ib} Fp_{ib} M_{ib} Rs_{ib}$ Fs_{ib} and NoC_i refer to the average value of Rp, Fp, M Rs, Fs, NoC of cluster *i*. While Rp_{max} , $Fp_{max} M_{max}$, $Rs_{max} Fs_{max} NoC$ max, and $Rp_{min} Fp_{min} M_{min}$, $Rs_{min} Fs_{min} NoC_{min}$, represent the largest and smallest value of Rp, Fp, M, Rs Fs, and *NoC* attributes of all customers data.

The Recency variables (Rp and Rs) are normalized using equations (4 and 7) because they have negative impact to CLV (the lower recency of purchasing or session the higher customer value and vice versa). Frequency attributes (Fp and Fs), Monetary, and Number of clicks are normalized using equation (5, 6, 8 and 9) because of their positive affect on CLV (the higher Frequency of purchase, Frequency of session, Monetary, and Number of clicks, the higher customer value).

Table 4 displays the average normalized value of R_p , F_p , M, R_s , F_s , and NoC attributes of each resulted cluster, the CLV of each resulted cluster, and the corresponding cluster Rank.

3.4 BRFM cluster Analysis

In this section, the BRFM clusters are analyzed based on their lifetime value, patterns, and characteristics associated with each cluster and then compared with the traditional RFM to identify the impact of adding the web behavioral attributes to RFM in providing marketers with new categories of customers that deliver a richer customer insight. Different to RFM Model, in which the resulted clusters reflect only the customers' profitability, the BRFM clusters reflect customers' interesting, stickiness, intention to future purchase, and loyalty besides reflecting their profitability. That helps marketers to better understand their customers' behavior and

characteristics, and subsequently propose and deliver more effective target marketing.

The online retailer considered in this study is an enterprise that sells office supplements products such as book cases, tables, office furnishing, chairs, copiers and fax, telephones, papers, pens, etc. The dataset used in this study is available in [26]. The transaction data has 14 attributes: Order ID, Customer ID, User Name, Order Date, Order Quantity, Sales amount, Discount, Unit Price, Shipping Cost, Region, Product Category, Product Name, Ship Date. Part of the transaction dataset is shown in Table 5. The customers' web log files store user clicks streams while navigating the web site and contain the following fields: date and time of log, client-ip, client-username, request type, cs-uri-stem, and HTTP status code as shown in Figure2.

The used data contains one year of transactions that is stored in excel sheet. This data contains 1429 purchases records generated from 155 customers, the web log data of those customers is also used for conducting customer value analysis based on Behavioral RFM attributes.

2012-12-01 00:00:30 172.22.255.255 Neoma Murray Get /home.htm 200 2012-12-01 00:00:30 172.22.255.255 Neoma Murray Get /Technology.htm 200 2012-12-01 00:00:35 172.22.255.255 Neoma Murray Get /Technology/Office Machines.htm 200 2012-12-01 00:00:36 172.22.255.255 Neoma Murray Get /Technology/Office Machines/Epson FX-2180 Wide Format Dot Matrix Printer.htm 200 2012-12-01 00:00:40 172.22.255.255 Neoma Murray Get /Technology/Office Machines/home' Epson DFX5000+ Dot Matrix Printer.htm 200 2012-12-01 00:00:45 172.22.255.255 Neoma Murray Get /Office Supplies.htm 200

Figure 2. Sample of a Web Log File

Table 6 shows eight BRFM clusters when applying the BRFM model on the described data, each cluster is presented with its lifetime value, patterns, and characteristics as follows:

This cluster has the largest CLV, it contains 7% of all customers who are considered as golden customers as they are the most profitable, loyal, and interested customers to the company. They have purchased recently and make frequent purchases with big spends. They also have visited the web site recently, and they visit the site frequently and perform a lot of clicks. This indicates high interesting, stickiness, loyalty, and value. So, this cluster should be the target that company aims to push all of its customers toward it.

• Cluster 7 Rank 2 ↑↑↑↑↓↓ (High profitability, less stickiness &loyalty)

This cluster has the next largest rank, it contains 9 % of customers. Customers in this segment have high purchasing indices, they have purchased recently and do a lot of purchases with high spends, but they are not frequent visitors and make a few clicks which mean low stickiness, interesting, and loyalty to the company. In traditional RFM, customers in this cluster are considered to be loyal and have same value as customers in Cluster 3 Rank 1 ($\uparrow\uparrow\uparrow\uparrow\uparrow\uparrow$), this is because they have high profitability and same purchasing patterns ($\uparrow\uparrow\uparrow$).

