

# Rewriting Logic based Approach for the Formalization of Critical Systems based on Multi-Agent System

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## ABSTRACT

The agent-oriented paradigm is an emerging technology, which has significant and growing interest, particularly through its ability to be used in the modeling of all types of systems and representation of knowledge.

However, this potentiality should not hide the difficulties associated with them in the design and verification, which may cause the scientific credibility of multi-agent modeling field, especially for the case of embedded and critical systems.

In this paper, we propose a new formal approach based on rewriting logic, in which we attempt to bridge the gap between agent based system analysis and its specification. In addition, our approach includes a well-known and effective verification technique, model checking, and allows independent of the used formalism to verify an important number of properties deemed relevant on critical system based on agent paradigm.

## General Terms

Software Engineering, Agent-Based System.

## Keywords

Critical System, Model-Checking, Multi-agent systems, Maude, Rewriting logic, Specification, Testing, Verification.

## 1. INTRODUCTION

Firstly, if we simply put that, a system is an organized collection of parts (or subsystems) that are highly integrated to accomplish an overall goal. System modeling is the process, which we show how the system should be working. The use of this technique is to examine how various components work together to produce a particular outcome.

Secondly, nowadays applications (or systems) are strongly characterized by their complexity. They are usually composed by heterogeneous and distributed entities, which must cooperate and coordinate in an "intelligent" way to exchange and share knowledge, in order to solve problems which are difficult or impossible for an individual entity.

The paradigm of multi-agent systems [41, 42], which offers an original way of modeling, is considered as an appropriate method that faces the problem of modeling such kinds of applications. Therefore, multi-agent based modeling method is present in the most of sectors: telecommunications, finance, Internet, energy, health, embedded systems ... etc.

Thirdly, the potential of multi-agent systems should not hide the difficulties associated with them in the design. These difficulties may discredit the field of agent based modeling as a whole and affects their relevance, and their scientific credibility. Moreover, at this time there is no evidence of a well-established engineering approach for building multi-agent based applications.

Therefore, it becomes crucial to have rigorous methods of formal specification and verification to ensure the safe development of agent based systems, which may be critical systems, and not risk erroneous attribution to this type of system, some properties such as security, integrity and robustness.

In this paper, we present an efficient formal approach based on rewriting logic formalism by using its language "Maude", and includes a well-known and effective verification technique, model checking. In fact, this approach is the extension and the improvement of our previous work [01, 02].

## 2. PRELIMINARIES

In this section, we first present some preliminaries and definitions related to the work to be presented in this paper.

### 2.1 Agent and Multi-Agent Systems

The increasing complexity of the industrial systems and the delocalization of the processing call more and more upon the use of new techniques where the processing can be decentralized. Therefore, this situation imposes the need for using *entities* able to solve problems, and also equipped with capacities of *communication* and *social reasoning*, i.e., they are able to reason the ones on the others. These entities are known with the name of *Agent*. Where an agent is an encapsulated computer system that is situated in some environment and that is capable of flexible, autonomous action in that environment in order to meet its design objectives [35], and the set of these agents, with these various capacities constitute a *Multi-Agents System* (MAS).

Various definitions from different disciplines have been proposed for the term multi-agent system. As given in [40], "Multi-agent systems are a new paradigm for understanding and building distributed systems, where it is assumed that the computational components are autonomous: able to control their own behavior in the furtherance of their own goals".

The most important reason to use agent paradigm when designing a system, is that some domains require the aptitude and competence of a set of agents, in order to solve problems, which are difficult or impossible for an individual agent. In addition, agents can model complex systems, and the agent-based modeling of critical industrial applications works better than other approaches. For example, in a production factory, the behavior of a complex machine that has own internal situations, its own rhythm, different reactions in different situations, can be effectively modeled by an agent.

