# Digital Watermarking for Vector Drawings based on Discrete Haar Wavelet Transform

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# ABSTRACT

Recently, a massive amount of cartoons or "manga" comics are distributed in digital format. Although raster format is a current mainstream format, it will be likely to use vector format from the viewpoint of data capacity and image quality. In such a situation, copyright protection technology for vector format is strongly required. In this paper, we propose a novel digital watermarking scheme for vector drawings based on discrete Haar wavelet transform. By utilizing Haar wavelet transform, the proposed method has robustness against geometric transformations such as translation, rotation, and scaling. Experimental results show that the proposed method can successfully embed watermarks without causing significant degradation to the original drawings and it also has robustness against geometric transformations.

# Keywords

Digital watermarking, vector drawing, discrete Haar wavelet transform

# 1. INTRODUCTION

In recent years, the digital distribution of cartoons or manga comics has become more popular because of the development of electronic books and portable devices [1, 2]. On the other hand, many cartoons are plagued by the emergence of their pirated editions. Currently, most of such materials are distributed in raster formats such as JPEG or PNG. However, from the viewpoint of data capacity and image quality, the adoption of vector format is likely to become more popular. Vector drawings are substantially different from raster images in that they retain shapes like lines and points instead of a large set of pixels. Therefore, to protect the copyright, the need for a digital watermarking algorithm focused on vector drawings has recently been highlighted.

Some types of watermarking schemes for digital vector map have been proposed recently. In [3, 4], the watermarking schemes which embed watermarks into the spatial domain coefficients are proposed. There are other types of watermarking algorithms which embed watermarks in the frequency domain coefficients [5, 6]. Recently, the watermarking method for vector maps which utilize neural network is proposed in [7]. These schemes can successfully embed watermarks into vector maps. Although the algorithm proposed in [7] can tolerate geometric transformations to some extent, most of the previously proposed methods cannot resist geometric transformations, such as translation, rotation, and scaling. As for cartoons, several watermarking algorithms have been proposed in [8, 9, 10]. However, these schemes treat cartoons in raster format data. In [11], watermarks are embedded into the bezier curves which are derived from original raster format drawings. Within the scope of our survey, there is not a watermarking method which specializes in cartoons in vector format.

We have already proposed a scheme which can directly embed watermarks into vector format cartoons in [12] as an improvement version of Kaneshiro and Inaba's method[13]. These schemes are robust against isotropic scaling and translation since they are based on P–type Fourier descriptor[14] that is invariant against these transformations. However, there are some problems with the schemes. Namely, shapes are possible to deviate from the original by embedding, and the watermark capacity is not enough, and they are fragile against rotation.

In this paper, a new scheme of digital watermarking for vector drawings based on discrete Haar wavelet transform is proposed. The proposed method is supposed to suppress the changes of a whole shape of drawing and increase capacity and robustness against geometric transformations.

The rest of this paper is organized as follows. Discrete Haar wavelet transform for vector drawings is introduced in Section 2. In Section 3, the proposed watermarking algorithm is described in details. Experimental results and analysis are provided in Section 4. Finally, conclusions are drawn in Section 5.

# 2. HAAR WAVELET TRANSFORM FOR VECTOR DRAWINGS

# 2.1 The representation of vector drawings

In the proposed method, watermarks are embedded into vector drawings using discrete Haar wavelet transform (HWT). When applying HWT to vector drawings, it is assumed that the original curve consists of a set of N lines. Fig. 1 illustrates the approximation used in this scheme. C denotes the original curve,  $\delta$  is a length of each line. Each node of lines is presented by  $\mathbf{z_m}$ . By using this conversion, the approximation form of C is obtained as  $G = \{\mathbf{z_m} \mid m = 0, 1, \cdots, N-1\}$ . The parameter  $\delta$  determines the accuracy of G. As a result, more precise G is available with smaller  $\delta$ . However, a smaller  $\delta$  results in the increase in N and this leads to an increase in file size. So the value of  $\delta$  must be determined depending on the demand for the vector drawings. In the following discussion, we define  $\mathbf{z_m}$  as

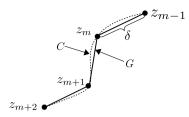


Fig. 1: Segmentation of a curve

$$\boldsymbol{z}_m = x_m \boldsymbol{i} + y_m \boldsymbol{j} \ (m = 0, 1, \cdots, N-1) \,. \tag{1}$$

where i = (1, 0), j = (0, 1).

