Prediction of Customer Churn using Fuzzy Balanced Probabilistic C-means Algorithm

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ABSTRACT

Churn prediction in telecom sector is a major task for any of the service providers to increase the telecom subscriber's worldwide and also to sustain in the competition. Prediction of churners for a company is always a difficult task due to the sparsity, hugeness and unbalanced nature of data. Generally the term churn indicates the customer who is dissatisfied with the services providing by the telecom provider, likely to unsubscribe from the services or leave the company. The main intension of churn prediction is to estimate the churners and to find out the accurate causes which dissatisfy the customer. To effectively assist the telecommunication organizations, this paper provides fuzzy based clustering methods to enhance the business strategies and marketing activities. A new clustering algorithm called Fuzzy balanced probabilistic c-means with α (distance measure) is used to identify the customers those are more prone to churn. FBPCM- a has more semantic strength and accuracy than traditional FCM. This paper also addresses the different issues related to fuzzy clustering for handling the data preprocessing steps, initial centroids, unbalanced datasets, distance measures and validity indices to get qualitative clusters. Experimentation was done on china telecom data to identify analogous group of clients who are more likely to prone to churn from the telecom services.

Keywords

Fuzzy clustering, Semantic Driven Subtractive Clustering Algorithm, FBPCM- α , Churn data

1. INTRODUCTION

Customer churn refers to shifting of customer from one company/organization to other company. Churning of customer is observed in various sectors; such as banking, financial services, telecommunication, social network services, online gaming and airlines [12] etc. This problem is mainly observed in telecom sector. So retention of customer is main concern for CRM (Customer Relationship management). Now a day's organizations are primarily concentrating on observing the behavior of a customer in a period of time for maintaining long-term relationship with their customers. Companies are adopting various data mining or machine learning techniques for knowledge discovery process [1] to find out hidden patterns for the given information. Companies realizing that acquiring a new customer is very difficult than maintain loyalty of existing customer. This fact attracted tele companies to invest in Customer Relationship Management to uphold customer information. This customer information is collected from historical data stored in CRM. To sustain in this competitive environment there is a lot of need for service providing organizations to analyze the factors that leads to customer churn. Churning of customer effects the company's performance is summarized as:

- (i) Losing the loyal customers (retention of new customer is more difficult task).
- (ii) Majorly causes the low sales because of limited customers.
- (iii) Competitors can promote their business by gaining the new customers.
- (iv) Overall performance of company may be affected.
- (v) Leading to major revenue loses.
- (vi) More risk to company's popularity in the competitive environment with loss of customer base.

Churn prediction analytics helps companies/organizations to assess valuable customers and to predict the customers those are more chance to churn. Identifying the features of particular group of customers those are more risk of churning can help for business enterprises. It helps in anticipating and managing of risk factors related with churning. Recognizing the key areas that help to enlarge the business value.

1.1 Clustering

Clustering is commonly used, most powerful and popularly used unsupervised method. Main procedure of clustering involves in gathering similar objects together or objects with common features into clusters (groups). Clustering [13] is majorly familiar with analyzing the data visually and used for efficient decision making process. Clustering is broadly used in a range of applications like education, field of computer science, marketing, insurance, surveillance detection, fraud detection and scientific discovery to mine the functional information from the data. The selection of distance measures and the category of data that a clustering algorithm cans effort is a decisive step in clustering. It defines how two elements are resemblance with each other and how this resemblance will impact the outline of the clusters. Another foremost difficulty in clustering process is to determine the goodness or validity of the cluster.

Clustering is mainly of two types Fuzzy Clustering and Hard Clustering. In hard clustering strictly each element is solely dedicated to one group only. In hard clustering, crisp sets are used to represent element's membership function to update the partition matrix, i.e. the membership function of objects in a cluster is represented in binary terms (either 0 or 1). Hard clustering obeys the condition of bivalent theory that elements either belong or not belongs to the cluster. In contrast, soft clustering contains the objects that are not solely belonging to any one of particular group; instead the fraction of membership function is used to cluster the objects, this type of clustering is called as Fuzzy clustering. So, fuzzy clustering does not restrict the membership function to binary value, it represented by real unit of interval [0, 1]. Noticed that main challenges while utilizing telecom data are: a) some of the existing DM algorithms cannot handle the churn data efficiently. Because of the fuzziness in churn data and due to the unbalanced data. b) Definition of "customer churn" in terms of fuzzy concept is a difficult task. For example how a company will define the customer loss? Is it based on no calling within or in arrears for more than 3 months (both prepaid and postpaid customers)? Is it based on elimination of telephone numbers etc. We need to define a set of rules that define the customer churn problem.