	Number								
Cluster#	of customers	R _p	Fp	М	Rs	Fs	NoC	CLV	Rank
1	20 (13%)	0.5715	0.1056	0.0906	0.5522	0.075	0.1128	0.5715	7
2	24 (15%)	0.5458	0.2361	0.1587	0.7893	0.5313	0.5620	2.8233	4
3	11 (7%)	0.8433	0.6667	0.3512	0.9178	0.8296	0.6753	4.2837	1
4	21 (14%)	0.8605	0.1217	0.0658	0.8571	0.1369	0.2117	2.2538	5
5	22 (14%)	0.8307	0.1768	0.1041	0.9117	0.4205	0.4324	2.8762	3
6	20 (13%)	0.2509	0.0722	0.0926	0.1889	0.0875	0.1563	0.8484	8
7	14 (9%)	0.8870	.2857	.5275	.88535	.1875	.1717	2.9448	2
8	23 (15%)	0.2642	0.12	0.1329	0.7336	0.3967	0.4093	2.0567	6

Table 4. CLV BRFM Rank-Based

Table 5. Part of Transaction Dataset

Order ID	Customer ID	User Name	Order Date	Order Quantity	Sales amount	Discount	Unit Price	Shipping Cost	Product Category	Product Name	Ship Date
37218	21	Frank Merwin	12/19/2012 01:09:30	23	153.02 USD	0.08	6.48 USD	5.82 USD	Office Supplies	Xerox 1998	12/20/2010
50307	40	Bill Overfelt	10/15/2012 12:18:30	31	542.01 USD	0.06	17.48 USD	1.99 USD	Technology	Maxell Pro 80 Minute CD-R, 10/Pack	10/15/2010
57314	51	Patrick O'Brill	10/12/2012 07:10:01	26	2238.5 USD	0	85.99 USD	2.79 USD	Technology	6340	10/19/2010
27232	60	Ralph Arnett	8/18/2012 06:05:12	19	671.59 USD	0.05	34.99 USD	7.73 USD	Office Supplies	Hunt Boston® Vacuum Mount KS Pencil Sharpener	8/20/2010
22820	77	Craig Yedwab	8/17/2010 14:09:20	18	144.84 USD	0	7.89 USD	2.82 USD	Office Supplies	Staples Vinyl Coated Paper Clips, 800/Box	8/20/2010

Table 6. The Characteristics of BRFM Resulted Clusters

	Number	er Attributes									
Cluster #	of customer s	R _P	F _P	Μ	Rs	Fs	NoC	patterns	CLV	Rank	Characteristics
1	20 (13%)	0.571	0.106	0.091	0.552	0.075	0.113	$\downarrow \downarrow \downarrow \downarrow \downarrow \downarrow \downarrow \downarrow \downarrow$	1.39	7	Low profitability & loyalty
2	24 (15%)	0.546	0.236	0.159	0.789	0.531	0.562	$\downarrow\uparrow\uparrow\uparrow\uparrow\uparrow$	2.26	4	Low recency, high profitability & loyalty
3	11 (7%)	0.843	0.667	0.351	0.918	0.829	0.675	$\uparrow\uparrow\uparrow\uparrow\uparrow\uparrow$	3.61	1	Golden customers
4	21 (14%)	0.861	0.122	0.066	0.857	0.137	0.212	$\uparrow \downarrow \downarrow \uparrow \downarrow \downarrow$	2.04	5	High recency, low loyalty & profitability
5	22 (14%)	0.831	0.177	0.104	0.912	0.420	0.432	$\uparrow \downarrow \downarrow \uparrow \uparrow \uparrow$	2.44	3	High recency, low profitability & high interesting
6	20 (13%)	0.251	0.072	0.093	0.189	0.088	0.156	$\downarrow \downarrow \downarrow \downarrow \downarrow \downarrow \downarrow \downarrow \downarrow$	0.69	8	Least valuable
7	14 (9%)	0.887	0.286	0.527	0.885	0.186	0.172	$\uparrow\uparrow\uparrow\uparrow\downarrow\downarrow\downarrow$	2.77	2	High profitability, less stickiness &loyalty
8	23 (15%)	0.264	0.12	0.133	0.734	0.397	0.409	$\downarrow\downarrow\downarrow\uparrow\uparrow\uparrow\uparrow$	1.65	6	Low profitability & high loyalty
Full data	(155)	0.604	0.192	0.164	0.717	0.316	0.336				

Although both clusters have high profitability and same purchasing patterns, customers in this cluster have visited the web site just few times, and did not request a lot of pages to view as customers in Cluster Rank $1(\uparrow\uparrow\uparrow\uparrow\uparrow\uparrow\uparrow)$, that indicate low interesting, low stickiness and willing to know about the company's product, and low loyalty.