# 2.2 Definition

HWT for the sequence of vector  $\boldsymbol{z}_m$  is defined as (2) and (3).

$$a_n = \frac{z_{2n} + z_{2n+1}}{2}$$
 (2)

$$r_n = \frac{z_{2n} - z_{2n+1}}{2},$$
 (3)

where  $n = 0, 1, \dots, N/2 - 1$ .  $a_n$  and  $r_n$  are called approximation coefficient vectors and detailed coefficient vectors respectively. Following equations show the inverse HWT for the two-dimensional vector sequence.

$$z_{2n} = a_n + r_n$$

$$z_{2n+1} = a_n - r_n.$$
(4)

The above equations reproduce the original vectors.

#### 2.3 Invariance for geometric transformations

In this section, the invariant characteristics of HWT coefficients will be shown. For each vector  $\mathbf{z}_m = (x_m, y_m)$  in G, apply to scale  $s_x, s_y$ , rotation around the origin  $\theta$  and translation  $t_x, t_y$ . The result vector  $\mathbf{z}'_m$  is represented in (6).

$$\boldsymbol{z}'_{m} = \begin{bmatrix} s_{x} \cos \theta & -s_{y} \sin \theta \\ s_{x} \sin \theta & s_{y} \cos \theta \end{bmatrix} \begin{bmatrix} x_{m} \\ y_{m} \end{bmatrix} + \begin{bmatrix} t_{x} \\ t_{y} \end{bmatrix}.$$
(6)

Applying HWT to  $z'_m$ , these coefficients are available.

$$\boldsymbol{a}_{n}^{\prime} = \frac{1}{2} \begin{bmatrix} s_{x} \cos \theta & -s_{y} \sin \theta \\ s_{x} \sin \theta & s_{y} \cos \theta \end{bmatrix} \\ \times \begin{bmatrix} x_{2n} + x_{2n+1} \\ y_{2n} + y_{2n+1} \end{bmatrix} + \begin{bmatrix} t_{x} \\ t_{y} \end{bmatrix}$$
(7)

$$\mathbf{r}'_{n} = \frac{1}{2} \begin{bmatrix} s_{x} \cos \theta & -s_{y} \sin \theta \\ s_{x} \sin \theta & s_{y} \cos \theta \end{bmatrix} \times \begin{bmatrix} x_{2n} - x_{2n+1} \\ y_{2n} - y_{2n+1} \end{bmatrix}.$$
(8)

In (8), there is no  $t_x$  and  $t_y$ , which means detailed coefficient vectors are invariant against translations.

Now we introduce the different value  $\alpha_n$  as follows.

$$\boldsymbol{\alpha}_{n} = \boldsymbol{a}_{n+1}^{\prime} - \boldsymbol{a}_{n}^{\prime}$$

$$= \frac{1}{2} \begin{bmatrix} \alpha_{n,x} s_{x} \cos \theta - \alpha_{n,y} s_{y} \sin \theta \\ \alpha_{n,x} s_{x} \sin \theta + \alpha_{n,y} s_{y} \cos \theta \end{bmatrix}.$$
(9)

$$\alpha_{n,x} = x_{2n+2} + x_{2n+3} - x_{2n} - x_{2n+1}. \tag{10}$$

$$\alpha_{n,y} = y_{2n+2} + y_{2n+3} - y_{2n} - y_{2n+1}. \tag{11}$$

Considering inner product  $\zeta_n = \alpha_n \cdot (-r'_n)$  and cross product  $\eta_n = \alpha_n \times (-r'_n)$ ,