1.2 Imbalanced data

Imbalanced data or class imbalance is major problem facing by many of data mining and machine learning algorithms. The overall performance of the ML techniques can be degrades because of Imbalance data sets. As well as the overall accuracy also effects and decision making will be biased to the only majority class, this leads to formation of noisy data and also results in misclassification of classes in the minority class samples. This paper mainly concentrates on providing solution for class imbalance problem by using modification of existing fuzzy algorithms like FCM. Also while clustering choosing of approximates distance measure also provides solution.

In data preprocessing stage if dataset contains majority observations to one class and minority observations to another class leads to class imbalance. Simply imbalance data occurs when there is disparity or inequality among the response or class variable. This problem can be explained by using following example.

Consider a data set consisting of 3333 observations. This data set consists of description related to telecom churn data. Class label is churn. It contains two classes whether customer will churn or not. In 3333 observations: 2850 observations belong to class 1 and 483 observations belong to class 2. I.e. class1 probability is 0.8550855 and class2 probability is 0.1449145.

Some of the reasons why imbalance data effect the performance of algorithms:

- i) When there is disparity or inequality among the response or class variable, the accuracy of ML algorithm degraded.
- ii) This causes the biased towards majority class and less bias towards minority classes.
- iii) The overall error to which the minority class contributes very less.
- iv) ML algorithms imagine that the considered data set has unbalanced class distributions.
- v) They also imagine that errors obtain from various different classes have same cost.

Solution for Imbalanced data:

In data preprocessing stage some sampling methods can be used to balance data. Some of the sampling methods are under sampling, oversampling and synthetic data generation. But this results in varying the size of original data. Under sampling method try to reduce the records from majority class. Oversampling tries to increase the number of records from minority class. From these ways the ratio of the classes can be balanced. But by applying these methods the size of original dataset is varying a lot. So there is a need to propose an algorithm which itself can handle the dataset without any modification of data initially. This can be done by introducing a new algorithm called Fuzzy balanced probabilistic c-means with α (FBPCM- α).

2. RELATED WORK:

Several researches were done on this churn prediction. Previously many researchers provide a lot of effective ways in handling the literature for customer churn data management problem. Several analytical techniques such as machine learning, statistical measure models and various data mining approaches can be used. Castro and Tsuzuki introduced a frequency approach analysis based on (KNN)[2] k-nearest neighbor's machine learning algorithm for major attribute representation from data base login records for churn analytical modeling. Another neural network model is used to identify the top key attributes affecting churn based on the 80-20 rules [3, 4]. Awnag et al proposed regression customer churn prediction methods [5] that identify churners by multiple regression analysis. This model utilizes the small amount of customer feature data to generate good performance. Au et al proposed a (DMEL) data mining by evolutionary learning technique [6], to handle the classification problems. Furthermore, it is extended to predict different churn rates regarding telecom subscriber dataset. By using DM methods such as neural network, Decision tree and K-means, constructed predictive models for telecom data. Their empirical evaluation suggests that DM techniques can effectively recommend telecom company providers to make valuable and more accurate decisions. Verbraken et al. designed cost based benefit analysis [7] architecture to achieve maximum profit criterion. This architecture is then applied on churn data to handle churn problem of cost based benefit structure. Some of the genetic algorithms are also proposed by Idris et al [8]. In to handle this problem. Huang et al. in proposed a Meta heuristics [9] for handling the complex features of data, association rule generation is used to rule generation on customer churn data in telecom sector. A hybrid based firefly algorithm [10] also proposed that estimates the initial centroids for a given data and predicts the churning of customers. Several logistic regression techniques in combination of classification algorithms are used for prediction of customer churn. Recently, a robust boosting algorithm [11] has been applied successfully in banking industry churn problem. Although some of these methods can provide a solution for customer churn, there are certain limitations on data, such as unbalanced data, size of data, fuzziness in the data etc. For a data set class imbalance plays a significant role in affecting the accuracy and reliability of a classifier. The main issue in class imbalance is the scenario where the number of observations or records belongs to one class is very significantly lesser than those records which belong to other classes.

