ABSTRACT
Algorithms for Blind Audio Source Separation (BASS) in time domain can be categorized as based on complete decomposition or based on complete decomposition. Partial decomposition of observation space leads to additional computational complexity and burden, to minimize resource requirement complete decomposition technique is preferred. In this script an optimized divergence based ICA technique is proposed to perform ICA decomposition. After decomposition components having similar behaviour are grouped in form of clusters and source signals are reconstructed. The authors implemented complete decomposition for BASS using ICA methods and K-mean cluster technique is introduced. For performance evaluation a three source and three microphones combination is used and result advocates complete decomposition by optimized ICA is a better option than other methods in competition for audio source separation in blind scenario.

General Terms
Blind Audio Source Separation, Independent Component Analysis, Unsupervised Learning

Keywords
Blind Source Separation, Complete Decomposition, Clustering, K-mean Clustering

1. INTRODUCTION
There are various emerging applications in the field of signal processing like Humanoids, Human Machine Interactions (HMI), speech communication for distant talking, hearing aids for deaf peoples and many more [1]. A blind Audio Source separation technique plays a vital role and beholds a very promising future. The ultimate objective of BASS is to estimate a audio sources from their convolutive mixture obtained by recording the "m" microphones. The mixed signals are termed as observed signals y1(p), y2(p), . . . , yn(p).

which depicts a blind scenario of mixing of source signals S1(p), S2(p), . . . , Sn(p).

\[ y_j(n) = h_j(n) \otimes S_j(n) \] (1)

Where hj(n) is impulse response of microphones. There are three kind of mixing mechanism; if “i”=”j” critically determined, if “i”<”j” under determined and if “i”>”j” over determined [2].

The source separation process is analogous to identifying a linear process, which includes estimation of filter coefficients. So, those audio sources can be estimated by applying blind deconvolution process [3].

\[ \hat{S}_j(n) = w_j(n) \otimes y_j(n) \] (2)

The BASS can be performed in time domain and in frequency domain as well. In frequency domain source separation approach signals needs to be transformed in frequency domain using Discrete Fourier Transform (DFT) [3]-[4]. According to properties of DFT the convolution process in (1) and (2) converts in simple multiplication [5]. This process derives convolution model in instantaneous mixture of complex valued function for each frequency component. The frequency domain technique facilitates computation of long separating filter coefficient, which is definitely suitable for audio applications. But for the estimation of long filter coefficient the recording length should be long to generate sufficient amount of data for each frequency component [6].

In time-domain techniques the convolution model derived into an instantaneous form by introducing matrices or data vectors and the convolutive process is simply converted into a matrix multiplication process. Matrices are defined from available signal data captured by microphones and considered as observation space. Generally a matrix is defined so that its rows contain the time-delayed copies of signals received from microphones. The objective of time domain ICA decomposition is to find out subspace that corresponds to separated signals [7]. The observation space can be decomposed completely or partially [8]. In complete decomposition the original signals are represented as “n” independent subspaces covering the entire observation space. In partial decomposition signals are considered as one dimensional subspace.

The problem of complete decomposition can be shorted out with certain limitations. The decomposition matrix could have some special structure, as explained by Belouchrani et al. [9] or as explained by Kellermann et al in form of block-Toeplitz [10]. Fevotte introduced a decomposition method using two stages [11]. There is an assumption with constrained complete decomposition, that there should be same dimension for each independent subspace, which is a potential drawback. The unconstrained based complete decomposition can be considered as an alternative, which an effective way for proper utilization of available data but this process becomes bit lengthy [12]. The important finding of [12] is, when this method implemented with joint block diagonalization (JBD) the algorithm fails for data belongs with long observation space.