$$\begin{aligned} \zeta_n &= \frac{1}{4} \alpha_{n,x} \left( x_{2n+1} - x_{2n} \right) s_x^2 \\ &+ \frac{1}{4} \alpha_{n,y} \left( y_{2n+1} - y_{2n} \right) s_y^2 \end{aligned} \tag{12} \\ \eta_n &= \frac{1}{4} \alpha_{n,y} \left( x_{2n} - x_{2n+1} \right) s_x s_y \end{aligned}$$

$$-\frac{1}{4}\alpha_{n,x}\left(y_{2n}-y_{2n+1}\right)s_{x}s_{y}.$$
 (13)

In (12) and (13),  $\theta$  is not included, so this means  $\zeta_n$  and  $\eta_n$  are invariant against rotation. However, each  $\zeta_n$  and  $\eta_n$  contain  $s_x$  and  $s_y$ , they are affected by scaling. Now let assume  $s_x = s_y = s$ . In this case,  $\zeta_n$ ,  $\eta_n$  are calculated as follows.

$$\zeta_{n} = \frac{1}{4} \alpha_{n,x} \left( x_{2n+1} - x_{2n} \right) s^{2} + \frac{1}{4} \alpha_{n,y} \left( y_{2n+1} - y_{2n} \right) s^{2}$$
(14)

$$\eta_n = \frac{1}{4} \alpha_{n,y} \left( x_{2n} - x_{2n+1} \right) s^2 - \frac{1}{4} \alpha_{n,x} \left( y_{2n} - y_{2n+1} \right) s^2.$$
(15)

Considering the ratio of  $\zeta_n$  and  $\eta_n$ .

$$\frac{\eta_n}{\zeta_n} = \frac{\alpha_{n,x} \left( x_{2n+1} - x_{2n} \right) + \alpha_{n,y} \left( y_{2n+1} - y_{2n} \right)}{\alpha_{n,x} \left( x_{2n} - x_{2n+1} \right) + \alpha_{n,y} \left( y_{2n} - y_{2n+1} \right)}.$$
 (16)

This does not contain s. Let  $\varphi_n \in (-\pi/2, \pi/2)$  be the angle between  $\alpha_n$  and  $-r'_n$ , following relation is derived.

$$\tau_n = \frac{\eta_n}{\zeta_n} = \frac{\sin \varphi_n}{\cos \varphi_n} = \tan \varphi_n.$$
(17)

(17) shows that  $\varphi_n$  is invariant against uniform isotropic scaling. As a result, it is clear that  $\varphi_n$  is invariant against translation, rotation, and uniform isotropic scaling.

# 3. PROPOSED METHOD

From the discussion in 2.3, it is proven that watermarks which are robust against geometric transformation can be embedded in G by controlling  $\varphi_n$ . To control  $\varphi_n$ , either  $\alpha_n$  or  $-r_n$  is a candidate for controlling. Because  $\alpha_n$  hold important information about the figure of curves, it is preferable to change  $r_n$  for watermark embeddings.

#### 3.1 Preliminaries

Define watermark data D as follows.

$$D = (d_k), \ d_k \in \{0, 1\}$$
(18)

where  $k=0,1,\cdots,N/2-2.$  For embedding and extracting watermark, quantizer  $Q_{\mu,\lambda}$  is used.

$$Q_{\mu,\lambda}(m) = \left\lfloor \operatorname{clamp}\left[\frac{m - (\mu - \lambda)}{2\lambda}\right] \times 7 \right\rfloor.$$
 (19)

where clamp is a function which is defined as follows.

$$\operatorname{clamp}(x) = \begin{cases} 1 & \text{if } x > 1 \\ 0 & \text{if } x < 0 \\ x & \text{otherwise.} \end{cases}$$
(20)

Inverse quantizer  $Q_{\mu,\lambda}^{-1}$  is also defined as

$$Q_{\mu,\lambda}^{-1}(t) = \mu - \lambda + \frac{t + 0.5}{7} \times 2\lambda.$$
 (21)