3. EXISTING CHURN FUZZY CONCEPT

Fuzzy based clustering method usually calculates the conditional probabilities of class and then class is chosen based on the expected probability. In contrast, non-fuzzy clustering method directly estimates the boundaries of class without any estimation of probabilities of class.

3.1 Fuzzy c means

Fuzzy c-means [14] is a most widely used clustering method in which each observation or data point belong to any of the cluster with degree specified by a membership function grade. This was proposed by Jim Bezdek in 1981. Consider a dataset with $X=\{x_1, x_2...x_n\}$ points in dimensional space. Input is the unlabeled dataset X from x_1 to x_n , where n denotes the total number of observations. Output is the cluster centers containing in the set $V=\{v_1, v_2...v_c\}$ where c represents the total number of clusters. Objective function or the performance index of the FCM to be optimized is shown in Equation (1):

$$J_{m} = \sum_{i=i}^{N} \sum_{j=1}^{C} U_{ij}^{m} \left| \left| X_{i} - C_{j} \right| \right|, 1 \le m \le \infty$$
(1)

Certain condition is induced on FCM [14] as each of the entries in U lies in [0, 1]; i.e. the sum of each row should be more than zero; and the sum of each column should be equals to 1. Condition to be satisfied is: $\sum_{i=1}^{c} U_{ik} = 1$, for all k

Algorithm steps:

Step1: Initially initialize the fuzzy partition or membership matrix.

Step2: Now calculate the initial cluster centers based on Vij

$$V_{ij} = \left(\frac{\sum_{k=1}^{N} (U_{ik}^m)^2}{\sum_{k=1}^{N} (U_{ik}^m)^2} X_{kj}\right)$$
(2)

Step3: Updation of membership matrix is done based on formulae Uik equation (3), Condition is that $\sum_{i=1}^{c} U_{ik} = 1$

$$U_{i,k} = \left(\sum_{j=1}^{c} \left(\frac{d_{ik}}{d_{jk}}\right)^{\frac{2}{m-1}}\right)^{-1}$$
(3)

Step4: Repeat this process until the convergence criteria $\max \left| |U_{ik}^{(r+1)} - U_{ik}^{r}| \right| \le \epsilon \text{ is met.}$

3.2 SDSCM

It is the new clustering algorithm used to produce the initial cluster centroids. It is developed by combining the fuzzy c-mean algorithm with subtractive clustering method. The cluster results from Fcm are used to pass initial parameters for the SCM in the following ways:

1. Compute the sum of absolute differences of $\mu n(xk)$

$$P_{i} = \sum_{k=1}^{n} \left| \mu_{\eta}(x_{i}) - \mu_{\eta}(x_{k}) \right|$$
(4)

2. Select minimum value of pi as the first cluster centroid.

$$P_1^F = \min\{P_i\} \quad x_1^F = x_i \tag{5}$$

3. Calculate neighborhood radius T1

$$d_{i} = |x_{i} - x_{1}^{F}|^{2} \qquad d_{x} = \frac{1}{n} \sum_{i=1}^{n} d_{i} \quad \tau_{i} = \frac{1}{n} \sum_{i=1}^{n} (d_{i} - d_{x})$$
(6)

4. To avoid getting closer centroids, set weight coefficient as

T2 = 1.5 * T1

5. Compute the mountain function of xi from equation (7)

$$M_{1}(x_{i}) = \sum_{j=1}^{n} \exp\left(-\frac{||x_{i} - x_{j}||^{2}}{\left(\frac{\tau_{1}}{2}\right)^{2}}\right)$$
(7)

6. Select the maximum mountain function

7. Update the mountain function by equation (8)

$$M_{i}(x_{i}) = M_{1}(x_{i}) - M_{l-1}^{*} \exp\left(-\frac{||x_{i}-x_{j}||^{2}}{\left(\frac{\tau_{1}}{2}\right)^{2}}\right)$$
(8)

8. Repeat until $\mu_l^* < \varepsilon \mu_1^*$ convergence criteria is met.

9. Finally output the cluster centroids.

Now this initial seed points will be passed to the kmeans algorithm to obtain the desired cluster outputs.