Finally, even if the multi-agent systems offer an original way of modeling, and their uses are very different in practice, because of its promise as a new paradigm for designing software and systems. We can resume the inherent difficulties in three points:

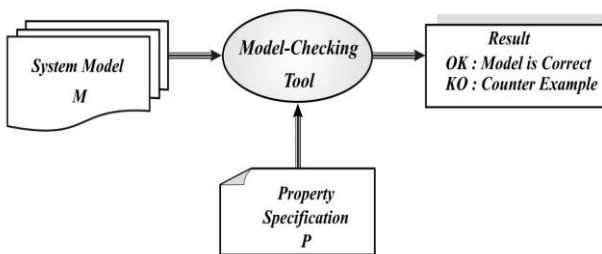
- 1) At this time, there is no evidence of a well-established engineering approach for building MAS-based applications.
- 2) The agent-based modeling has generated lots of excitement and the absence of proof for general properties of a model leads to problems that may affect multi-agent systems [03].
- 3) It would be practically impossible to develop a universal "MAS Library" and design generic secure models especially for safety critical systems.

Therefore, it is important to ask about the validation, and search for rigorous, automated and efficient methods of design and verification for agent-based systems. The disposition of such methods will help the designer to develop, validate and ensure the reliability of critical systems based-agent before its implementation. These methods should not be limited to one phase, but it must cover all the process of their development, in order to prove the safety of models intended to represent the relevant functions of the system.

## 2.2 Model-Checking

Model checking is a formal verification technique [05, 06, 07], that determines whether given properties  $\phi$  of a system are satisfied by a model  $M$ , where a model is defined as a formal representation of the real world [04]. We write  $M \models \phi$  as a judgment and say a model checker verifies or refutes such judgments, based on a partial or exhaustive exploration of the state space of the model. In other words, this formal verification technique analyzes the reliability, performance and checks the consistency between a property specification and a behavior model of the system. Its main objective is to ensure that none of all these states is inconsistent with the desired behavior.

The software tool validating a model and solving the model-checking problem is called model checker. A model checker typically as presented in the figure (Fig. 1) supports two different levels of specification: (1) a system specification level, in which the concurrent system to be analyzed is formalized; and (2) a property specification level, in which the properties to be model checked are specified. On the other hand, model checker outputs either a claim that the property is true or a counter example reporting the inconsistency. A counterexample is an execution trace of the state machine showing how the predicate is false.



**Fig 1. Model Checking Approach**

Currently, the "on the fly" or "symbolic" model checking are the most common used. These approaches, initially introduced to overcome the problem of infinite state machines. The big advantage of the on-the-fly approach is that hopefully only a fragment of the overall state space might need to be generated and analyzed to be able to produce the correct result [36][37]. Contrary to classical methods, their effectiveness has been

demonstrated, and they were used to analyze real systems of significant size [33, 34].

## 2.3 Rewriting Logic

Rewriting logic is a computational logic proposed by Meseguer [13] as a unified logic for (true) concurrency, which builds upon equational logic by extending it with "rewrite rules" to adapt it to changes [10], and specification of concurrent systems. In other words, rewriting logic is known as a flexible logic and as a unifying semantic framework in which other logics and a very wide range of concurrency models and programming languages can be represented, such as : Petri Net [12], Labeled Transition Systems [13], E-LOTOS [14], CCS [15, 16], PLAN [17], Pi-Calculus [18] ... etc.

In rewriting logic, a concurrent system can be specified easily by a rewriting theory. A *rewrite theory*  $R$  is defined as a 4-tuple  $R = (\Sigma, E, L, R)$  where :  $(\Sigma, E)$  is an equational theory,  $L$  is a set of labels, and  $R$  is a set of possibly conditional labeled *rewrite rules*,  $t \rightarrow t'$  that are applied modulo the equations  $E$ . Intuitively, the signature  $(\Sigma, E)$  of a rewrite theory describes a particular structure for the states of a system, and the rewrite rules describe which elementary local transitions are possible in the distributed state by concurrent local transformations if a condition  $C$  is verified [11,13].

