# Satisfying Essential Normalization Properties of Neutrosophic Decomposed Relations

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## ABSTRACT

Neutrosophic database is an extension of classical database model with the framework of neutrosophic data and similarity measure formula to process uncertain data. Designing good neutrosophic database, normalization plays an important role in which a relation is decomposed into smaller relations with respect to neutrosophic functional dependencies to obtain desired neutrosophic normal forms. The objective of this paper is to investigate lossless join and dependency preservation properties of normalization in neutrosophic database. Two algorithms are designed to maintain lossless join and dependency preservation of decomposition of a relation in neutrosophic database. The algorithms have been tested and validated with examples.

### **Keywords**

Neutrosophic Data, Neutrosophic functional dependency, Neutrosophic Lossless Join and Dependency Preservation

## **1. INTRODUCTION**

In relational database model normalization technique plays an important role in designing good database. Normalization as introduced by Codd [1] is a technique by which authors can decompose a relation into minimum 3NF relations to reduce different anomalies. These decomposed 3NF and BCNF relation in traditional database always satisfy lossless join and dependency preservation properties of normalization. Present day since the communication is not restricted only in certain data so, fuzzy database model has been developed to process uncertain data. These database theories are also developed using fuzzy set [2] and vague set [3] while processing uncertain data. Authors have studied fuzzy and vague normalization to process lossless and dependency preservation in the literatures [4-10]. Researches in designing neutrosophic database which manages an inconsistent data related problem has started after the invention of new concept of neutrosophic set by Smarandache [11] in 2001. A few research have been reported in the literature [12-16] to defined neutrosophic functional dependency ( $\alpha$  -nfd), neutrosophic closure of attribute set, neutrosophic key and neutrosophic normal forms. No such work is reported on neutrosophic dependency preservation and lossless join decomposition into desire normal forms in neutrosophic database.

This paper is focused on these two important issues such as dependency preserving and lossless join decomposition to design a neutrosophic relational database. In this work authors have designed two algorithms that guarantee neutrosophic lossless join and dependency preservation properties while decomposing a relation into smaller relations to achieve desired neutrosophic normal form.

The paper is organized as follows: In section 2, all previous work which is useful to explain present work is revisited.

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Algorithms for testing neutrosophic lossless join and dependency preservations of decomposition into neutrosophic third normal form or Boyce Codd normal form have been presented with examples in **section 3**. The final conclusion of the paper is drawn in **section 4**.

# 2. BASIC DEFINITIONS Definition 1: Neutrosophic Set

Let  $U_1$  is the universe set and m is the one element of  $U_1$ .

N is a neutrosophic set on  $U_I$ , represented by the membership functions such as:

i) Membership of truthness function  $t_N : U_1 \rightarrow [0,1]$ ,

ii) Membership of falseness function  $f_N: U_1 \rightarrow [0,1]$ ,

iii) Membership of indeterminate function  $i_{i}: U_1 \rightarrow [0,1]$  with  $t_N(m) + f_N(m) \le 1$  and

 $t_N(m) + f_N(m) + i_N(m) \le 2$ , written as

 $N = \left\{ \left\langle m, \left[ t_N(m), i_N(m), f_N(m) \right] \right\rangle, m \in U_1 \right\}.$ 

# Definition 2: Similarity Measure between two neutrosophic data

Let two neutrosophic values of p and q represented as  $p = [t_p, i_p, f_p]$  and  $q = [t_q, i_q, f_q]$  where  $0 \le t_p \le 1$ ,  $0 \le i_p \le 1$ ,  $0 \le f_p \le 1$  and  $0 \le t_q \le 1$ ,  $0 \le i_q \le 1$ ,  $0 \le f_q \le 1$ with  $0 \le t_p + f_p \le 1$ ,  $0 \le t_q + f_q \le 1$ ,

