Impact of Integrating Wind Energy into Power Grid System

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ABSTRACT

Wind is one kind of free energy and this "must-take" wind power generation is integrated into the system operation. The optimal power flow (OPF) problem with integration wind energy was explored and exploited in this paper. This paper presents the impact integration wind wnergy on different performance parameters of power systems such as the total generation cost, voltage profile, power flow and power losses, by optimally integrate the wind farm in power systems. The modified IEEE 30 system with six thermal generating units and two wind farms. Several scenarios were conducted to determine the impact of single and multiple wind farm on the performance of the IEEE 30 bus system. In this paper, using programming language (Matlab) and PowerWorld software Version 19 to get the results.

Keywords

Optimal Power Flow, wind power, linear programming, voltage profile, PowerWorld.

1. INTRODUCTION

Because wind power does not generate any emissions, it has been promoted as a clean way to generate electricity, with a variety of government policies encouraging its use [1]. In latest years, global wind energy has evolved hastily. Wind power capacity worldwide reaches 597 GW, 50.1 GW added in 2018. [2]. Using the optimal power flow calculation (OPF) we can discover the impact of renewable energy on energy systems. The OPF is an important tool that system operators require to operate the network with a high penetration of wind power more efficiently, keeping all restrictions within tight limits. The OPF optimizes the static operating conditions of a power generation transmission system. The main advantages of the optimal energy flow are: (i) guaranteeing the static safety of the service quality by imposing limits on the operation of the generation transmission system, (ii) optimizing the voltage / reactive power planning and (iii) improving The operation economy through the full use of the eligible operating range of the system and the precise coordination of transmission losses in the planning process [3].

The objectives of this paper include studying the impact of the wind power penetration on as voltage profile, power flow of transmission lines, and reduction of the active and reactive power losses.

2. THE GRID INTEGRATION OF LARGE SCALE WIND GENERATORS

In the coming years there will be an elementary change in the composition of the generation as a result of the need to replace many power plants due to aging. In this situation, the specific growth of renewable and dispersed generation plays an important role. Renewable energy generation is coFiras Mohammed Tuaimah, PhD Electrical Engineering Department University of Baghdad

financed by fixed high-level prices for various renewable energy sources (RPS). These prices are independent of the network level in which RPS connections are provided. In-feed of power via large wind farms is essentially difficulty to different patterns as is the case with conventional power sources together with thermal, gas turbine or hydroelectric generating plants. Three essential problems need to be solved for the combination of huge wind farms in transmission system: (1) wind strength output relies upon on meteorological situations and can be intermittent. (2) A higher level of reserve strength than before ought to be furnished. (3) Suitable transmission capacities have to be created in order for the strength to reach the load facilities. Wind power manufacturers are entitled to switch their manufacturing to the gadget thru the electricity distribution or transmission business enterprise whenever the absorption of the strength via the network is "technically feasible" [4].

3. PROBLEM FORMULATION

3.1 Mathematical Formulation

The OPF hassle incorporating wind power is the trouble to be studied in this paper and the planned wind energy blended with the power output of thermal electricity plant are as the variables to be optimized. Keep in mind that, the unbiased device operator might be accountable for the dispatching of wind strength and decide the corresponding power price.

The usual OPF problem can be formulated as a restrained optimisation problem as follows [5]

Minimize,

 $F(x,u) = \begin{pmatrix} f_1(x,u) \\ . \\ f_k(x,u) \end{pmatrix} \text{ where } k = 1,2. \text{ No of objective}$

Subject to:

g(x,u)=0

h (x,u)≤0

Here x and u represent vector of dependent and control variables respectively. For example, the dependent variables represent slack bus power, bus voltage angles, load bus voltage magnitudes etc whereas PV bus voltage magnitude, generated power, tap position of tap changers, shunt compensators etc are represented by the control variables. g(x, u) denotes the real and reactive power balance equations and h(x, u) represents network or components operational limits.