For embedding and extracting watermark, a random number sequence E is introduced. Each element of E is unsigned 8 bit integer and  $e_{k,b} \in \{0,1\}$  denotes *b*-th bit of  $e_k$ .

$$E = (e_k), \ e_k = \sum_{b=0}^{7} 2^b e_{k,b}.$$
 (22)

If watermark bit is d, embedding is executed by replacing b such as  $e_{k,b} = d$ . When extracting watermark, we can recover  $e_{k,b'}$  from quantized value b' where  $e_k$  must meet following condition.

$$\forall k \{ \exists b_0 [e_{k,b_0} = 0] \text{ and } \exists b_1 [e_{k,b_1} = 1] \}$$
(23)

# 3.2 Watermark Embedding

Watermarks are embedded by executing following procedures for  $k = 0, 1, \dots, N/2 - 2$ .

- (1)  $\alpha_k = a_{k+1} a_k$ .
- (2) calculate  $\tau_k$  using  $\alpha_k$ ,  $-r_k$ .

$$\tau_k \leftarrow \frac{\boldsymbol{\alpha}_k \times (-\boldsymbol{r}_k)}{\boldsymbol{\alpha}_k \cdot (-\boldsymbol{r}_k)}.$$
(24)

(3)  $t_k \leftarrow Q_{\mu,\lambda}(\tau_k)$ 

(4) For  $e_{k,c}$  and  $d_k$ , choose a minimum integer  $c \in \{0, 1, \dots, 7\}$  that satisfy  $e_{k,c} = d_k$  and (25) and  $c_k \leftarrow c$ .

$$f(c) = |c_{k-1} - c| + 2 |t_k - c|,$$
  
where  $c_{(-1)} = 3.$  (25)

(5)  $\dot{\tau}_k \leftarrow Q_{\mu,\lambda}^{-1}(c_k)$ 

(6) Generate vector  $\rho_k$  from  $\dot{\tau}_k$  and replace  $r_k$  by  $r'_k$ .

$$r'_k \leftarrow -\rho_k$$
 (26)

$$\boldsymbol{\rho}_{k} = \frac{\boldsymbol{\alpha}_{k}}{|\boldsymbol{\alpha}_{k}|} * \left\{ \frac{|\boldsymbol{r}_{k}|}{\sqrt{1 + \dot{\tau}_{k}^{2}}} \begin{bmatrix} 1\\ \dot{\tau}_{k} \end{bmatrix} \right\}.$$
 (27)

For vector  $\boldsymbol{u}$  and  $\boldsymbol{v}$ , an operator \* defined as follows.

$$\boldsymbol{u} * \boldsymbol{v} = (u_1 v_1 - u_2 v_2) \, \boldsymbol{i} + (u_1 v_2 + u_2 v_1) \, \boldsymbol{j}.$$
 (28)

where  $\boldsymbol{u} = u_1 \boldsymbol{i} + u_2 \boldsymbol{j}, \, \boldsymbol{v} = v_1 \boldsymbol{i} + v_2 \boldsymbol{j}.$ 

(7) calculate modified vector  $z_k$  using (4), (5).

The parameters of quantizer  $\mu$ ,  $\lambda$  are determined as  $\mu = \mu_{\tau}$  and  $\lambda = 3\sigma_{\tau}$ , where  $\mu_{\tau}$  is the average of  $\tau_k$  and  $\sigma_{\tau}$  is the standard deviation of  $\tau_k$ .

# 3.3 Watermarking Extraction

Embedded watermarks are extracted by following procedures for  $k = 0, 1, \cdots, N/2 - 2$ .

