A New Robust Methodology of Image Compression based on CDF Wavelets

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ABSTRACT  
It is used specially for the compression of images where tolerable degradation is required. With the wide use of computers and consequently need for large scale storage and transmission of data, efficient ways of storing of data have become necessary. With the growth of technology and entrance into the Digital Age, the world has found itself amid a vast amount of information. Dealing with such enormous information can often present difficulties. Image compression is minimizing the size in bytes of a graphics file without degrading the quality of the image to an unacceptable level. The reduction in file size allows more images to be stored in a given amount of disk or memory space. It also reduces the time required for images to be sent over the Internet or downloaded from Web pages. JPEG and JPEG 2000 are two important techniques used for image compression.

Keywords  
Image, wavelets, transform, compression

1. INTRODUCTION  
An image may be defined as a two-dimensional function f(x, y), where x and y are spatial (plane) coordinates, and the amplitude of f at any pair of coordinates (x, y) is called the intensity or gray level of the image at that point. When x, y, and the amplitude values of f are all finite, discrete quantities, we call the image a digital image. The field of digital image processing refers to processing digital images by means of a digital computer. Note that a digital image is composed of a finite number of elements, each of which has a particular location and value. These elements are referred to as picture elements, image elements, pixels, and pixels. Pixel is the term most widely used to denote the elements of a digital image.

MATLAB  
MATLAB is software package that lets you do analyze data, mathematics and computation; develop algorithms, simulation and modeling, and produce graphical displays and graphical user interfaces. MATLAB is a powerful computing system for handling scientific and engineering calculations. The term MATLAB stands for Matrix Laboratory, because the System was designed to formulate matrix computations particularly easy [20].

Objectives:  
A new compression scheme will developed for images.

Objective of this work are:  
• The objective of image compression is to reduce the redundancy of the image and to store or transmit data in an efficient form.
• Analysis the wavelets family with discreet wavelets transformation  
• To Calculate MSE for proposed algorithms.

2. LITERATURE SURVEY  
a. Discrete Wavelet Transform:  
The Discrete Wavelet Transform, which is based on sub-band coding, is found to yield a fast computation of Wavelet Transform. It is easy to implement and reduces the computation time and resources required. The discrete wavelet transform uses filter banks for the construction of the multi resolution time-frequency plane. The Discrete Wavelet Transform analyzes the signal at different frequency bands with different resolutions by decomposing the signal into an approximation and detail information.

b. Inverse discrete wavelets transform:  
The IDWT block computes the inverse discrete wavelet transform (IDWT) of the input subbands. By default, the block accepts a single sample-based vector or matrix of concatenated subbands. The output is frame based, and has the same dimensions as the input. Each column of the output is the IDWT of the corresponding input column.

2.1 Literature Survey  
There are read flowing research papers related to work thesis work

M. Mozammel et al. [28] states a new image compression scheme based on discrete wavelet transform is proposed in this research which provides sufficient high compression ratios with no appreciable degradation of image quality. The effectiveness and robustness of this approach has been justified using a set of real images. The images are taken with a digital camera.

Somasundar Reddy et al. [29] proposed a theory based on Image compression which is of prime importance in Real time applications like video conferencing where data are transmitted through a channel. This method provides better results in terms of compression ratio, mean square error and peak signal to noise ratio. Proposing a simple and effective method combined with effective thresholding for further compression in this paper that saves a lot of bits in the image data transmission.

Fathima et al. [30] analyzed lossy compression of an RGB image by 2D Haar DWT and recovered it by inverse operation and provide acceptable recovery at a glance till 90% of zeros on each block. The algorithm is much simpler than JPEG or JPEG 2000 hence the technique is applicable in pattern recognition of complicated image like biometric (human face, fingerprint, retina or manual signature) identification where the process time is the main concern. The entire work can be extended using other wavelet matrix to make the comparison of performance even we can apply the algorithm for de-nosing operation of images.
3. IMPLEMENTATION AND RESULTS

3.1 Mean Square Error
The Mean Square Error (MSE) is the error metrics used to compare image compression quality. The MSE represents the cumulative squared error between the compressed and the original image, whereas PSNR represents a measure of the peak error. The lower the value of MSE, the lower the error. In the previous equation, \( M \) and \( N \) are the number of rows and columns in the input images, respectively.

\[
MSE = \frac{\sum_{i,j} (I_1(i,j) - I_2(i,j))^2}{MN}
\]

3.2 Compression Ratio
The compression ratio typically affects the picture quality. Generally, the higher the compression ratio, the poorer the quality of the resulting image. The trade-off between compression ratio and picture quality is an important one to consider when compressing images. Furthermore, some compression schemes produce compression ratios that are highly dependent on the image content. For example, a highly detailed image of a crowd at a football game may produce a very small compression ratio, whereas an image of a pure blue sky may produce a very high compression ratio.