 $0 \le t_p + i_p + f_p \le 2,$ 

 $0 \leq t_q + i_q + f_q \leq 2 \,.$ 

Now the similarity measure between two neutrosophic data denoted by SE(p,q) is defined as follows

$$SE(p,q) = \sqrt{1 - \frac{\left|(t_p - t_q) - (i_p - i_q) - (f_p - f_q)\right|}{3}} \left(1 - \left|(t_p - t_q) + (i_p - i_q) + (f_p - f_q)\right|\right)}$$

# **Definition 3:** Neutrosophic $\alpha$ -equality of $t_1[X]$ and $t_2[X]$

Consider r(R) be a neutrosophic relation with schema of R (A<sub>1</sub>, A<sub>2...</sub> A<sub>n</sub>). Let  $X_1 \subset R$  and  $t_1$ ,  $t_2$  are any two tuples in r. Then  $t_1$  and  $t_2$  are said to be  $\alpha$  -equal on  $X_1$  if  $SM(t_1[A_i], t_2[A_i]) \ge \alpha$  $\forall i = 1$  to k. This equality is represented as  $t_1[X_1](NE)_{\alpha} t_2[X_1]$ .

## **Definition 4: Neutrosophic Functional Dependency** ( $\alpha$ -nfd)

Let  $R(A_1, A_2, A_n)$  be a neutrosophic relation schema and  $X_1$ ,  $Y_1 \subset R$ . Now  $X_1$  neutrosophic functionally determines  $Y_1$  at the level of  $\alpha \in [0,1]$  is denoted by  $X_1 \xrightarrow{nfd} X_1$  and is defined as for any two tuples  $t_1$  and  $t_2$  if  $t_1[X_1](NE)_{\alpha} t_2[X_1]$  is true then  $t_1[Y_1](NE)_{\alpha} t_2[Y_1]$  is also true.

The above  $\alpha$  -nfd can also be read as, " $Y_1$  is neutrosophic functionally determined by  $X_1$  at  $\alpha$  level".

For  $\alpha$  -nfd the following propositions are straightforward.

The following proposition is straightforward from the above definition.

# **Proposition 1**

If  $0 \le \alpha_2 \le \alpha_1 \le 1$ , then

 $t_1[X](NE)_{\alpha_1}t_2[X] \Longrightarrow t_1[X](NE)_{\alpha_2}t_2[X]$ 

# **Proposition 2**

If 
$$0 \le \alpha_2 \le \alpha_1 \le 1$$
, then  $X_1 \xrightarrow{nfd} Y_1 \Longrightarrow X_1 \xrightarrow{nfd} Y_1 \Longrightarrow X_1$ 

## **Proposition 3** $\alpha$ -nfd union rule

If 
$$\{X_1 \xrightarrow{nfd} \alpha_1 \to A_1, \dots, X_1 \xrightarrow{nfd} \alpha_n \to A_n\}$$
 then  
 $X_1 \xrightarrow{nfd} A_1, \dots, A_n$ 

## 2.1. Neutrosophic closure of attribute set

Neutrosophic closure helps to obtain key of any relation in neutrosophic database. Following algorithms is used to find neutrosophic closure of any attribute set.

# Algorithm 1: Find the Neutrosophic Closure of any attribute set

Input:

Schema of neutrosophic relation i.e.  $R_1$ , a set of **nfds** N on  $R_1$  and attributes set  $X_1$ .

### Output:

Attributes set  $X_{I}^{+}$ , the closure neutrosophic set of  $X_{I}$ . Method:

Let  $X_1^+ = X_l$ .

i.e.,  $X_1^+ = (X_1, \alpha_1)$  where  $\alpha_1 = 1 [Q X_1 \xrightarrow{nfd} X_1]$ 

$$X_1^* = X_1^+$$
.

for each nfd  $Y_1 \xrightarrow{nfd} Z_1$  in N

do

if  $Y_1 \subseteq X_1^+$  then  $X_1^+ = (X_1^+ \cup Z_1, \alpha_3)$  where  $\alpha_3 = \min(\alpha_1, \alpha_3)$ 