Figure 3 shows an example of the customers' division from cluster 3 Rank 1 ($\uparrow\uparrow\uparrow$) using RFM model into two different new clusters with different characteristics using the BRFM.

As shown in Figure 3 customers in cluster 3 rank 1 ($\uparrow\uparrow\uparrow$) using RFM are similar to each other in their purchasing behavior, but they have different web behavior characteristics which reflect their interesting, stickiness, and loyalty to the company. So, customers are split into two different clusters using the BRFM Cluster 3 Rank 1 ($\uparrow\uparrow\uparrow\uparrow\uparrow\uparrow$) and Cluster 7 Rank 2 ($\uparrow\uparrow\uparrow\uparrow\uparrow\downarrow\downarrow\downarrow$), where customers in each new BRFM cluster are more similar to each other in their purchasing and in their behavioral loyalty than the previous clustering using RFM.

• Cluster 5 Rank 3 \\\\\\\ (High purchase recency, low profitability and high interesting)

This cluster has the third CLV rank and formed with 14% of all customers. Customers in this cluster have purchased recently, and make few number of purchases with little contribution to the company profit. Although the small purchases and spends of customers in this cluster, their web behavior indices indicate high interesting and loyalty to the company, they frequently visit the web site and make a lot of clicks which indicate high stickiness, interesting and intention for future purchases.

Cluster 2 Rank 4 ↓↑↑↑↑↑↑ (Low recency, high profitability and high loyalty)

This segment takes rank 4 and contains 15 % of all customers. Customers of this cluster are profitable and loyal but they didn't make purchases recently.

Comparing with the traditional RFM which consider those customers are churned to competitors, using the web behavioral attributes reveal that they are still visiting the web site and still interested in the company which indicate an intention to make future purchase. On another side, web behavior data may insure the idea that customers are churned to competitors if the web behavior patterns show that customers didn't visit web site recently and frequently.

	$\frac{\text{RFM: Cluster 3 Rank 1 (\uparrow\uparrow\uparrow)}}{\text{RFM: Cluster 3 Rank 1 (\uparrow\uparrow\uparrow)}}$														
	ID Customer name								R	F	М				
			1392	3	Ed Braxton]	2/7/2012	9 2	8666				
	31270 Michelle Lonsdale						1	1/23/2012	8 2	28416					
16134 Nathan Mautz							1	1/19/2012	3 2	21804					
			7423	7	Ricardo	o Emerso	n	1	2/15/2012	4 1	7731				
	BR	FM: Cluster	3 Rank	: 1 (<u>†</u> †††	<u>(</u>)				BRFN	1: Cluster 7 R	ank 2	(↑↑↑↑↓↓)			
ID	Customer name	R	F	М	Rs	Fs	NoC	ID	Customer name	R	F	М	Rs	Fs	NoC
13923 Ed Braxton 12/7/2012 9 28666 12/7/2012 10 524						524	7427	Ricardo Emerson	12/15/2012	4	17731	12/15/2012	2	166	
31270	Michelle Lonsdale	11/23/2012	8	28416	12/11/2012	9	494	16134	Nathan Mautz	11/19/2012	3	21804	11/19/2012	3	58
		-		_							-				

Fig 3: Split of customers in same cluster using RFM in two different clusters with different characteristics using BRFM

• Cluster 4 Rank 5 $\uparrow \downarrow \downarrow \uparrow \downarrow \downarrow$ (High purchase recency, low profitability and low loyalty)

This cluster Takes rank 5 with 14% of all customers. Compared to traditional RFM model, which considers customers in this cluster as cluster having the same value as customers in cluster 5 rank 3 ($\uparrow\downarrow\downarrow\uparrow\uparrow\uparrow$) based on their profitability and purchasing patterns. BRFM attributes distinguish customer in this cluster from cluster 5 rank 3 ($\uparrow\downarrow\downarrow\uparrow\uparrow\uparrow$). Customers in this cluster are less loyal than customers in cluster 5 Rank 3 ($\uparrow\downarrow\downarrow\uparrow\uparrow\uparrow\uparrow$). They visit the web site just few times and react to the website with few number of clicks which mean lower interesting and loyalty to the company.