3.2 Objective Functions

3.2.1 Fuel Cost

The objective of fuel cost minimization is finished by allocating high-quality community settings that minimizes normal fuel cost characteristic whilst pleasing other network constraints. The generator cost curve that's a feature of strength output, may be represented by using the following quadratic equation.

$$F(P) = \sum_{i=1}^{n} (a_i + b_i P_i c_i P_i^2)$$
(2)

where n is the number of generators; aj, bj, cj are the fuel cost coefficients, ej and fj are fuel cost coefficients of the jth unit with valve points effects and Pj is the real power generated by the jth unit[6].

3.2.2 Active and Reactive Power Loss

The objective is to minimize the total active and reactive power losses in the transmission lines may be expressed as follows:

$$= \sum_{k=1}^{m} G_{K} \left(V_{i}^{2} + V_{j}^{2} 2 V_{i} V_{j} \cos(\delta_{i} - \delta_{j}) \right)$$
(3)

$$QL = \sum_{k=1}^{m} B_{K} \left(V_{i}^{2} + V_{j}^{2} - 2V_{i}V_{j}\sin(\delta_{i} - \delta_{j}) \right)$$
(4)

Where m is the total number of lines in the system; Gk is the conductance of the kth line; Bk is the susceptance of the kth line; Vi is the voltage magnitude at bus i; Vj is the voltage magnitude at bus j; δi is the voltage angle at bus i; δi and is the voltage angle at bus j [7].

3.2.3 Voltage Deviation

To have a good voltage performance, the voltage deviation at every load bus have to be made as small as possible. The voltage deviation (Δv) to be minimized is given in [8].

$$\Delta V = \sum_{k=1}^{N_{PQ}} |V_{K} - V_{K}^{des}|$$
(5)

Where NPQ is the number of load buses and V_k^{des} the desired or target value of the voltage magnitude at load bus k.

3.3 Constraints

3.3.1 Overloaded Lines

This objective is to minimize the power flow in overloaded transmission lines; this objective is calculated for every line of the system. The lines loading have to be less than one 100%. The active power and reactive power flow on lines can be applied as follows:

$$PGi-P_{Di} = V_i \sum_{k=1}^{m} V_j (G_K \cos(\delta_i - \delta_j) + B_K \sin(\delta_i - \delta_j))$$
(6)

$$QGi-Q_{Di} = V_i \sum_{k=1}^{m} V_j (G_K \sin(\delta_i - \delta_j) + B_K \cos(\delta_i - \delta_j))$$
(7)

Where P is the real power generation at bus i; PDi is the real power demand at bus i; QDi is the reactive power generation at bus i; QDi is the reactive power demand at bus i; m is the total number of buses in the system; Vi is the voltage magnitude at bus i; Vi is the voltage magnitude at bus j; is the conductance of the kth line; is the susceptance of the kth line; δi is the voltage angle at bus i; and δj is the voltage angle at bus j[9].

3.3.2 Generation capacity constraints

The real power output of generating units have be restricted within their respective lower and upper bounds (inequality constraints) as follows:

$$P_{Gj}^{\min} \le P_{Gj} \le P_{Gj}^{\max}$$
 for $j = 1, 2 \dots n$ (8)

Where n is the no of generators. P_{Gj}^{min} and P_{Gj}^{max} are minimum and maximum power outputs of jth generating unit respectively.

3.3.3 Other constraints

The other operational constraints involved in OPF problem are generator reactive power, voltages of all PV buses, transformer tap positions, VAR compensator position, bus voltage magnitudes of all PQ buses etc. These constraints can be formulated as follows:

$Q_{Gj}^{\min} \leq Q_{Gj} \leq Q_{Gj}^{\max}$	for j = 1,2 nPV	(9)
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$\left V_{Gj}^{\min} \right \le \left V_{Gj} \right \le \left V_{Gj}^{\max} \right $ for $j = 1$	$, 2, \dots nPV$ (10)
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$$\left| T_{Gj}^{\min} \right| \le \left| T_{Gj} \right| \le \left| T_{Gj}^{\max} \right| \quad \text{for } j = 1, 2, \dots n P V$$

$$(11)$$

$$|Q_{ci}^{\min}| \le |Q_{ci}| \le |Q_{ci}^{\max}|$$
 for j = 1, 2, ... nc (12)

$$\left| V_{j}^{\min} \right| \le \left| V_{j} \right| \le \left| V_{j}^{\max} \right| \qquad \text{for } j = 1, 2, \dots nPV \tag{13}$$

Where nPV and nPQ are the number of PV buses and PQ buses respectively. nT and nC are the number of tap changing transformer and switchable VAR compensator respectively[10].

4. OPTIMAL POWER FLOW (OPF)

Optimal power flow (OPF) problem has been one in all the foremost wide studied subjects within the power grid community since Carpentier 1st revealed the conception in 1962. The objective of optimum Power Flow (OPF) algorithm is to search out a gentle state operation purpose that minimizes generation price, network loss etc. or maximizes welfare or system utilization etc. even as preserving an acceptable system overall performance in phrases of limits on generators' active and reactive powers, line go with the flow limits, most output of numerous compensating devices and many others.. Take optimum active power dispatch as associate degree example, the target operate is to attenuate total generation price or network losses whereas the system is working at intervals its security limits [11].

5. LINEAR PROGRAMMING OPF

The early LP - based OPF method was restricted to network constrained economic power dispatch. The earliest versions used the fixed constraint approximations, primarily based on the purely dc power flow. In a while, incremental formulations have been brought, wherein constraint linearization is iterated with ac energy glide, to model and put into effect the constraints precisely. The benefits of the LP based OPF are:

- 1. Reliability of the optimization
- 2. Capability to recognize trouble infeasibility quick, in order that suitable strategies can be positioned into impact
- 3. The variety of operational limits can be easily accommodated and handled, together with contingency constraints
- 4. Convergence to engineering accuracy is fast, and conjointly accepted once the changes within the controls became very small [11].

6. INCREMENTAL LINEAR PROGRAMMING METHOD

Studies have shown that the progressive linear programming (LP) technique will be accurately applied to a large vary of applications, and might manufacture a similar results as information NLP methods on power systems of every kind and sizes. Several benefits of the incremental LP technique over different existing strategies encompass its reliability, its ability to quickly understand trouble infeasibility, its capacity to deal with a wide range of operating limits, a very speedy computational speed, and extra flexibility for change-offs between computing speed and convergence accuracy. The incremental LP method is performed by linearizing the Fig.1.

$$min\sum_{i=1}^{N_b} F_i\left(P_{gen_i}\right) + \frac{\partial F_i\left(P_{gen_i}\right)}{\partial P_{gen_i}} \Delta P_{gen_i}$$
(14)

$$\sum_{\forall j \in B} \frac{\partial P_i(V,\theta)}{\partial V_j} \Delta |V_j| \sum_{\forall j \in B} \frac{\partial P_i(V,\theta)}{\partial \theta_j} \Delta \theta_j = \Delta P_{gen_i} \ (\forall i \in B)$$
(15)

$$\sum_{\forall j \in B} \frac{\partial Q_i(V,\theta)}{\partial V_j} \Delta \mid V_j \mid \sum_{\forall j \in B} \frac{\partial Q_i(V,\theta)}{\partial \theta_j} \Delta \theta_j = \Delta Q_{gen_i} \ (\ \forall i \in B \)$$
16)

$$\Delta \quad V_i = 0 \left(i \in B_{refbus} \right) \tag{17}$$

 $\Delta \theta_i = 0 \left(i \in B_{refbus} \right) \tag{18}$

$$\Delta P_{gen_i} = 0 \ (i \in B_L) \tag{19}$$

$$\Delta Q_{gen_i} = 0 \ (i \in B_L) \tag{20}$$

$$\begin{array}{rcl} P_{gen_i}^{min} & - & P_{gen_i} \leq \Delta P_{gen_i} \leq P_{gen_i}^{max} & - & P_{gen_i} \quad (\forall i \in B) \quad (21) \end{array}$$