 $lpha_2$  ). end for

until  $(X_1^* = X_1^+).$ 

### **2.3. Neutrosophic Key**

Neutrosophic key of neutrosophic relation  $R_1$  is defined as follows:

Let  $K_I$  a subset of attribute set of  $R_I$  and N be a set of nfds for  $R_I$ . Now  $K_I$  is a neutrosophic key of  $R_I$  at  $\alpha$  -level of choice with  $\alpha \in [0,1]$  if  $K_I$  is minimal subset of  $R_I$  and  $K_1 \xrightarrow{nfd} R_1$  holds in N.

## 2.4. Neutrosophic Normalization

Inconsistent data may lead to different database anomalies during database operation. For designing anomaly free information retrieval database, it must satisfy minimum third normal form. In this section the definition of different neutrosophic normal forms i.e., neutrosophic first (1NNF), neutrosophic second (2NNF), neutrosophic third (3NNF) and neutrosophic BCNF (NBCNF) normal forms is also revisited.

## **Definition 5: Neutrosophic First Normal** Form

Let  $D_i$  has the attributes domain  $A_i$ ,  $R_l$  is the schema of a relation which is called the first neutrosophic normal form (1NNF) for any relation  $r_l$  in  $R_l$ , no one attribute is multi-

valued and  $\, lpha \,$  -cut similarity based relation is in 1NNF.

### **Definition 6: Neutrosophic Second Normal** Form

Let *N* is the nfds set for the schema of  $R_1$  relation and *S* is a neutrosophic key at  $\alpha$  –level.  $R_1$  is called the second neutrosophic normal form (2NNF), for no one of attribute in nonprime manner is partly dependent on the neutrosophic key.

## **Definition 7: Neutrosophic Third Normal** Form

Let consider relation schema  $R_1$  with the nfds set and the neutrosophic key is *S* at  $\alpha$  –level.  $R_1$  is to be in third neutrosophic normal form(3NNF), only if  $R_1$  is in 2NNF and  $R_1$ should not contain any nonprime attribute with nfd, for any non-trivial nfd  $X \xrightarrow{\eta fd} \alpha A$  in *N* either *A* is neutrosophic – prime or the neutrosophic key is present in *X*.

## **Definition 8: Neutrosophic Boyce Codd** Normal Form

In relation  $R_1$  schema consists of neutrosophic key *S* and the set of nfds noted by *N* at the level of  $\alpha$  .  $R_1$  is BCNF neutrosophic normal form (NBCNF), only if  $R_1$  is in N3NF and for any nfd which is non-trivial  $X \xrightarrow{nfd} \alpha \rightarrow A$  in *N*, *X* is a neutrosophic key of  $R_1$  means  $X \supseteq S$ .

# 3. NEUTROSOPHIC LOSSLESS JOIN AND DEPENDENCY PRESERVATION PROPERTIES TESTING

Normalization is a process in which a relation is decomposed into smaller relations. For good database designing, any decomposition always satisfies lossless join and dependency preservation properties. Lossless join means there should not be any loss of information between the original relation and the relation obtaining after joining of decomposed relations. Dependency preservation means all the dependencies in the original relation must be incurred from the closure of nfd set obtained after taking union of nfd sets of the decomposed relations. Objective of the present work is to design neutrosophic database model in such a manner that during decomposition of a relation it also satisfies both neutrosophic lossless join and dependency preservation properties. Authors also explained two algorithms which achieve these properties while decomposing a relation of neutrosophic database into desire normal forms with respect to a given neutrosophic functional dependency (nfd) set. The first step of algorithm is to find canonical cover of the given nfd set. Steps for obtaining canonical cover of any neutrosophic functional dependency set is stated below.

# **3.1.** Steps to obtain canonical cover of a given neutrosophic functional dependency set

Canonical cover of a given neutrosophic functional dependency set means to eliminate all extraneous attributes and redundant nfd from the neutrosophic functional dependency set.