For any term  $t$  in the rewrite theory  $T$ , we write  $[t]$  for its equivalence class, and we say that  $[t] \rightarrow [t']$  is provable in  $T$  when it is obtained by a finite application of the following deduction rules:

1. **Reflexivity**: for each term  $[t] \in T_{\Sigma, E}(X)$ ,

$$\frac{}{[t] \rightarrow [t]}$$

2. **Congruence** : for each operator  $f \in \Sigma_n$ ,  $n \in \mathbb{N}$

$$\frac{[t_1] \rightarrow [t'_1] \dots [t_n] \rightarrow [t'_n]}{[f(t_1, \dots, t_n)] \rightarrow [f(t'_1, \dots, t'_n)]}$$

3. **Remplacement** : for each rewriting rules :

$$r : [t(\bar{x})] \rightarrow [t'(\bar{x})] \text{ if}$$

$$[u_1(\bar{x})] \rightarrow [v_1(\bar{x})] \wedge \dots \wedge [u_k(\bar{x})] \rightarrow [v_k(\bar{x})] \text{ in } R,$$

with  $\bar{x}$  abbreviating  $x_1, \dots, x_n$

$$[w_1] \rightarrow [w'_1] \dots [w_n] \rightarrow [w'_n]$$

$$\frac{[u_1(\bar{w}/\bar{x})] \rightarrow [v_1(\bar{w}/\bar{x})] \dots [u_k(\bar{w}/\bar{x})] \rightarrow [v_k(\bar{w}/\bar{x})]}{[t(\bar{w}/\bar{x})] \rightarrow [t'(\bar{w}/\bar{x})]}$$

with  $\bar{w}/\bar{x}$  indicate the substitutions of  $x_i$  by  $w_i$   $1 \leq i \leq n$ .

4. **Transitivity** :

$$\frac{[t_1] \rightarrow [t_2] \quad [t_2] \rightarrow [t_3]}{[t_1] \rightarrow [t_3]}$$

### Deduction Rules of the Rewriting Logic

## 2.4 Maude System

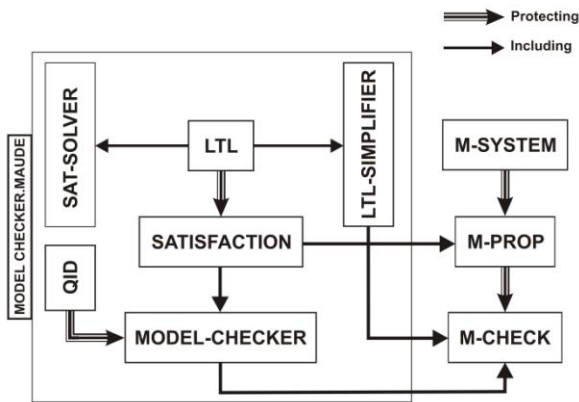
Maude [38] is a high-level language and a high-performance system supporting executable specification and declarative programming in rewriting logic. Maude is based on rewriting logic where the object systems from simple to more complex models are specified easily by the use of the theory of concurrent objects. The rewrite theory can describe the system as a configuration of objects declaratively with a high degree of abstraction.

Maude has been used for specification, prototyping and testing of a wide range of applications, because it has a collection of formal tools supporting different forms of verification such as:

- ◆ The Maude Termination Tool (MTT) : can be used to prove termination of functional Modules;
- ◆ The Maude Church-Rosser Checker (CRC) : can be used to check the Church-Rosser property of unconditional functional modules;
- ◆ An inductive Theorem Prover (ITP) : to verify properties (theorems), which are defined in functional modules;
- ◆ The Maude Coherence Checker (ChC) : can be used to check the coherence (or ground coherence) of unconditional system modules; and
- ◆ The Maude Sufficient Completeness Checker (SCC): can be used to check that defined functions have been fully defined in terms of constructors.

### 2.5 The Maude's LTL Model-Checker

Model-checking is as what we said previously, an automatic method for deciding if a circuit, program or a specification model, expressed as a concurrent transition system, satisfies a set of properties expressed in a temporal logic such as LTL. The Maude's LTL model checker is a very powerful model checker. It was designed with the goal of combining a very expressive and general system specification language (Maude) with an advanced on-the-fly explicit-state LTL model-checking engine. The main modules used by the Maude's LTL Model-Checker are presented in the figure (Fig. 2).