(1) 
$$\boldsymbol{\alpha}'_{k} = \boldsymbol{a}'_{k+1} - \boldsymbol{a}'_{k}.$$
  
(2) calculate  $\tau'_{k}$  using  $\boldsymbol{\alpha}'_{k}$  and  $-\boldsymbol{r}'_{k}$  by (24).  
(3)  $t'_{k} \leftarrow Q_{\mu,\lambda}(\tau'_{k}).$   
(4)  $d'_{k} \leftarrow e_{k,t'}.$ 

#### 4. COMPUTER SIMULATION

In this section, some experimental results of the proposed scheme for sample vector drawings are demonstrated. In the computer simulation, three SVG drawings shown in Fig. 2(0??) to 2(0??) are used. Specifications of each drawing are shown in Table 1. Computer simulations were performed for  $\delta = 0.01, 0.02, 0.05, 0.1, 0.2, 0.5, 1, 2, 5$ .

Table 1. : Specifications of each drawings

-	size (pixels)	paths
english	$541.621 \times 125.355$	1
hiragana	$561.825\times73.778$	15
girl	$338.029\times407.150$	64

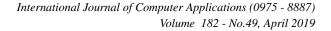


english





Fig. 2: Original SVG drawings



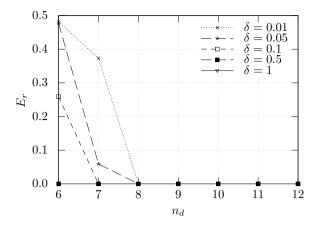


Fig. 3: The relation between  $n_d$  and  $E_r$  : english

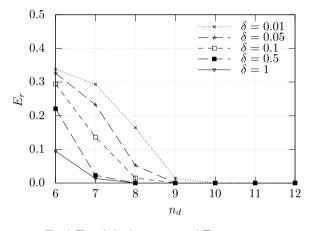


Fig. 4: The relation between  $n_d$  and  $E_r$ : hiragana

#### 4.1 Embedding Capacity

The relation between the number of nodes N in drawings and watermark embedding capacity  $C_{emb}$  [bits] is shown in Table 2. It is theoretically guaranteed that  $C_{emb} \leq N/2$  in the proposed method. From Table 2, it is obvious that  $C_{emb}$  approaches to N/2 when smaller  $\delta$  is used.

#### 4.2 Output Precision

In the proposed algorithm, modified values  $x'_m$ ,  $y'_m$  are recorded as SVG format. It is assumed that the floating point values  $x'_m$  and  $y'_m$  rounded to  $n_d$  digits after the decimal point are written to the output file. In this case,  $n_d$  affects the extraction error rate of watermarks. The extraction error rate  $E_r$  is defined as

$$E_r = \frac{\text{the total number of extracted erroneous watermarks}}{\text{the total number of extracted watermarks}}.$$
 (29)

The relations between the precision  $n_d$  and  $E_r$  for  $n_d = 6, 7, \dots, 12$  are investigated. Some of the results are shown in Fig. 3 to Fig. 5. From these results, it is clear that the less the value of  $\delta$  is, the larger  $n_d$  is needed. The required minimum values of  $\delta$  and  $n_d$  vary depending on the attribute of an original drawing.

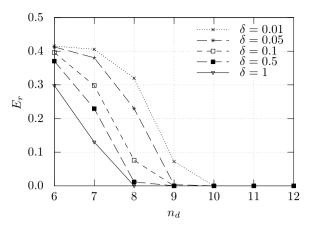


Fig. 5: The relation between  $n_d$  and  $E_r$  : girl

#### 4.3 The quality of embedded drawings

Some of the embedded drawings are shown in Fig. 6 to Fig. 8. As for the value  $n_d$ , the minimum value is adopted among those in which  $E_r = 0$ . For those parameters, no noticeable visual degradation can be observed. From the discussion in 2.1, smaller  $\delta$  is preferable for better image quality. However, smaller  $\delta$  causes an increase in the file size and  $n_d$ . Considering the above results,  $\delta = 1$  is an appropriate value in most cases.