3.3 Disadvantages

The below table 1 example contains the 4 records with two features. Now calculate the initial centroids and membership values to assign the data points to the any of two clusters. Example:

Table 1. Example records for FCM

Х	Y
1	3
1.5	3.2
1.3	2.8
3	1

First step is to assign the membership value to each data point representing 1 or 0. 1 means the data point belongs to the corresponding cluster, 0 means the data point is not belonging to the corresponding cluster.

$$\mathbf{U}^{0} = \begin{vmatrix} 1 & 1 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{vmatrix} \begin{vmatrix} \mathbf{C} 1 \\ \mathbf{C} 2 \end{vmatrix}$$

Now calculate the initial centroids by using V_{ij} formulae.

 $V_{11}=1(1)+1.5(1)+1.3(1)+3(0)/(1+1+1)=1.21$. Similarly calculate the initial centroids for all each cluster with respect to each feature as shown in table2.

Table 2. Initial centroids for FCM

V ₁₁ =1.21	V ₂₁ =3
V ₁₂ =3.0	V ₂₂ =1
C ₁ =[1.26,3.0]	C ₂ =[3,1]

Distance between data point to each cluster centroid is calculated as shown in table 3. $D_{11}=sqrt((1-1.26)^{2}+(3-3)^{2})$

Table 3. Distance between each point to centroids

D ₁₁ =0.26	D ₂₁ =2.82
D ₁₂ =0.31	D ₂₂ =2.66
D ₁₃ =0.20	D ₂₃ =2.47
D ₁₄ =2.65	D ₂₄ =0

Now update partition matrix by $U_{11} = \left[\left(\frac{d_{11}}{d_{11}}\right)^2 + \left(\frac{d_{11}}{d_{21}}\right)^2\right]$ Now U₂₁ is calculated by subtracting U₁₁ from 1. U₂₁=1-U₁₁

Final membership matrix is:

Problem for FCM:

As shown in fig 1 when the data points that are equidistant from the cluster centroids are formed problem will arise. Here the data points X_{11} and X_{12} are equidistant from the centroids. The membership value for data point $U_{11}=0.5$ and $U_{21}=0.5$. Here typicality of U_{11} and U_{21} are lost because unable to describe whether the data point U_{11} belongs to cluster 1 or cluster 2(because both have the same probability as 0.5). Typicality arises when not able to classify the data point to a particular cluster. So Typicality of X_{11} is lost.



Fig 1: Problem for FCM

Disadvantages:

- a. very sensitive to good initialization
- b. Sometimes results in coincident clusters
- c. May take long computational time
- d. Unbalanced data may not be handled well.
- e. More sensitivity to noise in data and outliers.

4. PROPOSED METHODOLOGY

FBPCM- α : **Fuzzy Balanced Probabilistic C Means:** To overcome the limitations of SDSCM a new clustering algorithm called FBPCM- α is proposed. In objective function along with the sum of within fuzzy fluctuations, sum of the between fuzzy cluster fluctuations are also introduced in this FBPCM- α .

Input: Unlabeled data set $X = \{x_1, x_2, k, ..., x_n\}$ n is the number of data point in X. $X_k \in \mathbb{R}^p$ R is the real number set. P is the number of features in each vector.

Output: Set of vectors $V = \{V1, V2, K, ..., Vc\} \subset R^p$ V_i is called "cluster center". Along with that a c-partition of X, which is $c \times n$ matrix U.

Here a data point belongs to more than one cluster at a time. This algorithm main aim is to optimize the objective function as shown in equation (9):

$$O_{FBPCM-\alpha}(U,T,V) = \sum_{i=1}^{C} \sum_{k=1}^{n} (U_{ik}^{m} + T_{ik}^{n}) \propto_{ik}^{2}$$
(9)

The membership U_{ik}^m need not satisfies relationship $\sum_{k=1}^{c} U_{ik}^m = 1$ for all i = 1,2,3...n. Where $0 \le U_{ik}^m < 1$, $0 \le T_{ik}^n < 1$ and m > 1. Both these factors are important. To assign a data point to cluster, data point must be closest to the centroid \rightarrow Membership. For typically decrease the undesirable effect of outliers on the cluster results there is a need for estimating the centroids. So remove the constraint $\sum_{i=1}^{c} U_{ik} = 1$. Introduce a new term called T_{ik} as shown in equation (11) which removes the constraint $\sum_{i=1}^{c} U_{ik} = 1$.