Let F be the given set of nfds. Initially assign F to G i.e., G := F

# 1<sup>st</sup> step: Make the right hand side atomic

Replacing each nfd  $X \xrightarrow{nfd} \{A_1, A_2, ..., A_n\}$  in G by n nfds as stated below

 $X \xrightarrow{nfd} A_1, X \xrightarrow{nfd} A_2, X \xrightarrow{nfd} A_n.$ 

# 2<sup>nd</sup> step: Remove extraneous attribute from left hand side

For any nfd  $X \xrightarrow{nfd} A_k$  in *G* if we get an attribute  $B \in X$ such that  $(X - \{B\}) \xrightarrow{nfd} A_k$  where  $\alpha_2 = \alpha_1$  the nfd  $X \xrightarrow{nfd} A_k$  contains extraneous attribute and is replaced by  $(X - \{B\}) \xrightarrow{nfd} A_k$  in *G*.

# 3<sup>rd</sup> step: Removal of redundant nfd

An **nfd**  $X \xrightarrow{nfd} A_k$  in *G* is redundant if {  $(G - \{X \xrightarrow{nfd} a_1 \to A_k\})$  is equivalent to *G*. Redundant nfd must be eliminated from *G*.

**Example 3.1:** Let  $R = (A_2, B_2, C_2, D_2, E_2)$  and a set of **nfds**   $NF = \{C_2D_2 \xrightarrow{nfd} 0.7 \rightarrow A_2B_2E_2, A_2D_2 \xrightarrow{nfd} 0.7 \rightarrow E_2, A_2 \xrightarrow{nfd} 0.8 \rightarrow B_2, B_2 \xrightarrow{nfd} 0.9 \rightarrow E_2\}$ Find minimal cover of NF.

### Solution:

Minimal cover **algorithm 3.1** is applied to get the minimal cover of *NF*. G is initialized to the set of **nfds** *NF* i.e.,  $G = \{C_2D_2, -\frac{\eta(d)}{D_2} \rightarrow A_2, B_2, A_2, D_2, -\frac{\eta(d)}{D_2} \rightarrow B_2, B_2, -\frac{\eta(d)}{D_2} \rightarrow E_2\}$ .

**Step1:** Make right hand side atomic  $G = \{C_2 D_2 - \frac{n/d}{07} \rightarrow A_2, C_2 D_2 - \frac{n/d}{07} \rightarrow B_2, C_2 D_2 - \frac{n/d}{07} \rightarrow E_2, A_2 D_2 - \frac{n/d}{03} \rightarrow E_2, A_2 - \frac{n/d}{08} \rightarrow B_2, B_2 - \frac{n/d}{09} \rightarrow E_2\}$ 

#### Step2: Remove any redundant left hand side attribute

From	$A_2$ -	nfd	$\rightarrow B_2$	and	$B_{2}$ –	$\xrightarrow{nfd} 0.9$	$E_2$ ,	using	α-	nfd-
transi	tive	rule,	we	get	$A_2$ -	$\xrightarrow{nfd}{0.8}$	$E_2$	which	imj	plies
$A_{2}$ —	$\xrightarrow{nfd} \rightarrow 0.7$	$E_2$	using	3	Propo	osition	2.	Hei	nce	in
$A_2D_2$		$\xrightarrow{l} E_2$	, D	is	а	redund	lant	attribu	ute.	So

$$A_2 D_2 \xrightarrow{-nfd} E_2 \text{ is replaced by } A_2 \xrightarrow{-nfd} 0.7 E_2 \text{ in G.}$$
$$\therefore G = \{C_2 D_2 \xrightarrow{-nfd} 0.7 A_2, C_2 D_2 \xrightarrow{-nfd} 0.7 E_2, C_2 D_2 \xrightarrow{-nfd} 0.7 E_2, A_2 \xrightarrow{-nfd} 0.7 E_2, A_2 \xrightarrow{-nfd} 0.7 E_2, A_2 \xrightarrow{-nfd} 0.7 E_2\}$$

