Computational Intelligence based Data-Driven Modeling: A case Study in Hydrology

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ABSTRACT
Nonlinearity exists in most of the real phenomenon and it is difficult to model the behaviour of such indefinite systems. Neural computing is one the important tools for modeling the nonlinear structures and efficiently applying in the measurement of inexplicit systems. The monsoon rainfall in Pakistan shows an important part in upstream flow in the Upper Indus Basin (UIB). This study, suggests different Dynamic Neural Network (DNN) models, based on time delayed autoregressive structures, for the upstream water flow of Tarbela Dam on upper Indus basin. The appropriateness of the models for training, validation and testing phases exhibits the accuracy of the models. This paper also gives a major preference when only the upstream flow gauge stations data are available, which can be beneficial for water-resource engineers.

General Terms
Computational Intelligence, Time Series Forecasting

Keywords
Upper Indus Basin, Dynamic Neural Network, Upstream water flow.

1. INTRODUCTION
Monsoon precipitation plays a significant part in discharge in Indus River and its tributaries from April to September [1]. Yearly precipitation changes from 1000-1400 mm in the whole area. Around 10% of the precipitation is lost by dissipation and about a 41 million section of land foot is lost by leakage from unlined trenches [2]. The losses could have been minimized with the suitable stream-flow estimating and enhancing the stream structures in Pakistan. We have different methods for estimation of stream flow analysis, such as estimation of hydrological parameter etc. A study estimates the risk of flood in River Indus of Pakistan by utilizing recorded information of most peak discharges which calculates the return period of various dams in Pakistan using probabilistic distributions e.g. Weibull distribution, Pearson type-3 analysis. GIS technique is also used for assessing the flood risk. A recent study has been employed nonlinear techniques of forecasting to analyze the long-term stream flow of the Indus River. On the other hand, completed a thorough study on the flood determining framework for the using a simulated neural system (NN) model [3] and they have reported that there is a space for further improvement for the NN model. During most recent couple of decades, different techniques have been produced for forecasting in which ARMA or NN model building methodologies are well accepted. The aim of this paper is to develop some Neural Network models of upper Indus Basin at Tarbela Dam. The other phase of this research is that it gives an inclination if only the observations of upstream flow station is possible, which might have been valuable for water-resource organizers.

2. RELATED WORK
Pakistan has different types of climatic conditions in different parts of the country. We see the extreme variations of temperature seasonally. The climate extremes in Pakistan incorporate high and low temperatures, heaviest precipitation which causes floods. Flood disasters in Pakistan are regularly activated by strong Indus River. The Indus River is an important trans-limit stream in Asia with nine tributaries. Its five tributaries on the left bank are the Beas, Chenab, Jhelum, Ravi, and Sutlej streams. The fundamental right bank tributaries are the Gomal, Kabul, Swat and Kurram streams. During the last few decades, Pakistan has encountered different catastrophic disasters activated by monsoon expected floods. According to the Asian Development Bank, Pakistan has run into twenty notable floods somewhere around 1950 and 2012 that guaranteed a sum of 8,887 human lives and delivered harm to 109,822 in towns with an expected financial loss of $19 billion. The significant reason for flooding in Pakistan is devastating inspired precipitation in the stream catchments which at times delayed by snowmelt streams that result the floods in most of part of streams during the monsoon season. In the upper Indus Basin, flood-water overflowing the riverbanks for the most part comes back to the stream. Besides, in the lower Indus Basin (Sindh, Pakistan) which is basically streaming at a higher rise than adjoining lands, the spill streams don't come back to the river. Flood risk can be estimated by using probability theory and its related conclusion. So, the risk analysis is performed by the occurrence of flood events [4]. The forecast of meteorological time series exhibits a vital part in many fields. ARMA models have been utilized for demonstrating water asset time series in light of the fact that such models are acknowledged as a standard representation of stochastic time series [5]. However, such models don't endeavor to the non-direct flow innate in the hydrologic systems, and may not generally perform well [6]. A recent study has employed nonlinear methods for analysis and forecasting the continuing regular behavior of the Indus Basin. A utilization of least squares support vector machine (LS-SVM) for transitory expectation of meteorological time series (e.g. solar irradiation, air temperature, relative humidity, wind speed, wind direction and pressure) was presented by [7] and this study indicates that LS-SVM gives promising results to transient forecast of meteorological information.
3. DATA DESCRIPTION AND LOCATIONS
The Indus River is around 2,800 km long, with 2,682 km of it, extended in the middle of northern and southern bounds Pakistan. Its alluvial plain zone is around 207,200 km while its deltaic region is about 20,000 km. It starts in the Tibetan tableland, on Kailas Parbat (mountain) close to Mansarwar Lake. It then goes through the Himalayan range, and gathers overflow from the Hindu Kush and Suleiman ranges. In upper to mid district scopes of Indus Basin, are the fundamental tributaries like Jhelum and Chenab reasons for floods, stream floods especially hit Punjab and Sindh. Tarbella Dam is the world largest earth fill dam on the Upper Indus Basin (UIB) in Khyber Pakhtunkhwa in Pakistan and also largest by structural volume.