- U_{ik} is influenced by the position of all c cluster centroids.
- Whereas T_{ik} is affected by only one in c

Both of these terms are important to classify a data point because cluster centroid has to be closest to data point membership. The sum of within fuzzy cluster fluctuations must be small to optimize the objective function. The sum of between fuzzy cluster fluctuations must be large to optimize the objective function. This between cluster logic is included in T_{ik}^n and the within cluster logic is included in U_{ik}^m .

Table 4. Variable description for FBPCM

U _{ik} ^m	It describes the membership of data point xi in cluster k (where i range from 1C, K ranges from 1n). U_{ik}^m is a function of X_k and all c centroids
m	is the membership degree
T_{ik}^n	Whereas T_{ik} is affected by only one in clust c
\propto_{ik}^2	It specifies the distance measure between 'xi' and cluster center V_k
V _{ij}	Vector of initial cluster centroids

4.1 Algorithm of FBPCM- α:

Step1: The first initialization of partition matrix is done based on initially passed centroids.

Step2: Now calculate the initial cluster centers based on V_{ii} .

$$V_{ij} = \left(\frac{\sum_{k=1}^{n} (U_{ik}^{m} + T_{ik}^{m}) \times X_{kj}}{\sum_{k=1}^{n} (U_{ik}^{m} + T_{ik}^{m})}\right)$$

Step3: Updation of membership matrix is done based on formulae U_{ik} and $T_{i,k}$.

Where
$$U_{i,k} = \left(\sum_{j=1}^{c} \left(\frac{\alpha_{ik}}{\alpha_{jk}}\right)^{\frac{2}{m-1}}\right)^{-1} for all i, k$$
 (10)

$$T_{i,k} = \left(\sum_{j=1}^{n} \left(\frac{\alpha_{ik}}{\alpha_{ij}}\right)^{\frac{1}{m-1}}\right)^{-1}$$
(11)

Step4: Repeat this process until the convergence criteria $\max \left| \left| U_{ik}^{(r+1)} - U_{ik}^{r} \right| \right| \le \epsilon \text{ is met.}$

 \propto_{lk}^2 is the one of following distance measures:

W

Euclidean distance $D(X, V) = \sqrt{\sum_{i=1}^{N} (X_k - V_i)^2}$, Manhattan distance $D(X, V) = \sum_{i=1}^{N} |(X_k - V_i)|$, Pearson correlation distance, Eisen cosine correlation distance, Kendall correlation distance and Squared Euclidian distance measure: $D(X, V) = \sum_{i=1}^{N} (X_k - V_i)^2$. Due to $T_{i,k}$ the typicality of a data point to a cluster, will be normalized with respect to the distance of all n data points from that cluster.

5. IMPLEMENTATION

To conduct the experiment china telecom dataset is considered. Churn data set contains 3333 records with 19 attributes as shown in table 5.

Table 5. Attribute description for churn data set

Features	Description	
State	State of customer	
Account length	How long the account has been active	
area code	Area code for customer in a state	
Inter plan	Whether subscribed for inter plan or not	
voice mail plan	Whether subscribed for voice mail plan	
tot day minutes	Count of total day minutes	
total day calls	Count of total day calls	
tot day charge	Count of total cost of day charge	
tot eve minutes	Count of tot number of evening minutes	

Tot eve calls	Count of tot number of evening calls	
tot eve charge	Count of total cost of evening charge	
tot night min's	Count of tot no. of min's in night time	
total night calls	Count of tot no. of calls in night time	
tot night charge	Count of total cost of night charge	
tot intl minutes	Count of tot no. of international minutes	
tot intl minutes tot intl calls	Count of tot no. of international minutes Count of tot no. of international calls	
tot intl minutes tot intl calls total intl charge	Count of tot no. of international minutes Count of tot no. of international calls Count of total international charge	
tot intl minutes tot intl calls total intl charge cust service calls	Count of tot no. of international minutes Count of tot no. of international calls Count of total international charge Count of tot no. of service calls	

Last attribute churn contains values 1 and 2.