Step3: Remove any redundant nfd

The **ffd**  $A_2 \xrightarrow{\eta fd} E_2$  is now redundant in G, since  $A_2 \xrightarrow{\eta fd} E_2$  is obtained from  $A_2 \xrightarrow{\eta fd} B_2$  and  $B_2 \xrightarrow{\eta fd} E_2$  of G by using  $\alpha$  -**ffd-transitive rule** and **Proposition 2.** So  $A_2 \xrightarrow{\eta fd} E_2$  is removed from G.

 $\therefore G = \{C_2 D_2 \xrightarrow{n / d} 0.7 \rightarrow A_2, C_2 D_2 \xrightarrow{n / d} 0.7 \rightarrow B_2, C_2 D_2 \xrightarrow{n / d} 0.7 \rightarrow E_2, A_2 \xrightarrow{n / d} 0.8 \rightarrow B_2, B_2 \xrightarrow{n / d} 0.9 \rightarrow E_2\}$  is the minimal cover of *NF*.

# **3.2. Dependency Preservation with Lossless Decompose into Third Neutrosophic Normal Form**

Following algorithm is designed to decompose a relation into neutrosophic third normal form satisfying both dependency preservation and lossless join properties.

# Algorithm 1: Decomposition into 3NNF satisfying dependency preservation and lossless join properties

**Input:** A neutrosophic relation schema  $R_n(A_1, ..., A_n)$  satisfying a set of neutrosophic functional dependencies  $F_n$ .

### Procedure:

1. Find the canonical cover  $(M_c)$  of nfd set  $F_n$ 

2. Create a new relation schema considering all attributes that are not included in any nfd of  $M_c$  and exclude them from  $R_n$ 

3. Convert all nfd in  $M_c$  with same LHS into a single nfd using **Proposition 3** i.e., if  $\{X_1 \xrightarrow{nfd} \alpha_1 \rightarrow NA_1, \dots, X_1 \xrightarrow{nfd} \alpha_n \rightarrow NA_n\}$  exists in  $M_c$  convert these into  $X_1 \xrightarrow{nfd} \dots MA_1, \dots, NA_n$ 

4. For every nfd  $X_1 \xrightarrow{nfd} NA_1, \dots, NA_n$  in  $M_c$ , create a new schema  $R_s$  with attributes  $\{X_1 \cup NA_1, \dots, \cup NA_n\}$  which guarantee neutrosophic dependency preservation properties

5. If decomposed relations do not acquire the neutrosophic key of  $R_n$ , then create another relation containing all attributes of neutrosophic key of  $R_n$ . This will guarantee the property of neutrosophic lossless join.

**Output:**  $R_n$  is decomposed into  $R_{nl}, R_{n2,...,}, R_{nk}$  be satisfying nfds  $NF_l$ ,  $NF_2, ..., NF_k$  respectively, such that  $M_c = \{NF_1 \cup NF_2 \cup ..., \cup NF_k\}$  and

$$R_n = R_{n1} > < R_{n2} > < \dots > < R_{nk}$$

### **Example 1**

Consider neutrosophic relation  $R_d = (A_2, B_2, C_2, D_2, E_2)$  with set of nfds

$$NF = \{C_2 D_2 \xrightarrow{-nfd}_{0.7} \rightarrow A_2 B_2 E_2, A_2 D_2 \xrightarrow{-nfd}_{0.7} \rightarrow E_2, A_2 \xrightarrow{-nfd}_{0.8} \rightarrow B_2, B_2 \xrightarrow{-nfd}_{0.9} \rightarrow E_2\}$$

**Solution:** neutrosophic key of  $R_d$  is  $C_2D_2$  at  $\alpha = 0.7$  level of tolerance.

**1<sup>st</sup> step:** Find out  $M_c$  for NF. Here minimal cover is

$$\therefore M_C = \{C_2 D_2 - \frac{n / d}{0.7} \rightarrow A_2, C_2 D_2 - \frac{n / d}{0.7} \rightarrow B_2, C_2 D_2 - \frac{n / d}{0.7} \rightarrow E_2, A_2 - \frac{n / d}{0.8} \rightarrow B_2, B_2 - \frac{n / d}{0.9} \rightarrow E_2\}$$

as calculated in the section **3.1**.