**Fig 2. The Main Modules of Maude's LTL Model-Checker**

In Order to verify such a property, the Maude's LTL model checker takes as inputs the following modules, which are defined by the user:

1. Rewrite theory specified by a Maude system module M-SYSTEM, which describing the behavior of the system.
2. PROP-M module, which contains the set of predicates expressed in standard LTL propositional logic as the defined syntax in the module SATISFACTION.
3. The initial state from which the model checker starts checking, is specified in module M-CHECK.

In addition to modules defined by user, the Maude's LTL model checker includes other modules that have well defined roles:

- MODEL-CHECKER: This is the main module in the verification process.
- LTL : This functional module formalizes the syntactic and semantic definitions of linear temporal logic (LTL);
- LTL SIMPLIFIER : It tries to further simplify the negative normal form of the formula  $\neg\varphi$  : in the hope of generating a smaller Büchi automaton  $B_{\neg\varphi}$ ;
- SAT-SOLVAR : It can be used to check both satisfiability of an LTL formula and LTL tautologies;
- SATISFACTION: A very simple module defines the standard LTL propositional logic used to express the set of predicates.

### 3. CRITICAL SYSTEM FORMALIZATION

When we want to talk about the formalization of critical systems, it is strongly advised to explore the attempts of formalization of other systems that can be considered as critical systems, such as real-time systems, parallel and complex systems. In addition, because the agent-based modeling is one of the most used approaches and it works better than other approaches in the case of critical systems. We will focus in this section on formalization of multi-agent based systems.

In the last two decades, multi-agent systems have both become widely applied and increasingly complex. Therefore, a lot of approaches, languages and methods have been proposed to face the problem of developing agent-based systems [43, 56].

In this section, we will present the works that we are seeing significant in the field of specification and verification of multi-agent systems. Then, we will try to summarize the previous attempts of formalization, in order to reveal the advantages and the limitations of either kind of approach.

#### 3.1 Formal Specification

The process of development of the information processing systems includes a whole of phases such as specification, design, validation and tests. We generally start from an abstract description of the system, using the natural language and the passage to the design phase is intuitive. Nevertheless, when the reliability of the system is too important, it becomes necessary to start from a formal specification, which describes the system behavior by means of a formal language. Many languages were proposed, we give briefly here four examples:

##### A. CASL Specification Language

The Cognitive Agents Specification Language (CASL) is a framework for specifying Multi-agent systems, which allows the specifier to view agents as entities with mental states, such as knowledge, beliefs, and goals, and to define the behavior of the agents in terms of their mental states [44]. It combines two powerful components. The first one is a declarative action theory, which allows the specifier to describe the effects of actions on the world and the mental states of agents. The second component is a rich programming/process language with constructs for concurrency and non-determinism to facilitate the specification and verification of multi-agent systems.

##### B. AUML

The best-known initiative to extend UML with facilities for describing agents called AUML. It starts from the idea that multi-agent systems are often characterized as extensions of

object-oriented systems. In other words, if the unified modeling language (Unified Modeling Language) is an attempt to unify the different paradigms of analysis and design object oriented software and provide a unique notation for modeling object-oriented systems, the AAML was proposed to adapt the UML notation to describe the agent-oriented modeling [45,46].

### C. The Agent Modeling Language: AML

The Agent Modeling Language (AML) is a semi-formal visual modeling language, specified as an extension to UML 2.0. AML is designed to capture the aspects of multi-agent systems. The ultimate objective for AML is to provide a means for software engineers to incorporate aspects of multi-agent system engineering into their analysis and design processes. In other words, AML is designed to support business modeling, requirements specification analysis, and design of software systems based on software agent concepts and principles [55, 58].

### D. SLAB Language

In his paper [52], the author was presented a powerful formal specification language (SLAB) for multi-agent systems. The (SLAB) language integrates a number of novel language facilities that support the development of agent-based systems. In order to show that these facilities are powerful and useful for the formal specification of agents in various models and theories, the author specified example systems of agent-based systems in SLAB.