• Cluster 8 Rank 6 ↓↓↓↑↑↑ (Low profitability and high loyalty)

Customers in this cluster have low profitability and purchasing patterns and high behavioral loyalty. They visit the web site recently, frequently and do a lot of clicks. Traditional RFM considers customers who have low RFM patterns $(\downarrow\downarrow\downarrow)$ are lost and no effort should be taken with them.

According to RFM approach, customers of this cluster have the same value as customers in both cluster 1 ranked with 7 $(\downarrow\downarrow\downarrow\downarrow\downarrow\downarrow\downarrow)$ and cluster 6 ranked with 8 $(\downarrow\downarrow\downarrow\downarrow\downarrow\downarrow\downarrow)$, that because all have the same low purchasing pattern. BRFM Model differentiates customers of this cluster from customers in cluster 1 ranked with 7 $(\downarrow\downarrow\downarrow\downarrow\downarrow\downarrow\downarrow)$ and cluster 6 rank with 8 $(\downarrow\downarrow\downarrow\downarrow\downarrow\downarrow\downarrow\downarrow)$. Although all of these clusters have low profitability purchasing patterns, customers in this cluster are highly interested in the company and they have high web behavior loyalty. So, they shouldn't be treated as customers in cluster 1 ranked with 7 $(\downarrow\downarrow\downarrow\downarrow\downarrow\downarrow\downarrow)$ and cluster 6 ranked with 8 $(\downarrow\downarrow\downarrow\downarrow\downarrow\downarrow\downarrow)$ who have low profitability and low web behavior patterns.

Figure 4 shows the split of customers who were clustered in cluster 4 rank 8 with pattern $(\downarrow\downarrow\downarrow\downarrow)$ using the RFM to two different clusters with different characteristics and different value using BRFM.

As shown in Figure 4, customers in cluster 4 rank 8 ($\downarrow\downarrow\downarrow$) using RFM model have low value and low purchasing pattern. Using the BRFM model divide customers in this cluster into two different clusters with different web behavioral characteristics. Customers in each new cluster (cluster 6 rank 8 ($\downarrow\downarrow\downarrow\downarrow\downarrow\downarrow\downarrow\downarrow$) and cluster 8 rank 6 ($\downarrow\downarrow\downarrow\downarrow\uparrow\uparrow\uparrow$)) are more similar to each other in their purchasing and their web behavioral patterns.

• Cluster 1 Rank 7 ↓↓↓↓↓↓ (Low profitability and Low loyalty)

Customers in this segment have low purchasing indices and low behavioral loyalty, they didn't purchase recently, make few purchases, and their spending is low. Moreover, they rarely visit the web site and make few clicks. So, this segment is considered unprofitable and disloyal. Different to the previous cluster 8 rank 6 ($\downarrow\downarrow\downarrow\uparrow\uparrow\uparrow\uparrow$), customers in this cluster are less valuable because they have low web behavioral patterns.

• Cluster 6 Rank 8 \\\\\\\\\\\\

This cluster has the least value rank and contain 13% of all customers. Customers in this cluster have same pattern as cluster 1 rank 7 ($\downarrow\downarrow\downarrow\downarrow\downarrow\downarrow\downarrow\downarrow$), they didn't purchase recently, make few purchases, and their spending is low, also they rarely visit the web site and make few clicks, so they are considered unprofitable, not interested in the company. But they have lower average value in Rp, Fp, and Rs attributes than cluster 1 rank 7 ($\downarrow\downarrow\downarrow\downarrow\downarrow\downarrow\downarrow$) as shown in Table 6, so this cluster takes rank eight.

After this analysis, we can conclude that using the BRFM model and adding the Rs, Fs, and NoC attributes to RFM model can reveal new categories of customers that are not shown using traditional RFM as follow:

- Customers who may still be interested in companies' products and loyal to it even if they didn't make recent purchase.
- Low profitable customers who are very interesting in the company's product, and willing to know more about its' products, which indicate high probability of future purchases.
- 3) Low profitable customers who are rarely visit the website, not interested in the company, and disloyal.
- 4) Profitable customers who purchased a lot but not frequent visitors and do not view a lot of web site pages, which indicate lower interesting, loyalty and stickiness than customers in the following next category,
- 5) Profitable customers who are very loyal, sticking and interested in the company.

These categories provide companies with a rich customer value insight, which help them to understand the customers' web behavior and their purchasing pattern, and targeting them with more effective marketing strategies based on this insight to maximize the customers' future value and loyalty.