3.3 Rate
A digital image can be represented by a two dimensional (2-D) array i.e., a matrix, each of whose element \( J_{(i,j)} \) corresponds to the value of the \((i,j)\)th pixel in the original image. If each pixel represents a shade of gray in monochrome images, we need to allocate only one byte or 8 bits per pixel (bpp). With \( 28 = 256 \) combinations, one can represent numbers ranging from 0 to 255[14].

In the imaging context, the pixel or block of pixel is considered as a set of symbol. A code, on the other hand, is sequence of symbols or number that are used to represent information. A string of codes is called a code word. The whole data compression process can now visualized as a mapping of all possible sequence of symbols of a message (of \( N_1 \) bits), separately or in a file, to a set of codes, separately or in file, using \( N_2 \) bits. The compression ratio \( Cr \) is then defined as \( N_1/N_2 \) and the relative redundancy \( Rd \) is defined as

\[
Rd = 1 - 1/Cr
\]

Now these scenarios emerge. In scenario one, \( N_2=N_1 \), this means that the compression ratio is 1 and relative redundant is 1-1/1=0. This indicates that there is no redundancy in the image. The input message is reproduced exactly.

3.4 Proposed algorithms:
- **Step 1:** Read the Gray Level Image /Color Image
- **Step 2:** Set transformation computation method
- **Step 3:** Apply the biorthogonal wavelet
- **Step 4:** Decide the iteration for biorthogonal wavelet
- **Step 5:** Compute iterated wavelets transformation using convolution method
- **Step 6:** Apply wavelets matrix method
- **Step 7:** Apply the fast convolution method using fft
- **Step 8:** Calculate execution time in second
- **Step 9:** Calculate the mean square Error (MSE)

3.5 Result
Using above proposed algorithms designed a tool in MATLAB and run on MATLAB command, with different test images which is shown in below figure.

![Test Image](image1.jpg)

**Figure 1: Test Image**

<table>
<thead>
<tr>
<th>Name</th>
<th>Size</th>
<th>Dimension</th>
</tr>
</thead>
<tbody>
<tr>
<td>Test1.bmp</td>
<td>301KB</td>
<td>640x480</td>
</tr>
<tr>
<td>Test2.bmp</td>
<td>257KB</td>
<td>512x512</td>
</tr>
<tr>
<td>Test3.bmp</td>
<td>768B</td>
<td>512x512</td>
</tr>
</tbody>
</table>

Table 1: Test Image Description

<table>
<thead>
<tr>
<th>Name</th>
<th>CR (in %)</th>
<th>Iteration</th>
<th>MSE</th>
</tr>
</thead>
<tbody>
<tr>
<td>Test1.bmp</td>
<td>85</td>
<td>2</td>
<td>0.000019515</td>
</tr>
<tr>
<td>Test1.bmp</td>
<td>90</td>
<td>2</td>
<td>0.00034015</td>
</tr>
<tr>
<td>Test1.bmp</td>
<td>95</td>
<td>2</td>
<td>0.0001161</td>
</tr>
<tr>
<td>Test1.bmp</td>
<td>99</td>
<td>2</td>
<td>0.15333</td>
</tr>
<tr>
<td>Test2.bmp</td>
<td>85</td>
<td>2</td>
<td>0.000015721</td>
</tr>
<tr>
<td>Test2.bmp</td>
<td>90</td>
<td>2</td>
<td>0.000026942</td>
</tr>
<tr>
<td>Test2.bmp</td>
<td>95</td>
<td>2</td>
<td>0.0019028</td>
</tr>
<tr>
<td>Test2.bmp</td>
<td>99</td>
<td>2</td>
<td>0.15636</td>
</tr>
<tr>
<td>Test3.bmp</td>
<td>85</td>
<td>2</td>
<td>0.00008218</td>
</tr>
<tr>
<td>Test3.bmp</td>
<td>90</td>
<td>2</td>
<td>0.00017704</td>
</tr>
<tr>
<td>Test3.bmp</td>
<td>95</td>
<td>2</td>
<td>0.0010384</td>
</tr>
<tr>
<td>Test3.bmp</td>
<td>99</td>
<td>2</td>
<td>0.0255847</td>
</tr>
</tbody>
</table>