Many works exist in literature using different formalisms such as Petri nets, Logics, Languages, UML. In general, we can distinguish two major kinds of approaches: [19, 20]:

#### Behavioral Approach

The first approach consists in specifying a system by giving a description whose semantics is founded on transition system (operational semantics). This approach makes it possible to describe the behavior of a system like the composition of elementary behaviors. Petri nets, graphs of states, algebras of process and the languages such as ESTELLE, LOTOS or SDL, are examples [19, 48].

#### Logic Approach

The second approach is generally based on the use of a language making it possible to express the whole of the system properties. In this case, the used language is of declarative type and the system specification will be expressed by a whole of properties using logic formulas. Temporal logics are examples of languages used by this approach for the expression of properties [47, 50, 54].

## 3.2 Formal Verification

According to the formalism used to represent the system specification, we distinguish two verification approaches: the behavioral and the logic verification. In the first approach, labeled transition systems is the most widely used formalism for the specification, and the verification process of a system property reduces to compare two labeled transition systems S and P. While the second approach, which is generally based on temporal logic to express all the system properties, the decision about the satisfaction of a property formula will be based on model-checking algorithms.

Finally, we can present in the figure (Fig.3) non-exhaustive list for the attempts were found in the literature for the formalization of multi-agent systems and the used formalisms.

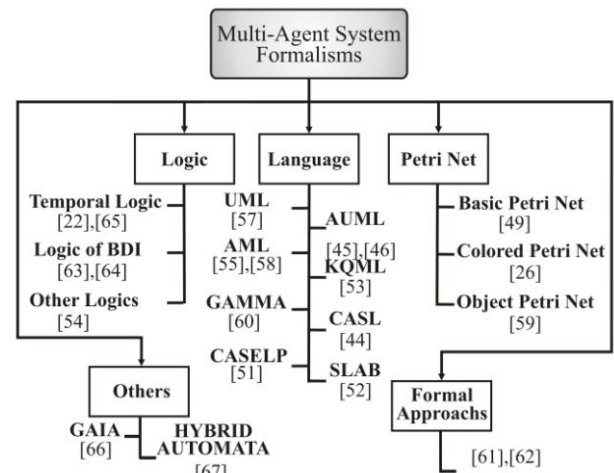


Fig 3. Formalisms used for the Formalization of MAS

## 3.3 Synthesis

First, we have to note that in our opinion, the two specification approaches are complementary, and their combination can be very interesting, as it is important to adopt the most appropriate formalism for the representation of the system. We justify this idea by:

- The main purpose of the specification is to provide a complete description of the system. This specification must sometimes be described in two different point of views to cover the Static (structural) and Dynamic (behavior) of the system. In addition, the combined analysis of static and dynamic aspects of a system is also necessary for detecting hot spots in the system. Static view provides an overview of the system that is structural while the dynamic view shows the behaviors, interactions and evolution of the system.
- It is possible to establish (make) another classification with other criterions, for example: a classification based on aspects or kind of properties to be checked (functional and non-functional) of the system. In addition, it is possible that two formalisms that do not belong to the same approach in the mentioned classification can be found together in an other approach if we change the classification criterions.
- The same formalism can be used to model the two aspects of the same system, taking the example of UML static diagrams and dynamic diagrams. Therefore, the same formalism may belong to two different approaches.

Then, because we are interested by the agent based design, we can also find in the literature, several attempts at formal specification of multi-agent systems, which tend to describe an agent in mathematical terms, and those based on Petri nets, finite state automata, X-machine such as :[21, 22, 23, 24, 25, 27, 28, 49], etc.

In the case of multi-agent systems, the specification is to develop an abstract model of the real system. The interest of a model is initially to be more explicit, simpler and easier to manipulate than the reality it is supposed to represent. Moreover, the specification of multi-agent systems must be based on a powerful operational and unambiguous formalization. Nevertheless, in the view of the absence of a consensus on the most suitable formalism for specifying multi-agent systems, we have to note here our agree with the ideas of [29, 30], that there is no perfect model, and we are

wrong if we think that the goal is to offer the most complete model and the most "beautiful", because the reality is always more complex than we imagine.