Fig 4: Customers' transition from cluster 4 rank 8 (↓↓↓) using RFM into cluster 6 rank 8 (↓↓↓↓↓↓) and cluster 8 rank 6 (↓↓↓↑↑↑) using BRFM.

4. BRFM EVALUATION

To evaluate the effectiveness of Behavioral RFM model over the traditional RFM model, we applied the traditional RFM model for customer segmentation using K-means clustering algorithm. The effectiveness of BRFM model is tested using Dunn index and Davies Bouldin to test the validity and accuracy of the customer segmentation using the BRFM Model in comparison with the RFM Model.

4.1 Dunn Index Evaluation

Dunn Index is one of the clustering validity measures that aims to evaluate the accuracy and validity of the resulted clusters based on the intra-cluster and inter-cluster distance measures [27, 28, 29].

Several Dunn index equations are found in literature. These equations are different in defining the inter-cluster and intracluster distance, and in placing the intra and inter-cluster distance in the denominator and numerator of equation.

In this section, three methods to calculate the Dunn Index are used to evaluate the accuracy and validity of clustering results based on RFM and BRFM and to verify the results.

A. First Method to Calculate Dunn Index:

This method is the most popular to calculate Dunn index as provided in (27, 28, 29, 30). This method defines Dunn Index as the ratio of the smallest distance between two observations that are not in the same cluster to the largest intra-cluster distance between observations in the same clusters as shown in equation (10).

 $D = min_{i=1...n_c} \left\{ min_{j=i+1,...,n_c} \left(\frac{d(c_i,c_j)}{max_{k=1...n_c}(diam(c_k))} \right) \right\}$ (10) Where: $d(c_i,c_j) = min_{x \in C_i, y \in C_j} \left\{ d(x,y) \right\}$ (11) $(diam(c_k)) = max_{x,y \in C_k} \left\{ d(x,y) \right\}$ (12)

Where *D* is Dunn index. n_c refer to number of clusters. *d* is distance based on Euclidian distance, $d(c_i, c_j)$ refer to the minimum inter distance between two clusters by measuring the distance between their closest points. (*Diam* (c_k)) refer to the maximum intra cluster distance. *d* (x, y) refer to distance between two data elements in same cluster.

The best clustering method that maximizes the inter-cluster distance (the numerator in this method) while minimizing the intra-cluster distance (the denominator in this method). So, the larger Dunn Index value means more after accurate cluster segmentation. The minimum distance between two customers in different clusters (inter-cluster distance) in RFM and BRFM is shown in Table 7, and the maximum distance between customers in same cluster (intra-cluster distance) in RFM and BRFM method is provided in Table 8.

As shown in Table 7, the maximum intra-cluster distance between customers in same cluster using RFM attributes is 34830, and the maximum intra-cluster distance between customers in same cluster using BRFM attributes is 30524. The Behavioral RFM minimize the maximum intra cluster distance between customers in same cluster than RFM.

In Table 8, minimum inter cluster distance in RFM is 3.648616176 and the minimum inter cluster distance in BRFM is 21.52436, which means that the BRFM maximize the minimum inter distance between clusters than using RFM attributes.

After getting the minimum inter-cluster distance in RFM and BRFM as shown in Table 7 and the maximum intra- cluster distance in RFM and BRFM as shown in Table 8, we calculate the Dunn Index for RFM and BRFM as follows:

Dunn Index in RFM=
$$\frac{3.648616176}{34830} = 0.0001$$

Dunn Index in BRFM= $\frac{21.82436}{30524.13} = .001$

Based on the previous two equations, the Dunn Index of RFM is 0.0001 and .001 for BRFM. The larger value of Dunn Index achieved by using the BRFM attributes in customer segmentation, which means that using BRFM attributes in customer segmentation lead to better clustering accuracy which increase the intra cluster compactness and inter-cluster separation than using the RFM.

B. The Second Method to Calculate Dunn Index

The second equation of Dunn Index is provided in [13]. This method is similar to the first method in the formation of Dunn Index equation. It is the ratio of minimum inter-cluster distance to maximum intra-cluster distance, but the difference is in the definition of inter-cluster and intra-cluster distance.

In this method, the minimum inter-cluster distance is the minimum distance between the mean of two clusters rather than the minimum distance between elements in two clusters. The maximum intra-cluster distance is calculated as the maximum distance between observations and their cluster center rather than the distance between observations in same cluster.