In this paper, a fast weight initialized divergence based ICA algorithm is proposed for partial unconstrained decomposition. The proposed method for BASS involved an efficient reconstruction mechanism, when the separation filters having similar length as the mixing one. In this paper computational complexity is taken into account and observation space is created for critically determined samples. The expectation from proposed method is to obtain better result than other competitors. Proposed method provides room for further improvement, especially for real time applications.
The remaining paper is organized as follows. Section II gives a detailed description of completed and partial decomposition method. Section III includes the basic structure of proposed method that include decomposition, proposed ICA procedure and reconstruction method. The simulation and result validation along with result analysis is given in Section IV. Final conclusion drawn along with limitations and future possibilities are described in final Section V.

2. REVIEW OF PARTIAL AND COMPLETE DECOMPOSITION

In time domain discrete convolution is transformed into matrix multiplication. Suppose there are two matrices Y and S having the block-Toeplitz structure. The dimension of matrices is \( n \times (M-L+1) \); where \( L \) is the required length of filter for demixing. The linear space enclosed is considered as observation space. The structure of matrix \( Y \) is as follows.

\[
Y = \begin{bmatrix}
y_1[1] & \ldots & y_1[M-L+1] \\
y_1[L] & \ldots & y_1[M]
y_2[L] & \ldots & y_2[M]
\end{bmatrix}
\]

Figure 1 Decomposition Matrix

Using this notation for both \( Y \) and \( S \) the equation (1) reduced to;

\[
Y = HS
\]

With the use of ICA proposed in next section the coefficients of demixing filter \( W \) can be estimated, which can be directly applied over transform of equation (2)

\[
S" = W \cdot Y
\]

The ICA procedure for separating audio sources from mixture can be classified on the basis of whether; partial or complete decomposition performed over available observation space.

One dimensional component (subspace) is estimated in the partial decomposition method. The partial decomposition method makes easier growth in dimensionality of ‘\. On the other hand, these techniques may find two components associated with a one source and skip another source completely. A method performing partial decomposition based on natural gradient was proposed by Amari et al. in [13]. Constrained complete decomposition reduces the computational requirement and inclusion of some assumptions for the sake of simplification subjected to decomposition of observation space.

Belouchrani in [14] proposed an ICA procedure SOBI for implementing constraint based complete decomposition. There is no inclusion of any simplified assumption in case of unconstrained complete decomposition. Hence this process makes maximum use of available data observation space.

Koldovsky et al. proposed an algorithm for unconstrained complete decomposition in [15].

3. STRUCTURE OF PROPOSED METHOD

Let us consider a critically determined mixing environment, which produces \( M \) simultaneously recorded samples from microphones as shown in figure 2. Where signals samples are available as, \( y_1(n), y_2(n), \ldots, y_k(n) \) and \( n=1, \ldots, M \).

The applied method for decomposition is as follows.

**Figure 2 Mixing Model**

**Step 1.** Create a data matrix \( Y \) as in figure 1 of dimension \( M \times (M-L+1) \) where \( M \) is the required length of filter for demixing. The linear space enclosed is considered as observation space.

**Step 2.** Apply modified ICA method over mixture given by ‘\( Y \)’ to determine all independent components. As there could be \( L \) independent components, the output matrix will have size of ‘\( L \times L \)’ and unmixing matrix \( W \) can be determined of the same size, and the components are given by \( Ic = W \cdot Y \). Each row of \( Ic \) will denote the components of signal defined by \( Ic_1(n) \) to \( Ic_L(n) \).

**Step 3.** Grouping of components in a cluster on the basis of similarity criterion will be performed in this step. The clustering process will be helpful for estimation of original sources. Here authors are recommends K-Mean clustering technique. Which is one of the simplest unsupervised clustering method. Some key points of K-Mean clustering algorithm is as follows.

Let \( Y = \{ y_1, y_2, \ldots, y_n \} \) be the set of data points and \( U = \{ u_1, u_2, \ldots, u_K \} \) be the set of centers.

1. Select randomly ‘\( c \)’ centre.
2. Cluster each data point by calculating distance from the centre.
3. Data point is allotted to any particular cluster which distance from centre minimum.
4. Recalculation of the new cluster centre using:
Where, ‘ci’ shows the number of data points in ith Cluster.