Table 2: Result of CR and MSE

This algorithm was verified using several input images having different resolution. The images contained different size and dimension. With all such images, the algorithm correctly compressed the image. This algorithm was also tried computation time also. After successfully implementing and verifying the algorithm in MATLAB, values of MSE record. Here results of Compression ration and MSE with four input image are shown.
SnapShots of Result:

**Figure 3:** Compression with 85%

**Figure 6:** Compression with 90%

**Figure 4:** Compression with 85%

**Figure 7:** Compression with 90%

**Figure 5:** Compression with 85%

**Figure 8:** Compression with 90%
Figure 9: Compression with 95%

Figure 10: Compression with 95%

Figure 11: Compression with 95%

Figure 12: Compression with 99%

Figure 13: Compression with 99%

Figure 14: Compression with 99%
3.6 Analysis of other comparison method results:
C.SomasundarReddy et al. [29] clearly discusses about the performance evaluation of the proposed method in terms of MSE Table 3 shows how the result of method defined in [29].

<table>
<thead>
<tr>
<th>S.No</th>
<th>Thresholding</th>
<th>MSE (DWT)</th>
<th>MSE (CWT)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>10</td>
<td>0.0916</td>
<td>0.0023</td>
</tr>
<tr>
<td>2</td>
<td>20</td>
<td>0.1987</td>
<td>0.0923</td>
</tr>
<tr>
<td>3</td>
<td>30</td>
<td>0.9984</td>
<td>0.2345</td>
</tr>
<tr>
<td>4</td>
<td>40</td>
<td>1.0645</td>
<td>0.986</td>
</tr>
<tr>
<td>5</td>
<td>50</td>
<td>2.0013</td>
<td>1.464</td>
</tr>
<tr>
<td>6</td>
<td>60</td>
<td>3.2045</td>
<td>2.8001</td>
</tr>
<tr>
<td>7</td>
<td>70</td>
<td>5.6123</td>
<td>5.0062</td>
</tr>
<tr>
<td>8</td>
<td>80</td>
<td>7</td>
<td>6.21</td>
</tr>
<tr>
<td>9</td>
<td>90</td>
<td>8.1254</td>
<td>7.9345</td>
</tr>
<tr>
<td>10</td>
<td>100</td>
<td>10.0234</td>
<td>9.0123</td>
</tr>
</tbody>
</table>

Fahima Tabassum et al. [30] Evaluates the mean square error between the original and recovered image which is image dependent. We worked on more than 200 images of two types: some structure with background and human face. We found that human face provides less error. MSE Table 3.4 shows how the result of method defined in [30].

<table>
<thead>
<tr>
<th>Sno</th>
<th>Image</th>
<th>MSE</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>Test1</td>
<td>0.0620</td>
</tr>
<tr>
<td>2</td>
<td>Test2</td>
<td>0.1059</td>
</tr>
<tr>
<td>3</td>
<td>Test3</td>
<td>0.1429</td>
</tr>
<tr>
<td>4</td>
<td>Test4</td>
<td>0.1779</td>
</tr>
<tr>
<td>5</td>
<td>Test5</td>
<td>0.2120</td>
</tr>
<tr>
<td>6</td>
<td>Test6</td>
<td>0.2496</td>
</tr>
<tr>
<td>7</td>
<td>Test7</td>
<td>0.2831</td>
</tr>
<tr>
<td>8</td>
<td>Test8</td>
<td>0.3476</td>
</tr>
</tbody>
</table>

Result of proposed method is shown in Table 3.2. Now we can conclude from table 3.3 and table 3.4 value of MSE is lesser than the mention in table 3.3 and table 3.4. if you find a compression scheme having a lower MSE , you can recognize that it is a better one. MSE low means good quality and high means bad quality.

4. CONCLUSION
We have studied Cohen–Daubechies–Feauveau (CDF) wavelet with different iteration and compression ratio. Here value of MSE is depending upon the iteration and how much compression ratio is our milestone. In the parallel of MSE calculation record the execution time for better performance of algorithms. In this thesis we have made comparison of our results with two base paper each have different order of values of MSE. We have alread know that the mean square error value is zero for ideal image as decompressed image degraded from its orginal image MSE will be increase from zero. concluded that our proposed algorithms is better in context of compression ratio to the other algorithms studied. The second conclusion that we have arrived that value of MSE is minimum (order of 0.0000XX) in comparison to other algorithms that we have considered .This proposed algorithm can save storage space in some online applications where picture and signature are stored in the databases for future reference.

5. REFERENCES


[17] Osman G. Sezer, Oztan Harmanciy, Onur G. Guleryuzy “Sparse Orthogonal Transforms For Image Compression” Georgia Institute of Technology, Atlanta, GA, USA.