$$\begin{array}{rcl} Q_{gen_i}^{min} & - & Q_{gen_i} \leq & \Delta Q_{gen_i} \leq & Q_{gen_i}^{max} & - & Q_{gen_i} & (\forall i \in B \) & (22) \end{array}$$

$$\begin{array}{rcl} V_i & {}^{min} & - & V_i & \leq \Delta & V_i & {}^{max} & - & V_i \\ B & & (23) \end{array} \tag{$\forall i \in A$}$$

 $-\delta_k \le \Delta P_{gen_i} \le \delta_k \tag{24}$

 $-\delta_k \le \Delta Q_{aen_i} \le \delta_k \tag{(\forall i \in B)} \tag{25}$

$$-\delta_k \le \Delta \ V_i \le \delta_k \tag{26}$$

$$\begin{aligned} -\delta_k &\leq \Delta \,\theta_i \leq \delta_k \\ B \,) \qquad (27) \end{aligned}$$

Constraint (12) represents the linearized real power equality constraints, (13) the linearized reactive power equality constraints, (14)-(17) the additional constraints on the swing bus and the load bus variables respectively for the problem to solve correctly, (18) the generator real power limits, (19) the generator reactive power limits, (20) the bus voltage magnitude limits, and (21)-(24) the size of the optimization region for each variable for the current iteration k. It should be noted that constraints (18)-(20) and (21)-(23) are overlapping. Thus, the constraints (18)-(20) will only be active if their corresponding variables Δ Pgeni , Δ Qgeni , or Δ |Vi| are at one of their limits. Otherwise, the variables will be free to move within the optimization region as specified in (21)- (23)[12].



7. CASE STUDY

Table 1. Test System Data

Generators	6
Buses	30
Load points	21
Total generation capacity	435MW
Fixed load	283.4 MW

The modified IEEE 30 system with six thermal generating units' two wind farms as shown in Fig.2. The wind power penetration level in this paper is defined as the ratio of the installed wind generation capacity to the total-installed system generation capacity of 10% (the installed wind generation capacity is 40 MW). Two wind farms including 10 wind generators each one have rating 2 MW (Type 4: Enercon E82 2MW) and connected at bus no. 10 and bus no. 24 (20 MW in each bus) is used to analyse the effect of connected wind farm on the total generation cost, voltage profile, power flow of transmission lines, the active and reactive power losses. Several scenarios with dispersed wind penetration levels from 0% to 100% have been investigated. The wind generators are connected at bus 10 and bus 24. The basic system data are

7.1 OPF Results without the Insertion of Wind Farms

The results including the generation cost, the minimum deviation and power losses in the case without the penetration of the Wind generators are tabulated in Table 2.

Variable	PowerWorld	Matlab
Pg1(MW)	196.351	195.6439
Pg2(MW)	44	43.8668
Pg5(MW)	22	21.4574
Pg8(MW)	10	10.5771
Pg11(MW)	10	10.0866
Pg13(MW)	12	12.0000
Production cost (\$/hr)	803.91	803.26
Power Loss (MW)	10.54	10.31
Power Loss (Mvar)	21.23	19.67

Table 2. Results of minimum total cost for IEEE 30-bus system by LPOPF

7.2 Impact of Single Wind Farm Site

The wind farm is connected at bus 10 and bus 24 (20 MW in each bus) separately, for penetration levels from 25% to 100% with an interval of 25%. From Table 3, it can be seen that the total generation cost, minimum voltage (level & phase angle) values, total active and active power generation, power flow of transmission lines, the active and reactive power losses (Table 3), and Fig.3 and 4 shows the voltage profiles.