5. Repeat step 4 to form new cluster
6. If no data point was reassigned then Stop.
Else Repeat from step 3.

The main reason behind recommendation of K-mean clustering is its robust nature, simplicity and fast speed.

Step 4. In this step compute a weight for each Cluster as a measure of confidence of the Component to be a part of that cluster. In next move compute a reconstructed version of matrix ‘Y’ and each row of Matrix ‘Y’ will corresponds to response of individual microphones.

The Reconstruction of jth cluster can be formulated as follows.

\[ S_{est} = W^{-1} \text{diag} \{ \gamma_{1}^{j}, \ldots, \gamma_{L}^{j} \} WY \]

Where \( \gamma \in [0, 1] \) denotes the weights and represents degree of match.

Step 5. Here a beamformer method will be applied To estimate the response of each source.

4. IMPLEMENTATION AND SIMULATION

To understand the proposed decomposition method discussed in previous section. Three sources have been taken; One recording of flute of duration 4 second, one recording of guitar and one male voice sample of same duration. The duration of recording is taken of 4 second because the author want to tackle problem addressed in introduction related to frequency domain decomposition. Figure 3 shows original source signals where 1500 sample were taken for the sake of uniformity. To create a situation of blind mixing all three source signals are stored in a matrix one signal per column and multiplied with one randomly generated 3X3 matrix. In result of this a mixture of three signals are obtained shown in Figure 4. In this research two techniques are compared, one is complete decomposition of audio mixture and then clustering on the basis of similarity criterion and second method is convex divergence based independent component analysis.

\[ U_{i} = \frac{1}{C_{i}} \sum_{j=1}^{C_{i}} y_{i} \]  

\( \text{(5)} \)

Mixed Signals are decomposed in independent components without transforming the domain by using complete decomposition technique as discussed in Section-2. The independent components are shown in Figure 7. It is clearly evident that some of the components holds similarity and conclusion can made that, the independent components can be grouped by applying clustering algorithm based on similarity criteria. For clustering of independent components K- mean clustering technique is applied and resultant clusters are shown in figure 5. Cluster 1 contains two independent components, cluster 2 and cluster 3 contains 5 components in each. Last step is to apply reconstruction procedure, as all sources sound simultaneously then reconstruction can be applied as

\[ Y_{i}(n) = S_{j1}(n) + \ldots + S_{jL}(n) \]  

\( \text{(7)} \)

The reconstructed versions of signals are shown in figure 7. The quality of separated signals are evaluated by BSS_Eval function available GNU public licence and separated signals SIR values are 29.7 dB, 31.4 dB and 34.3 dB respectively.
Second source separation technique is modified convex divergence ICA is applied for performance evaluation and details of algorithm and experimental details are given in ref [18]. Sources are estimated using NC-ICA algorithm in time domain without decomposition, as these techniques is intended to estimation of unmixing matrix base on unsupervised learning base neural structure. In this technique it is assumed that the mixing matrix is invertible and algorithm is based on estimation of inverse of mixing matrix, a modified convex divergence function is used for learning and scaled natural gradient technique is used for weight updation. The stopping criteria of this technique is inspired from central limit theorem, according to that independent sources have non-Gaussian profile and it is observed from experiments in blind sources separation techniques the estimated signals are in super-Gaussian in nature, irrespective to mixing condition and in result of that positive kurtosis value is taken as stopping criteria of algorithm.

5. CONCLUSION
A time domain complete decomposition based source separation method is proposed for blind audio source separation. Proposed method is a variation of T-ABCD method for blind source separation. The key objective of this paper is, to support the argument that, there is a big room for improvement in existing time domain decomposition algorithms for blind audio source separation techniques. In this paper modified divergence based algorithms and K-mean clustering method is incorporated in existing decomposition techniques. Results are evident that the performance and quality of separation is improved and Time domain complete decomposition and convex divergence based ICA techniques are close competitor. As both the techniques are exhibiting similar performance. The conclusion can be drawn that, the use of modified convex divergence base ICA in complete decomposition technique improves the quality of separation.
Fig 7 the independent components of mixed signals

6. REFERENCES


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