- 1. False (customer will not churn)
- 2. True (customer will churn)

5.1 Data preprocessing

It is undeniable that 80% of a data scientist's time and effort is spent in collection, integration, cleaning and preparing the data. Generally datasets consists of various sizes and different structures, this data need to be prepared to analyze the data.

5.1.1 Data Cleaning

Correcting inconsistent data. Churn data does not contain any missing values.

5.1.2 Data Integration

Schema integration, handling redundancies in data. Dataset is downloaded from https://WWW.kaggle.com/becksddf/churn-in-telecoms-dataset

5.1.3 Data Transformation

Removing any noise from the data. Data is converted into common format which is used for formatting. This is done by normalization, generalization and aggregation. Z-score normalization technique is applied equation (12) to dataset for scaling the values in the range of [0, 1]. After applying normalization time required executing an algorithm is significantly reduced. Moreover accuracy will be increased.

$$Z = \frac{Y - MEAN(Y)}{SD(Y)}$$
(12)

5.1.4 Data Reduction:

Reduction of unnecessary features of data based on requirement. Unwanted attributes from the data are removed. It is the most important decisive step to reduce the time complexity. This can be done by using clustering based feature selection methods. They are: filter methods and wrapper methods. Filter methods mainly concentrate on single factor analysis. The predictive capability of every entity variable is evaluated.

Method	Formulae	
Information gain	$ENTROPY(A) = \sum_{I=1}^{K} -C_I \log_2 C_I$ $IG = E(class) + E(attr) - E(class, attr)$	
Gain ratio	$\frac{E(class) + E(attr) - E(class, attr)}{E(attr)}$	
Symmetric relevance	$2*\frac{E(class) + E(attr) - E(class, attr)}{E(attr) + E(class)}$	
Subset selection	Start with fitting all combination of models with the given features that have k predictors, out of these k predictors select the p predictors.	
Forward Selection	Start with no predictors, search through all the single-variable models that best fits and Continue until some stopping rule is satisfied for a threshold value.	
Backward Elimination	Start with all the predictors, Now remove the variable with least statistically significant and Continue until a stopping rule is reached for a threshold value.	
Correlation	$COR(Y, X) = 1 - \left(\frac{\left(\sum_{l=1}^{N} (Y_l - Y_l)^2 (X_l - X_l)^2\right)}{\sqrt{\sum_{l=1}^{N} (Y_l - Y_l)^2 \sum_{l=1}^{N} (X_l - X_l)^2}}\right)$	

It contains some of methods like: Information gain, correlation measure, Gain ratio and symmetrical relevance. In wrapper methods the predictive and analysis capability of the variable or feature is evaluated jointly with comparison of other variables from data set. It contains some methods like subset selection, backward subset elimination and another important one is forward subset selection methods. These can be applied the dataset based on formulas of table 6:

5.1.5 Data Discretization

Partition the range of continuous attribute of data into intervals.

6. EVALUATION INDEXES:

To evaluate the performance of FBPCM- α following evaluation indexes are used. In general the classical indexes for analysing clustering results are betweenness (separation), withinness (compactness) and EVA. Furthermore to calculate the semantic strength new an evaluation index called SS and SSE (semantic strength expectation) is used.

a) **SPT:** SPT specifies the degree of separation between the clusters equation (13). The cluster quality increases with decrease in SPT.

$$SPT = \min \left| \left| v_i - v_j \right| \right|^2$$
(13)

b) CMP: CMP specifies the degree of withinness or tightness of the clusters equation (14). The cluster quality increases with increase in CMP.

$$CMP = 1/N \left(\sum_{j=1}^{N} \sum_{i=1}^{C} \mu_{ij}^{m} \left(x_{j} - v_{i} \right)^{2} \right)$$
(14)

c) EVA: However these two cannot completely reflect the overall performance of clustering. So EVA is used. The cluster quality increases with decrease in EVA. EVA = CMP/SPT

Table 7. Variable description for evaluation indexes

Sym	Description
v _i	The centroid of i^{th} cluster and $ v_i $ is the number of data points belonging to the cluster with centroid v_i
vj	The centroid of j th cluster
xj	The data point
N	The total number of data points
μ^m_{ij}	The membership of the j th data point
C	The number of clusters
μ^m_{ij}	The membership of x_j based on fuzzy concept

d) SS: Semantic strength describes the overall average membership of each cluster based on the explicit fuzzy concept equation (15). Thus if the SS is higher, then automatically membership of cluster will be higher. Variable description are shown in table 7.

$$SS(\mathbf{v}_{i}) = \frac{\sum_{x_{j} \in \mathbf{v}_{i}} \mu_{n}(x_{j})}{\left\| \mathbf{v}_{j} \right\|}$$
(15)

e) **Accuracy:** It describes how well the predictions done by our model are correct from equation (16). For determining accuracy construct a confusion matrix.