**2^{nd} step:** all attributes of  $R_d$  are incorporated in the nfds of the minimal cover.

3<sup>rd</sup> step: Using  $\alpha$  -nfd union based rule,

Once again  $M_c$  can be written as  $M_c = \{C_2 D_2 \xrightarrow{nfd} 0.7 \rightarrow A_2 B_2 E_2, A_2 \xrightarrow{nfd} 0.8 \rightarrow B_2, B_2 \xrightarrow{nfd} 0.9 \rightarrow E_2\}$ 

**4<sup>th</sup> step:** For nfd  $C_2D_2 \xrightarrow{\eta fd} A_2B_2E_2$  in  $M_c$ , we get  $R_{11} = (C_2, D_2, A_2, B_2, E_2)$  with nfds  $NF_1 = \{C_2D_2 \xrightarrow{\eta fd} 0.7 \rightarrow A_2B_2E_2\}$  and neutrosophic key is  $C_2D_2$  at 0.7 level.

Similarly, for  $A_2 \xrightarrow{nfd} B_2$ , we get  $R_{12} = (A_2, B_2)$  with nfds  $NF_2 = \{A_2 \xrightarrow{nfd} B_2\}$  and neutrosophic key is  $A_2$  at 0.8-level.

For  $B_2 \xrightarrow{nfd} 0.9 \rightarrow E_2$ , we get  $R_{13} = (B_2, E_2)$  with nfds  $NF_3 = \{B_2 \xrightarrow{nfd} 0.9 \rightarrow E_2\}$  and neutrosophic key is  $B_2$  at 0.9-level. Here we guaranteed the dependency preservation, is represented as  $M_c = NF_1 \cup \dots \cup NF_3$ .

5<sup>th</sup> step: It has been confirmed the lossless join, is denoted by  $R_d = R_{11} > < R_{12} > < R_{13}$ .

After decompose  $R_d$  into 3NNF with the fulfillment of dependency and join in lossless way, we got three new relations  $R_{11} = (C_2, D_2, A_2, B_2, E_2)$ ,  $R_{12} = (A_2, B_2)$  and  $R_{13} = (B_2, E_2)$ 

**3.3. Lossless join decomposition into NBCNF** Here we have designed an algorithm which decomposes a relation into neutrosophic Boyce Codd normal form (NBCNF) satisfying lossless join properties.

# Algorithm 2: Decomposition into NBCNF satisfying lossless join properties

**Input:**  $R_1(A_1, A_2,...,A_n)$  is a relation schema and a set of nfds N of  $R_1$ .

### **Procedure:**

1. Set  $\rho_1 \coloneqq \{R_1\}$ 

2. For any relation schema  $R_1$  in  $\rho$  which is not in NBCNF **do** 

{

Find neutrosophic functional dependency  $X_1 \xrightarrow{nfd} Y_1$  in  $R_1$  that violates the rules of NBCNF.

Decompose  $R_1$  into  $R_{11}$  and  $R_{12}$ .

 $R_{11}$  contain attributes  $X_1 \cup Y_1$  and  $R_{12}$  all attributes of  $R_1$  except the attributes in  $Y_1$ .

i.e.,  $R_{11} = \{X_1 \cup Y_1\}, R_{12} = \{R_1 - Y_1\}$ .