7.3 Impact of Multiple Wind Farm

In this case we show the impact of integration wind farm connected to bus 10 and bus 24 (20 MW in each bus) together. For penetration levels from 25% to 100% with an interval of 25%. From table 3, it can be seen that the total generation cost, minimum voltage (level & phase angle) values, total active and active power generation, power flow of transmission lines, the active and reactive power losses, and Fig. 5 shows the voltage profiles.

From table 3 (Wind farm connected to bus 10 & 24), the results show that variable wind power reduces the cost generation level, by optimal power flow. When system operate without wind farm show that the high MW cost of in generator at bus 5 at rated power 22MW as shown in Fig.6, but when integrated wind farm to bus 10 and 24 at fill rated power (20MW in each wind farm) effect to reduce MW generator at bus 5 to 15MW and reduce cost of it shown in Fig. 7. Thus, wind farms will be reduce the cost of fuel for conventional power plants.



Fig 2: IEEE 30-bus Electrical system with two Wind generator at bus10&bus 24

			Wind f	arm conn	ected at I	ous 10					
Variable		Р	owerWorld	l		Matlab					
Wind penetration	0%	25%	50%	75%	100%	0%	25%	50%	75%	100%	
slack bus (MW)	178	191	185	180	175	176	175	171	166	160	
Cost(\$hr)	803.91	785.4 6	766.73	748.5 3	730.4 2	802.46	791.03	776.83	764.63	753.42	
Losses (MW)	10.54	10.58	10.09	9.63	9.20	10.31	9.12	9.05	8.79	8.27	
Losses (Mvar)	20.23	19.18	19.08	18.94	18.9	19.67	19.12	18.74	18.15	17.8	
Vmin (p.u.)	0.9937	0.994 5	0.9953	0.996 1	0.996 8	0.9953	0.9964	0.9975	0.9986	0.9993	
Min angle (°)	-13.84	-13.55	-13.27	-12.98	-12.69	-13.42	-13.04	-12.89	-12.78	-12.62	
Line flow 1-2 (MVA %)	106	103	103	102	101	95	93	90	88	87	
			Wind f	arm conn	ected at l	ous 24					
Variable		P	owerWorld	l		Matlab					
Wind penetration	0%	25%	50%	75%	100%	0%	25%	50%	75%	100%	

Table 3. Results of LPOPF when connected wind farm with different wind penetration levels