Fig. 6: The quality of embedded drawing : english



Fig. 7: The quality of embedded drawing : hiragana

#### 4.4 Robustness against geometric transformations

The proposed method is robust to geometric transformations as discussed in 2.3. However, in real applications, the effect of  $n_d$  must be considered. As for the translation, it is evident that the proposed method is robust, so the simulations are performed only for rotation and uniform isotropic scaling. In Fig. 9,10, 11, the results for rotation  $\theta = \pi/2$  are shown. The results for uniform

δ		0.01	0.02	0.05	0.1	0.2	0.5	1	2	5
english	N	174973	87486	34991	17493	8744	3490	1739	860	338
	$C_{emb}$	87486	43742	17495	8746	4371	1744	869	429	168
hiragana	N	137145	68574	27433	13720	6865	2749	1377	690	281
	$C_{emb}$	68560	34275	13705	6850	3421	1363	676	333	129
girl	N	594780	297404	118978	59508	29765	11927	5976	3001	1209
	$C_{emb}$	294111	147042	58800	29380	14675	5852	2909	1438	548

Table 2. : The number of nodes and embedding capacity

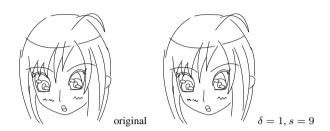


Fig. 8: The quality of embedded drawing : girl

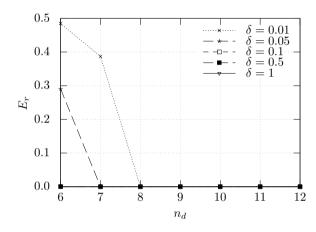


Fig. 9: Robustness against rotation : english

isotropic scaling are shown in Fig. 12, 13, 14. From these results, there are some differences in the value of  $E_r$ , the minimum  $n_d$  which give  $E_r = 0$  are the same values for non-transformed drawings and rotated or scaled versions. Therefore, no extra digits are needed to guarantee the proposed method being robust against geometric transformations.

# 5. CONCLUSION

In this paper, a novel watermark embedding method for vector drawings is proposed. The proposed method utilizes a Haar wavelet transform. By exploiting the nature of HWT, the proposed method is robust against geometric transformations such as translation, rotation, and uniform isotropic scaling. Experimental results show the embedding capacity, the excellent image quality of the proposed scheme, robustness against geometric transformations. Although some parameters have to be determined by experiments, our scheme has enough watermark capacity and can embed watermarks into vector drawings without significant degradation. Also, it is robust against geometric transformations by setting appropriate

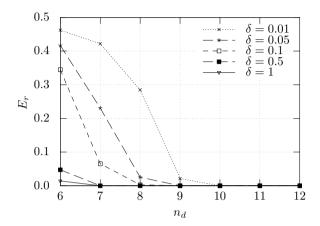


Fig. 10: Robustness against rotation : hiragana

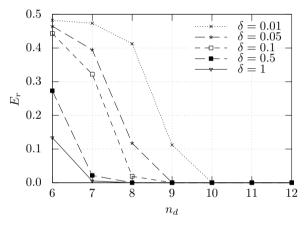


Fig. 11: Robustness against rotation : girl

parameters. Determining adequate parameters in our method is one of the future works.

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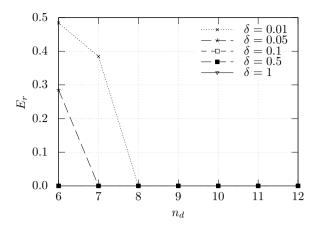


Fig. 12: Robustness against scaling : english

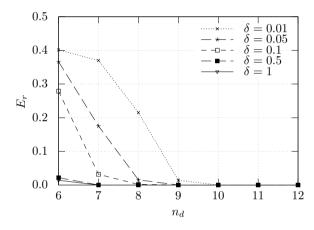


Fig. 13: Robustness against scaling : hiragana

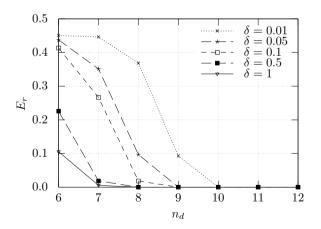


Fig. 14: Robustness against scaling : girl

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