Therefore, we must build the system model with the most suited formalism to check the properties in question, and not to limit to the use of a single formalism. Because, as noted in [31], if we take the example of the paradigm of multi-agent systems; the specification of system structure can be performed using UML, while the dynamics of the agents may be specified using Petri nets or inference rules.

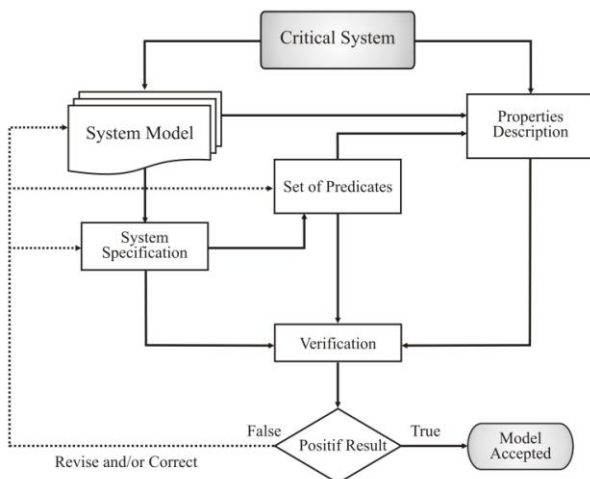
Finally, it is crucial to search for formalisms that allow full description of the multi-agent based system and the consistent expression of its different aspects: structure, behavior, control ... etc. In addition, a set of relevant properties of the system must be verifiable with the proposed formalisms by using effective tools. Because, as noted in [32]: "any sufficiently complex system has consequences that exceed its capabilities of proof" Therefore, the use of such a method is needed from the initial specification to implementation.

#### 4. FORMALIZATION APPROACH FOR CRITICAL SYSTEMS BASED ON MULTI-AGENT SYSTEMS

In system design, the process of verification and validation can be too complex, especially when it depends to ensuring that the system has no failures (unexpected behavior) and that it meets its specifications correctly. Indeed, in the case of designing critical systems, the steps of formal specification and verification are essential to avoid any type of error and validate systems before their implementation. The specification phase is intended to clearly express all the expected features of the system, while the integration of the verification phase in the design process can detect the error once it appears, and it allows to avoid repeating all the verification process by reusing intermediate results.

##### 4.1 Global Description

In our approach, which is based on the use of formal and automatic techniques, we start from a specification written in rewriting logic of the proposed model for the system, and a specification of the expected properties, in order to determine whether the system model satisfies the properties in all its possible executions. We present in the following figure Fig.4, the steps of the proposed approach for the verification of relevant properties of critical systems.



**Fig 4. Global Description of the Formalization Approach**

##### 4.2 Detailed Description

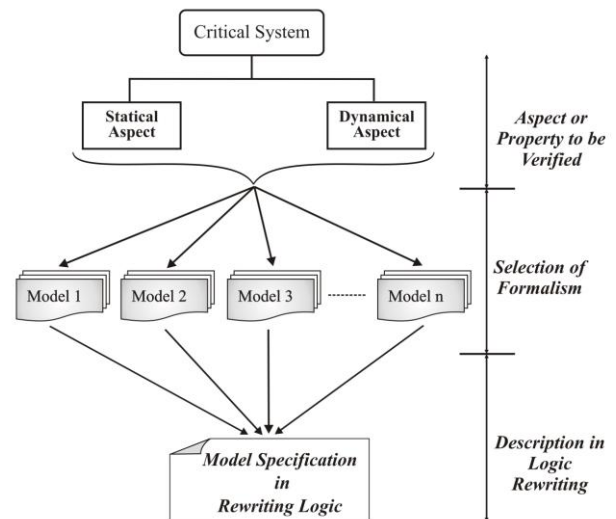
Our approach for the formalization of multi-agent based systems can be summarized into three essential steps:

###### Step 01: (System Specification)

The purpose of this step is to describe the full specification and to express all the expected features of the system. We note here that in the case of multi-agent systems, the first step of specification is to develop a model clearly and unambiguously. Using one of the most used formalisms such as UML [57], Petri nets, labeled transition systems ... etc

In our approach, we will not be limited to use only one specification approach or a single formalism, but according to the aspect or the property to check, we will choose the most adapted formalism to the case study. In other words, it is very judicious to use several formalisms for the same system to take advantages of each formalism and verify a large number of system properties. [29, 30].