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					. = .					
Slack bus (MW)	178	191	185	180	174	176	177	172	168	163
Cost(\$hr)	803.91	784.9 6	766.14	747.6 6	729.7 2	802.46	790.89	776.	764.63	753.42
Losses (MW)	10.54	10.45	9.89	9.39	8.95	10.31	9.03	8.85	8.34	7.96
Losses (Mvar)	20.23	20.05	19.83	19.71	19.58	19.67	19.03	18.61	18.11	17.83
Vmin (p.u.)	0.9937	0.997 2	1.0003	1.003 2	1.006 1	0.9953	0.9985	1.0014	1.0046	1.0061
Min angle (°)	-13.84	-13.44	-13.03	-12.64	-12.24	-13.42	-12.93	-12.74	-12.61	-12.5
Line flow 1-2 (MVA %)	106	103	102	102	101	95	93	89	88	87
			Wind farı	n connect	ted at bus	10 & 24				
	PowerWorld					Matlab				
Variable		P	owerWorld	l				Matlab		
Variable Wind penetration	0%	Po 25%	owerWorld 50%	75%	100%	0%	25%	Matlab 50%	75%	100%
Variable Wind penetration Slack bus (MW)	0% 178	P 25% 185	owerWorld 50% 174	75% 170	100% 161	0% 176	25% 170	Matlab 50% 159	75% 148	100% 138
Variable Wind penetration Slack bus (MW) Cost(\$hr)	0% 178 803.91	Po 25% 185 766.0 3	owerWorld 50% 174 729.58	75% 170 695.6 5	100% 161 661.7 3	0% 176 802.46	25% 170 758.89	Matlab 50% 159 736.91	75% 148 701.78	100% 138 680.59
Variable Wind penetration Slack bus (MW) Cost(\$hr) Losses (MW)	0% 178 803.91 10.54	Po 25% 185 766.0 3 9.85	owerWorld 50% 174 729.58 8.94	75% 170 695.6 5 8.76	100% 161 661.7 3 8.15	0% 176 802.46 10.31	25% 170 758.89 9.03	Matlab 50% 159 736.91 8.85	75% 148 701.78 8.34	100% 138 680.59 7.96
Variable Wind penetration Slack bus (MW) Cost(\$hr) Losses (MW) Losses (Mvar)	0% 178 803.91 10.54 20.23	Po 25% 185 766.0 3 9.85 19.1	owerWorld 50% 174 729.58 8.94 18.05	75% 170 695.6 5 8.76 17.73	100% 161 661.7 3 8.15 17.13	0% 176 802.46 10.31 19.67	25% 170 758.89 9.03 18.81	Matlab 50% 159 736.91 8.85 18.47	75% 148 701.78 8.34 18.0	100% 138 680.59 7.96 17.63
Variable Wind penetration Slack bus (MW) Cost(\$hr) Losses (MW) Losses (Mvar) Vmin (p.u.)	0% 178 803.91 10.54 20.23 0.9937	Po 25% 185 766.0 3 9.85 19.1 1.003 2	SowerWorld 50% 174 729.58 8.94 18.05 1.00572	75% 170 695.6 5 8.76 17.73 1.008 9	100% 161 661.7 3 8.15 17.13 1.019 3	0% 176 802.46 10.31 19.67 0.9953	25% 170 758.89 9.03 18.81 1.00745	Matlab 50% 159 736.91 8.85 18.47 1.00937	75% 148 701.78 8.34 18.0 1.01528	100% 138 680.59 7.96 17.63 1.01694
Variable Wind penetration Slack bus (MW) Cost(\$hr) Losses (MW) Losses (Mvar) Vmin (p.u.) Min angle (°)	0% 178 803.91 10.54 20.23 0.9937 -13.84	Po 25% 185 766.0 3 9.85 19.1 1.003 2 -13.4	SowerWorld 50% 174 729.58 8.94 18.05 1.00572 -13	75% 170 695.6 5 8.76 17.73 1.008 9 -12.43	100% 161 661.7 3 8.15 17.13 1.019 3 -12	0% 176 802.46 10.31 19.67 0.9953 -13.42	25% 170 758.89 9.03 18.81 1.00745 -12.81	Matlab 50% 159 736.91 8.85 18.47 1.00937 -12.69	75% 148 701.78 8.34 18.0 1.01528 -12.6	100% 138 680.59 7.96 17.63 1.01694 -12.05



Fig 3: Voltage profile when wind farm connected at bus 10 (Matlab)





Fig 4: Voltage profile when wind farm connected at bus 24 (Matlab)

Fig5: Voltage profile when wind farm connected at bus 10 & 24 (Matlab)

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Fig 6: IEEE 30-bus Electrical system of contouring \ marginal MW cost without Wind generator using PowerWorld



Fig 7: IEEE 30-bus Electrical system of contouring \ marginal MW cost without Wind generator using PowerWorld

8. CONCLUSION

This paper proposes the application of linear programming optimal power flow for a system that incorporates thermal units and wind farms during normal operation. The modified IEEE 30 system with six thermal generating units and two wind farms is used to analyse the impact of connected wind farm on the total generation cost, voltage profile, the power flow of transmission lines loaded, the active and reactive power losses, by optimally integrate the wind farm in power systems. Based on the technical results it has been concluded that an optimal integration, location and utilization of wind farms give significant benefit example like such as reducing in the fuel cost, real and active power losses, the power flow of transmission lines loaded with more than the allowable limit and amelioration in the voltage profile. The results obtained from different scenarios give a signal to the utility on what penetration level and location is optimal with respect to active

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power losses and voltage profile. Finally, the results are very much promising.

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