Table 8. Confusion matrix

MATRIX	Same cluster	Distinct clusters
Same class	true positive(TP)	false negative(FN)
Diff classes	false positives(FP)	true negative(TN)

From table 8 TP denotes true positive, it occurs while taking a decision to assign two similar points to the same cluster, TN denotes a true negative; it occurs while taking a decision to assign two unequal or dissimilar points to the distinct clusters. FP denotes false positive, it occurs while taking a decision to assign two unequal or dissimilar points to the identical cluster. FN denotes the false negative it occurs while taking a decision to assign two alike or similar points to distinct clusters.

$$Accuracy(E) = \frac{TP + TN}{TP + TN + FP + FN}$$
(16)

f) **SSE:** Moreover SSE is defined as the product of maximum clustering accuracy and Semantic strength of cluster. $SSE = max_{j \in I} (E * SS(c_j))$, Where E represents the Accuracy. The rise in value of SSE results in increase of quality of clustering.

7. RESULTS AND EXPERIMENTAL ANALYSIS:

7.1 Data normalization

Based on the dataset preprocessing techniques need to be applied. Basic k-means algorithm is applied on the churn dataset to find out best normalization technique that optimizes the accuracy and reducing time complexity. The results indicate that without applying normalization technique, by applying algorithm directly takes 3.5 minutes for execution. So Z-score normalization technique is applied as show in table 9. Z-score Normalization executes in 1.463876 seconds, accuracy=0.48453.

Table 9. Normalization results

Technique	Time	Accuracy
Without normalization	3.528135 minutes	0.3595545
Z-score Normalization	1.463876 seconds	0.48453

7.2 Data Reduction: Without applying feature selection the clustering results are obtained as shown in following figure. Clusters are not densed and well separated. So selection of important features to perform analysis is an major task. Apply clustering feature selection techniques like information gain, gain ratio, Symmetric relevance, subset selection, forward selection, backward elimination and correlation. Then check the accuracy, the technique that results in more accuracy is the best feature selection method.



Fig2: Clustering result without feature selection

As shown in table 10 information gain selects 6 features, gain ratio selects 10 features, Symmetric relevance selects 10 features, subset selection selects 7 features, forward selection selects 6 features, backward elimination selects 6 features and correlation selects 9 features. Among these information gain measure results in more accuracy. It selects the attributes total day minutes, total day charge, customer service calls, international plan, voice main plan, total international minutes and total international charge as an important features.

Table 10. Feature selection results

Feature selection	Number of features selected	Accuracy
Information gain	6	0.5334533
Gain ratio	10	0.45689
Symmetric relevance	10	0.432589
Subset selection	7	0.530153
Forward selection	6	0.43265
Backward elimination	6	0.496285
Correlation	9	0.526955

7.3 kmeans

Complexity of any clustering algorithm depends on type of data, size of data, dimensionality. For K-Means clustering algorithm complexity depends on initial seed points, selection of k value, dimensionality reduction and number of iterations. By applying k-means algorithm without passing initial cluster centers, for every iteration clusters, evaluation indexes, time

and number of iterations will vary as shown in table 11. Initial seed points should be obtained from FBPCM- α algorithm.

	1	1	1		
	Centers	Accuracy	Time	Iterations	
Iter1	1675 1657	0.54875	1.69845	17	
Iter2	1658 1675	0.5489	1.45966	10	
Iter3	1676 1657	0.4551	1.512545	11	
Iter4	1600 1673	0.36545	1.546545	12	
Iter					
Iter99	1675 1658	0.65455	1.5456	10	
Iter100	1673 1600	0.98445	1.78566	18	
Average		0.5560771	1.0713902	10.42	

Table 11. Results for k-Means

7.4 FBPCM-*α*

Membership values: Table 12 shows the membership value of each data point from 1 to 3333 to the corresponding clusters. The data point with the maximum membership value is assigned to a corresponding cluster. Example the for data point one the membership value for cluster 1 is 0.3171747 and for cluster 2 is 0.6828253. So the data point one will be assigned to the cluster 2. The table 13 shows the initial cluster centroids returned by the FBPCM algorithm. Totally for every feature with respect to the cluster the centroid will be returned.