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	Min inter clusters	distance in R	FM		Min inter cluste	rs distance ir	n BRFM
D12	377.63871623	D35	139.150997	D12	289.9413734	D35	34.92849839
D13	69.921384426	D36	3.64861617	D13	141.4991166	D36	51.33755058
D14	1073.6726689	D37	72.5603197	D14	197.3702105	D37	76.65749539
D15	66.015149776	D38	115.524889	D15	226.0707854	D38	152.3257119
D16	326.33294409	D45	404.8370042	D16	243.9241685	D45	81.92679659
D17	279.38145965	D46	26.75817632	D17	158.0537883	D46	71.47726911
D18	1167.0132836	D47	20.46948949	D18	169.4461566	D47	182.4033991
D23	301.9453593	D48	75.63729239	D23	153.4763825	D48	183.697469
D24	92.33634171	D56	177.2879285	D24	739.6654649	D56	85.75887184
D25	189.4069692	D57	29.76575213	D25	377.0716112	D57	21.82435566
D26	80.38034586	D58	164.9566128	D26	292.0256838	D58	142.5736708
D27	90.04998612	D67	39.06404997	D27	94.3980932	D67	81.46778504
D28	31.63858404	D68	56.25157776	D28	224.1048862	D68	73.50314551
D34	33.2565783	D78	21.72869992	D34	85.12343978	D78	83.0722577
The minim RFM	um Min inter-cluster	rs distance in	3.64861617	The minim in BRFM	um Min inter-clus	ters distance	21.82435566

Table 7. The Minimum Inter Cluster Distance in RFM and BRFM Using Dunn 1st Method.

Table 8. The Maximum Intra Cluster Distance in RFM and BRFM Using Dunn 1st Method

The max intra c	luster distance	The max intra cluster				
in RFM		distance in BRFM				
D1	34830	D1	25723.26			
D2	18795.02	D2	30524.13			
D3	11256.01	D3	11268.74			
D4	8464.005	D4	15571.16			
D5	16272.64	D5	10788.75			
D6	7119.2	D6	23430.61			
D7	7286.43	D7	18853.39			
D8	9391.12	D8	21120.61			
Max intra Dist	34830.00352	Max intra Dist	30524.13			

$$D = \frac{\min_{i,j=1,\dots,k, i\neq i} \delta(C_i, C_j)}{\max_{i=1,\dots,k} \Delta(c_i)}$$
(13)

$\delta(C_i, C_j) = d(\overline{c_i}, \overline{c_j})$	(14)
$\Delta(\mathbf{c}_{i}) = max_{x \in c_{i}}d(x, \bar{c}_{i})$	(15)

Where δ (C_i , C_j) is the inter distance between clusters, Δ (C_i) is the intra-cluster distance of cluster C_i , and k refers to the total number of clusters, \overline{c}_i , \overline{c}_j are the center of cluster C_i and C_j . Similar to previous method, the larger Dunn index value means more accurate clustering result.

The minimum inter-cluster distance between the centroid of two clusters in RFM and BRFM is shown in Table 9, and the maximum intra-cluster distance between observations and the centroid of same cluster in RFM and BRFM is provided in Table 10.

According to Table 9, the minimum inter cluster distance in RFM is 46.51 and the minimum inter cluster distance in BRFM is 118.3, which means that BRFM maximize the minimum inter distance between clusters more than using RFM as the previous method.

The maximum intra-cluster distance between the observations in a cluster and the centroid of this cluster as shown in Table 10 is 22068.87 using RFM, and 19488.66 using BRFM. So, the BRFM minimize the maximum intra cluster distance than using the RFM attributes. Based on the minimum inter-cluster distance in RFM and BRFM as shown in Table 9, and the maximum intra- cluster distance in RFM and BRFM as shown in Table 10. The Dunn Index for RFM and BRFM approach is calculated as follows:

Dunn Index in RFM=
$$\frac{46.51}{22068.87098}$$
 = .002

Dunn Index in BRFM= $\frac{118.36}{19488.66}$ = .006

Dunn Index of RFM is 0.002 and .006 for BRFM. The Dunn Index value is larger in BRFM than RFM, which means that BRFM increases the validity and accuracy of the clustering results than RFM.

C. The Third Method to Calculate Dunn Index

The third equation of Dunn Index is provided in [16]. This method is different than previous two methods in the formation of Dunn index equation. The numerator of Dunn index equation in this method is the intra- cluster distance and the denominator is the inter-cluster distance.