This stage ends with a description of each model in rewriting logic, which is logic of change and a unifying semantic framework. Taking advantage of its expressiveness and powerful tools built into its system Maude. A description of this step is illustrated in the following figure Fig 5.



**Fig 5. Description of the Specification Step**

###### Step 02: (Properties Specification)

If the aim of the first step, is to give a more or less abstract description of the system. A system can be formally defined by its properties. In this step, we must prepare a module that defines the set of predicates expressed in standard LTL propositional logic. These predicates will be considered by the Maude's model-checker tool as the set of verified properties in the system. We always refer to the proposed model and its specification of the first step. Then, the set of properties to be checked must be also expressed by using linear temporal logic.

###### Step 03: (Verification)

Finally, a verification step is necessary to show that the system satisfies the desired property and that it exhibits a stable behavior, and/or certify that the probable malfunctions of the system causes only moderate damages. Two verification techniques as illustrated in the figure Fig.6, are applied to perform this step:

### 1- Model-Checking:

In this technique, we try to check the intrinsic properties of a model by expressing it using linear temporal logic. The verification process is achieved with Maude's LTL model-checker tool.

### 2- Empirical Test :

This time, we use another Maude's tool, which is: *Search*. Its use is based on situations and empirical cases offered by experts in the field; in order to confirm the absence of critical situations in the model. The use of this technique is intended to accomplish the lack of the first technique, which permit to ensure only the properties expressed in linear temporal logic.

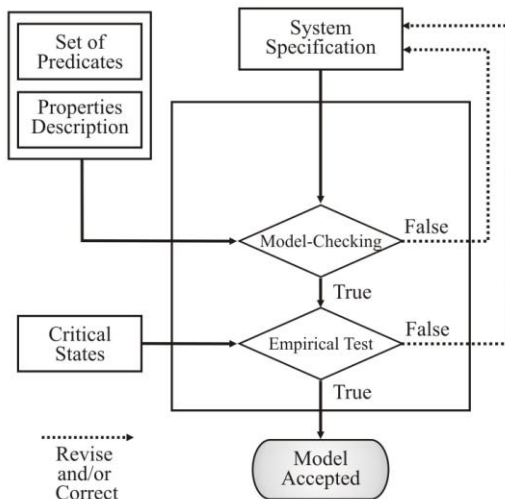


Fig 6. Description of the Verification Step

## 5. CONCLUSION AND FUTURE WORK

Research in the field of multi-agent systems (MAS) is becoming increasingly important, particularly through its ability to model all types of systems. However, the potential of multi-agent systems (MAS) should not hide the difficulties associated with them in the design and verification, especially for the case of critical systems. Formal methods have been proposed as mathematical techniques to help the designer to solve this problem. Nevertheless, each of these methods is used to solve a specific class of problems, depending to the type of formalisms used.

In this paper, we have extended our previous approach [1, 2], in order to provide a more comprehensive approach based on rewriting logic for the specification and verification of critical systems based agent, including model checking technique and the technique of empirical test. Our approach allows to verify a large number of properties of a critical system regardless of the formalism used for the specification. In other words, our approach tends to provide a full specification for critical systems based MAS, leaving the choice to the user to adopt the most appropriate formalism for the representation of models and the expression of properties.

The first advantage of this method is that it is applicable regardless of the type of formalism chosen. In addition, it has the advantage that it permits to verify several types of properties: properties that are expressed and those are not expressible in linear temporal logic. Third, the integration of verification into the design process can detect an error once it occurs and avoids redoing all the verification process by reusing intermediate results.

Our approach still suffers from the problem that it requires a mastery and competence in the use of the formalism of rewriting logic. Because the directly description of a model or the mapping from model to rewriting logic is not always easy.

Finally, in order to palliate this problem in our approach, we intend to continue our research on the axis of development of a framework for the automatic generation of the specification in rewriting logic; at least from the most used formalisms.

## 6. ACKNOWLEDGMENTS

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