} until all decomposed relations are in NBCNF

**Output**: A set of decomposed neutrosophic Boyce Codd normal form (NBCNF) relations  $R_1, R_2, ..., R_k$  satisfying lossless join property i.e.,  $R_1 = R_{11} > < R_{12} > < ... < R_{1k}$ 

### Example 2

Person = {Pfname, Pstate, Psstatus, Pincome, Pexp} relation and nfd set

 $N_{d} = \{Pstate \xrightarrow{nfd}_{0.99} \rightarrow Psstatus, P \exp \xrightarrow{nfd}_{0.9} \rightarrow Pincome, PfnamePstate \xrightarrow{nfd}_{1} \rightarrow P \exp \}$ 

Find a decompose join in lossless way of Person relation into NBCNF.

#### Solution:

Neutrosophic key of *Person* is (*Pfname, Pstate*) at 0.9-level as per neutrosophic closure property.

**Step1:**  $\rho := \{Person(Pfname, Pstate, Psstatus, Pincome, Pexp)\}$  **Step2:** Here *Person* relation is not in NBCNF, since in the nfd *Pstate*  $\xrightarrow{nfd}_{0.99}$  *Psstatus*, *Pstate* is not a neutrosophic key. Therefore, *Person* relation is decomposed as:

 $P_1(Pstate, Psstatus);$   $P_1 = \{Pstate \xrightarrow{nfd} 0.99 \rightarrow Psstatus\};$ neutrosophic key is *Pstate* at 0.99-level and

$$\begin{split} P_2(Pfname, Pstate, Pexp, Pincome); \\ P_2 &= \{P \exp - \frac{\eta dd}{0.9} \rightarrow Pincome, PfnamePstate - \frac{\eta dd}{1} \rightarrow P \exp\}; \\ \text{neutrosophic key} (Pfname, Pstate) \text{ at } 0.9\text{-level.} \end{split}$$

Here  $P_1$  is in NBCNF, but  $P_2$  is not in NBCNF since  $P \exp - \frac{nfd}{0.9} \rightarrow Pincome$  not satisfy the rules. Now, further decompose is required for  $P_2$  as follows:

 $P_A(Pexp, Pincome);$   $P_A = \{Pexp \xrightarrow{n/d} 0.9 \} Pincome\};$ neutrosophic key is Pexp at 0.9-level and

 $P_{B}(Pname, Pcity, Pexp);$   $P_{B} = \{PfnamePstate \xrightarrow{nfd}{1} Pexp\};$ neutrosophic key is (*Pfname, Pstate*) at 1-level.

Here both  $P_A$  and  $P_B$  are satisfying NBCNF.

Finally by applying algorithm 2, the *Person* relation is decomposed into three NBCNF relations as given below:

$$\begin{split} P_{I}(Pstate, Psstatus) \text{ with nfd } P_{I} &= \{Pstate \xrightarrow{nfd} 0.99 \rightarrow Psstatus\} \\ P_{A}(Pexp, Pincome) \text{ with nfd} \\ P_{A} &= \{P \exp \xrightarrow{nfd} 0.9 \rightarrow Pincome\} \\ P_{B}(Pfname, Pstate, Pexp) \text{ with nfd} \\ P_{B} &= \{PfnamePstate \xrightarrow{nfd} 1 \rightarrow P \exp\} . \end{split}$$

Also we get,  $Person = \{P_1 > < P_A > < P_B\}$  which satisfies lossless property.

### **4. CONCLUSION**

Neutrosophic database processing imprecise data may face problem of different anomalies and data redundancy like as classical relational data model if the design part is not proper. Normalization of neutrosophic representation with  $\alpha$  -nfd acts as an important role in designing good neutrosophic database. Normalization always decomposes a relation into smaller relations to achieve desire neutrosophic normal forms. After decomposing a relation into smaller relations confirmation of the dependency preservation and lossless join properties must be validated. In this paper authors have focused on these two properties and have developed two algorithms that guarantee that the dependency preservation and lossless join properties are achieved during decomposition.

### **Conflicts of interest**

The authors have no conflicts of interest to declare.

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