Table 12. Membership values for FBPCM algorithm

	Cluster 1	Cluster 2
1	0.3171747	0.6828253
2	0.5594513	0.4405487
3	0.3059092	0.6940908
3331	0.56745	0.44310
3332	0.4539787	0.5460213
3333	0.3830760	0.6169240

	Inter plan	Voice plan	Tot day min's
Clust1	-0.003713760	-0.6183035	0.00104126
Clust2	0.009711361	1.6168435	-0.0027228
	Tot day charge	Tot intl min	Custservice calls
Clust1	0.001042230	0.000814844	0.01102061
Clust2	-0.002725398	-0.00213071	-0.02881853

7.5 Clustering results

The figure 3 shows two clusters. Cluster 1 designates the customers those are not churn and cluster 2 designates the customers those are prone to churn.

In Cluster1: international plan: NO, voice main plan: Yes, total day minutes: more, total day charge: low, customer service calls: low, total international minutes: low In Cluster2:

International plan: Yes, voice main plan: No, total day minutes: Less, total day charge: More, customer service calls: More, total international minutes: More



Fig3: Result of FBPCM clustering

7.6 Evaluation indexes for churn dataset

The table 14 shows the evaluation indexes like accuracy, CMP, SPT, EVA and SSE for various algorithms. Among these algorithms FBPCM- α results in more accuracy. Moreover SPT is higher, CMP is lower, EVA is lower and SSE is maximum which results in increase of quality of cluster. So FBPCM has the more accuracy, high separation, low compactness, low EVA and higher SSE. So FBPCM algorithm gives the better clustering results compared to the other algorithms such as SDSCM, SCM and FCM. Fig 4 shows the bar plot representation of evaluation indexes among all algorithms the highest accuracy is 0.9249626 for FBPCM algorithm, Highest SPT is 0.4998145 for FBPCM, low CMP 0.01326774 is for FBPCM algorithm, low EVA is 0.03334784 for FBPCM algorithm.

Table 14. Evaluation index table for chur	1 data
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Algorithm	Accuracy	SPT	CMP	EVA	SSE
SDSCM	0.8352	0.471	0.015	0.044	0.790
SCM	0.7011	0.461	0.0143	0.045	0.722
FCM	0.7677	0.431	0.0142	0.041	0.771
FBPCM	0.9249	0.499	0.0132	0.033	0.913





Fig4: Bar plot representation for evaluation indexes

SS represents the semantic strength of FBPCM- α algorithm. From fig 5 cluster 1 has more semantic strength than cluster 2 as shown in figure. From the clustering results we can say those customers who subscribed for voicemail plan, talk more minutes in a day, paid the less charge and who does less number of customer calls have low risk of churning. Those customers who subscribed for international plan, talk less minutes in a day, paid the high charge for talk time, who not subscribed for voice mail plan and who does more number of customer calls have more porn to churn.



Fig5: Semantic Strength for FBPCM clustering algorithm

8. CONCLUSION

In this paper, mainly concentrate on providing the marketing companies with most effective techniques to reduce the churning of customers. First proposed a new clustering method called FBPCM based on FCM and PFCM. FBPCM improves clustering accuracy of SDSCM and K-means. Moreover, it reduces the risk of vague operations by using fuzzy concept. Experiment results indicate that FBPCM has stronger clustering semantic strength than SDSCM and FCM. Secondly, the customer churn problem in China telecom data is solved with FBPCM clustering algorithm. In this case, the Evaluation indexes are measured to test the performance issues related to the proposed FBPCM clustering algorithm. Experimental results indicate that the marketing simulation activities are essential to retain maximizing profits for organizations. Moreover the organizations should concentrate on loyal customer's retention and need to pay more attention towards customers. In conclusion, the whole process of solution for customer churn in China Telecom has presented the novel insights for service providers, managers to expand the level of customer churn management more accurately. In the future, the algorithm can be improved further to validate the effectiveness in terms of other risk analysis and can use more abundant platform like big data for implementation.

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