Similar to the second method of Dunn index, the inter cluster distance is calculated as the distance between the means of two clusters, and the intra cluster distance is calculate as the distance between mean of the cluster and other objects in the same cluster.

$$D_{ij=\frac{max(dist in c_i)}{dist(c_i, c_j)}} \qquad i \neq j \text{ and } 1 \le i, j \le k \quad (16)$$

This equation is calculated k*(k-1) times for each pairwise of clusters [16]. In our case, for RFM and BRFM, Dunn Index equation will be calculated 8*(8-1) times, and the maximum Dunn index in RFM is compared with the maximum Dunn index in BRFM.

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	Min inter clusters	distance	in RFM	Min i	nter clusters dista	ance in BI	RFM
D12	8281.060102	D35	8748.82	D12	7278.18	D35	1585.52
D13	14941.43444	D36	2251.94	D13	10190.74	D36	1192.71
D14	15628.85951	D37	2263.72	D14	7936.66	D37	592.32
D15	6193.286901	D38	2250.81	D15	11773.04	D38	521.91
D16	17193.14511	D45	9435.98	D16	9003.28	D45	3839.63
D17	17203.81896	D46	1564.30	D17	10751.92	D46	1070.06
D18	17189.11	D47	1575.45	D18	10667.63	D47	2823.10
D23	6662.19	D48	1562.38	D23	17462.49	D48	2738.55
D24	7348.98	D56	11000.28	D24	15210.14	D56	2772.91
D25	2087.87	D57	11010.73	D25	19041.94	D57	1027.28
D26	8913.23	D58	10995.90	D26	16274.37	D58	1117.98
D27	8923.43	D67	50.00	D27	18018.80	D67	1754.99
D28	8908.40	D68	93.03	D28	17934.87	D68	1669.72
D34	688.43	D78	46.51	D34	2255.44	D78	118.36
The minimum Min inter clusters distance in RFM 46.51					inimum Min inter clu	sters distanc	ce in BRFM 118.36

Table 9. The Minimum Inter Cluster Distance in RFM and BRFM Using Dunn 2nd Method.

Table 10. The Maximum Intra-cluster Distance in RFM and BRFM Using Dunn 2nd Method

The max intra cluster distance in RFM		The max intra cluster distance in BRFM		
D1	22068.87098	D1	14164.00	
D2	10235.21943	D2	19488.66	
D3	7191.315251	D3	7131.47	
D4	6100.706447	D4	9571.14	
D5	10580.51202	D5	8074.73	
D6	5137.361559	D6	18081.13	
D7	5339.566051	D7	15141.25	
D8	7414.399603	D8	17308.94	
Max intra Dist	22068.87	Max intra Dist	19488.66	

The clustering which has minimum of the maximum Dunn index is chosen as the best clustering.

The maximum Dunn Index of RFM is 159.411 and 146.24 for BRFM. Based on this method, the minimum of maximum Dunn index value is obtained using the BRFM. As a result, BRFM model leads to more accurate clustering results than RFM.

4.2 Davies-Bouldin Evaluation

The proposed BRFM model is further evaluated in comparison with RFM model using Davies-Bouldin measure. Davies-Bouldin is one of the clustering validity measures based on the intra-cluster and inter-cluster distance measures to identify clusters which are compact and well separated (Davies & Bouldin, 1979; 27).

$$DB = \frac{1}{k} \sum_{i=1}^{K} \max_{1 \le j \le k, j \ne i} \left(\frac{\operatorname{diam}\left(c_{i}\right) + \operatorname{diam}\left(c_{j}\right)}{\operatorname{dist}\left(c_{i}, c_{j}\right)} \right)$$
(17)

Where K is the number of clusters, *diam* (c_i) is the average distance of all patterns in cluster i to their cluster center ci, *diam* (c_j) is the average distance of all patterns in cluster j to their cluster center cj , and *dist* (c_i , c_j) is the distance of cluster centers ci and cj . Small values of Davies-Bouldin means more compact and well separated clusters. Table 11 shows the average intra-cluster distance in each cluster using RFM and BRFM, and the inter-cluster distances between the center of clusters in RFM and BRFM is the same as values supported in Table 9.