For upstream flow forecasting model, it is not improved to make use of rainfall precipitation because of the elongated difference in time (order of days) between rainfall and the consequent river water flow. In other words, there is a weak correlation between rainfall and flows. So, the utilization of stream flow observations is most likely to adopt for the good upstream flow forecasting model. This paper considers mean monthly upstream flow observations of upper Indus Basin (UIB) i.e. Tarbella Dam from April to September (rainfall season) for each year, ranging from 1977 to 2012 as in Figure 1.

4. NEURAL NETWORK
Neural Network (NN) [8, 9] is one of the major research area, unaided or integrated, in the paradigm of computational intelligence. NN consist of neurons functioning in parallel which are inspired by biological nervous phenomena. In general, functioning of the NN depends on the interconnection between the neurons and train the network by adjusting the values of the connections, called weights. The Figures 2 and 3, as a pictorial example, exhibit the procedure of NN.

5. PROPOSED MODELS OF DNN
The Dynamic Neural Network (DNN) models are based on the following known inputs and the target variable $Q_t$ depends on nonlinear autoregressive structure in which the predicted series built on past or delayed observations. DNN is a three-layers model consist of one input, one hidden layer with different number of neuron (based on the behaviour of the system) and a single output layer. Integrated with 70% observations set for training, 5% for validation and 25% for testing purpose.

Table 1. Dynamic Neural Network functional models

<table>
<thead>
<tr>
<th>Model No.</th>
<th>Delayed Inputs Functional Models</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>$Q_t = f (Q_{t-1}, Q_{t-2})$</td>
</tr>
<tr>
<td>2</td>
<td>$Q_t = f (Q_{t-1}, Q_{t-2}, Q_{t-3})$</td>
</tr>
<tr>
<td>3</td>
<td>$Q_t = f (Q_{t-1}, Q_{t-2}, Q_{t-3}, Q_{t-4})$</td>
</tr>
<tr>
<td>4</td>
<td>$Q_t = f (Q_{t-1}, Q_{t-2}, Q_{t-3}, Q_{t-4}, Q_{t-5}, Q_{t-6})$</td>
</tr>
</tbody>
</table>

$Q_t$ = Mean monthly upstream water flow at time $t$
$Q_{t-1}$ = Mean monthly upstream water flow at time $t-1$ (lag 1)
$Q_{t-2}$ = Mean monthly upstream water flow at time $t-2$
(lag 2)
\( Q_{t-3} \) = Mean monthly upstream water flow at time \( t-3 \)
(lag 3)
\( Q_{t-4} \) = Mean monthly upstream water flow at time \( t-4 \)
(lag 4)
\( Q_{t-5} \) = Mean monthly upstream water flow at time \( t-5 \)
(lag 5)
\( Q_{t-6} \) = Mean monthly upstream water flow at time \( t-6 \)
(lag 6)

**Standard Training Parameters**

- Total number of epochs: 1000
- Minimum gradient: 1.0 e-07
- Initial step size (\( \mu \)): 0.001
- Step decrementing rate: 0.10
- Step incrementing rate: 10
- Maximum step size: 1.0 e+10

**Training function**
The Levenberg–Marquardt (LM) method [10, 11] is used in training phase for predicting of nonlinear system of upstream flow at Tarbella Dam because LM is a standard optimization technique for nonlinear least-squares problems.

**Evaluation Metrics**

- Mean Squared Error = \( MSE = \frac{\sum_{i=1}^{n}(Q_i^{o} - Q_i^{f})^2}{n} \)
- Root Mean Squared Error = \( RMSE = \sqrt{MSE} \)
- Coefficient of Correlation = \( R = \left[ \frac{\sum_{i=1}^{n}(Q_i^{o} - \bar{Q}^{o})(Q_i^{f} - \bar{Q}^{f})}{\sqrt{\sum_{i=1}^{n}(Q_i^{o} - \bar{Q}^{o})^2} \sqrt{\sum_{i=1}^{n}(Q_i^{f} - \bar{Q}^{f})^2}} \right] \)
- Coefficient of Determination = \( R^2 = \frac{\sum{(Q_i^{f} - \bar{Q}^{f})^2}}{\sum{(Q_i^{o} - \bar{Q}^{o})^2}} \)

where \( Q_i^{o} \) = observed upstream flow at time \( t \)
\( Q_i^{f} \) = forecasted upstream flow at time \( t \)
\( \bar{Q}^{o} \) = mean of observed upstream flow
\( \bar{Q}^{f} \) = mean of forecasted upstream flow

### 6. RESULTS AND DISCUSSION

#### 6.1 DNN Model 1
- Number of neurons in hidden layer: 10
- Number of delays: 2

#### 6.2 DNN Model 2
- Number of neurons in hidden layer: 10
- Number of delays: 3
6.3 DNN Model 3
Number of neurons in hidden layer 12
Number of delays 4

6.4 DNN Model 4
Number of neurons in hidden layer 12
Number of delays 6

6.5 Models’ Evaluation Metrics
The following tables of evaluation metrics of DNN models are given for mean monthly upstream flow at Tarbela Dam and will select a network model on the basis of the following criteria:

a. Network model has maximum value of the coefficient of correlation ($R$) on the validation set to test forecasts.

b. Network model has maximum value of the coefficient of determination ($R^2$) on the validation set to test forecasts.

c. Network model has minimum error (RMSE) on the validation set to test forecasts.

<table>
<thead>
<tr>
<th>Model No.</th>
<th>Training</th>
<th>Validation</th>
<th>Testing</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>0.8901</td>
<td>0.8012</td>
<td>0.8287</td>
</tr>
<tr>
<td>2</td>
<td>0.8967</td>
<td>0.8245</td>
<td>0.8707</td>
</tr>
<tr>
<td>3</td>
<td>0.9282</td>
<td><strong>0.9176</strong></td>
<td>0.8614</td>
</tr>
<tr>
<td>4</td>
<td>0.96</td>
<td>0.8781</td>
<td>0.8894</td>
</tr>
<tr>
<td>Model No.</td>
<td>Training</td>
<td>Validation</td>
<td>Testing</td>
</tr>
<tr>
<td>----------</td>
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<td>---------</td>
</tr>
<tr>
<td>1</td>
<td>0.79228</td>
<td>0.641921</td>
<td>0.6867</td>
</tr>
<tr>
<td>2</td>
<td>0.80407</td>
<td>0.6798</td>
<td>0.7581</td>
</tr>
<tr>
<td>3</td>
<td>0.86156</td>
<td>0.84199</td>
<td>0.742</td>
</tr>
<tr>
<td>4</td>
<td>0.9216</td>
<td>0.77106</td>
<td>0.791</td>
</tr>
</tbody>
</table>

Table 4. Evaluation criteria of RMSE

<table>
<thead>
<tr>
<th>Model No.</th>
<th>Training</th>
<th>Validation</th>
<th>Testing</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>39881</td>
<td>30306.2</td>
<td>38032.4470</td>
</tr>
<tr>
<td>2</td>
<td>38763.7</td>
<td>45715.73</td>
<td>43165.4175</td>
</tr>
<tr>
<td>3</td>
<td>31678.8</td>
<td>27051.51</td>
<td>38600.0824</td>
</tr>
<tr>
<td>4</td>
<td>21893.9</td>
<td>46340.95</td>
<td>38824.6858</td>
</tr>
</tbody>
</table>

7. CONCLUSIONS
This paper presented the pursued of our research for developing Neural Network based models which could predict and forecast mean monthly upstream flow through delayed or lagged variables. Within the paradigm of Dynamic Neural Network (NN), it is obvious to follow a criterion where a system could select a Network from the different trained networks models and employ them in predictions and forecasting. The nonlinear autoregressive (NAR) based four different DNN models are inferred or extracted through Figures 4 to 11 with the optimized parameter of number of neurons in a hidden layer. By using the three measures of goodness of fit through models’ evaluation metrics Tables from 2 to 4 over training, validation, and testing sets, it is concluded that the values of the performance measures are sufficient to obtain the DNN model 3 as an appropriate autoregressive structure based neural network model for mean monthly upstream flow on upper Indus Basin at Tarbela. As a future research, extend the proposed approach with other computational intelligence techniques such as Fuzzy Logic (FL) or Differential Evolution (DE) based modeling to accomplish the optimal behavior and higher accuracy of the system.

8. ACKNOWLEDGEMENT
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9. REFERENCES
[1] Khan, B., Iqbal, M. J., and Yosufzai, M. A. Y. 2011 Flood risk assessment of river Indus of Pakistan, Arab J Geosci. 4, 115-122.