Table 11.	Average Intra Cluster Distance in RFM and	d
	BRFM using Davies-Bouldin	

Avg. intra-cluster distance in RFM		Avg. intra-cluster distance in BRFM	
K1	6658.368156	K1	6382.451774
K2	7353.444634	K2	5850.320844
K3	2985.402501	K3	2239.673115
K4	1294.376223	K4	3989.292588
K5	3487.285751	K5	2044.541924
K6	1896.518806	K6	5145.444613
K7	1615.587372	K7	4335.850478
K8	1455.18994	K8	4105.018154

After getting the average intra cluster distance in each cluster and the inter-cluster distances between clusters in RFM and BRFM, the Davies-Bouldin measure is calculated for RFM and BRFM based on equation (17). Davies-Bouldin in RFM is 51.91and 22.67 in BRFM. The BRFM Model minimizes the intra cluster distance and maximizes the inter distance between clusters, and result in more accurate and compact clusters that are well separated than RFM model.

5. RESULTS DISCUSSION

The accuracy and validity of the clustering results based on RFM attributes and the Behavioral RFM attributes is tested based on Dunn index and Davies Bouldin measure. Table 12 summarizes the results of evaluating the accuracy and validity of clustering results in RFFM and BRFM using three different methods to calculate the Dunn Index measure and Davies Bouldin measure.

Based on the three mentioned methods for Dunn Index calculations, using BRFM in customer segmentation satisfies the criteria of choosing the best clustering configuration. When using the first and the second equations, the clustering method with larger Dunn index value is the best. Dunn index of clustering results using BRFM attributes is .001 in first equation and .006 in second equation which is larger than Dunn index value of RFM that is .0001 in first equation and .002 in second equation. In the third equation, the best clustering method has the minimum of the maximum Dunn index value. The maximum Dunn index value of clusters using BRFM attributes is146.24 and smaller than the maximum Dunn index of RFM clusters which is 159.11.

Method	Criteria of choosing the best clustering	RFM	BRFM	
1 st Equation Dunn	larger value of Dunn Index	.0001	.001	iteria
2 nd Equation Dunn	larger value of Dunn Index	.002	.006	sfy the cr
3 rd Equation Dunn	The minimum of the maximum Dunn index.	159.11	146.24	Sati
Davies- Bouldin	Minimum value of Davies- Bouldin	51.91	22.67	

Table 12. Summary of Dunn Index Evaluation Results

In Davies-Bouldin measure, the more accurate clustering result is that minimizes the value of Davies-Bouldin. The value of Davies-Bouldin in BRFM is 22.67 and it is smaller than the value of Davies-Bouldin in RFM which is 51.91.

It can be concluded that adding the three web behavioral attributes represented in the Recency of session, Frequency of session, and Number of clicks to the traditional RFM attributes enhances the validity and accuracy of customer value segmentation than using the RFM. Using BRFM attributes result in more intra-cluster compactness and well inter-cluster separation than RFM, where customers in the same cluster are more similar to each other and more separate from customers in other clusters.

6. CONCLUSION AND FUTURE WORK

In this paper, a new model called Behavioral RFM (BRFM) is proposed for providing richer customer insight and enhanced view of customers in online market, where three web behavioral attributes represented in Recency of session (Rs), Frequency of session (Fs), and Number of clicks (NoC) are added to the traditional purchasing RFM attributes for customer segmentation, and then the value of customers in the BRFM resulted clusters are calculated.

BRFM resulted clusters are analyzed to understand the characteristics of each cluster, and then they are compared to the traditional RFM model. While RFM clusters reflect customers' purchasing patterns and their profitability, the BRFM clusters provide marketers with a rich customer insight that reflects customers' interests, stickiness, intention to future purchase and loyalty besides reflecting their profitability. This is done through presenting new categories of customers are not shown using traditional RFM. These new categories are illustrated in how recently the customers visit the web site, and number of their visits and browsing behavior, besides their purchasing and spend behavior. These new customer clusters help marketers to better understand their customers' behavior and value to put more effective marketing strategies, and develop long-term profitable relationship with them

The effectiveness of the proposed BRFM model is evaluated against the RFM model using Dunn index and Davies Bouldin measure to test the validity and accuracy of the customer segmentation. Results show that the BRFM model results in more accurate clustering that maximizes the intra cluster compactness and the inter cluster separation than RFM model.

For future work, other web behavioral attributes may be added to the Behavioral RFM model is such as date of registration, duration of session, and number of customer complaints which may enhance the accuracy of customer segmentation.

Moreover, this study provides marketers with richer insight into their customers' value and characteristics concerning their web behavior and their profitability. Proposing and delivering the most suitable marketing strategies for customers based on the characteristics of the cluster they belong to is also considered a future work to maximize customers' value and loyalty to the company.

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