

Performance Comparison of Texture Pattern based Image Retrieval using Haar Transform with Binary and Ternary Image Maps

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ABSTRACT

The theme of the work presented here is performance comparison of texture pattern based image retrieval techniques using Haar transform with binary image maps and ternary image maps. Different texture patterns namely '4-pattern', '16-pattern', '64-pattern', '256-pattern' and '1024-pattern' are generated using Haar transform matrix and then compared with the two image maps binary and ternary (one a time) to generate the feature vector as the matching number of ones & minus ones (in case of binary image maps) and ones, zeros and minus ones (in case of ternary image maps) per texture pattern. The proposed content based image retrieval (CBIR) techniques are tested on a generic image database having 1000 images spread across 11 categories. For each proposed CBIR technique 55 queries (randomly selected 5 per category) are fired on the image database. To compare the performance of image retrieval techniques, crossover point of average precision and recall values of all the queries are computed per image retrieval technique. Ameliorated performance (higher precision and recall values) has been observed with the ternary image maps. Further the performance of proposed image retrieval methods is enhanced using the combination of original image and even image part. In the discussed image retrieval methods, the combination of original and even image part for 16-pattern texture with ternary image maps gives the highest crossover point of precision and recall reflecting better performance.

Categories and Subject Descriptors

- 1.4 Image Processing and Computer Vision
- 1.4.2 Compression (Coding):- Approximate methods
- H.3.3 [Information Search and Retrieval]

General Terms

Algorithms, Performance

Keywords

CBIR, Haar transform, Texture, Pattern, Binary, Ternary, Image maps

1. INTRODUCTION

One of the major challenges being faced by the technicians in various disciplines of ICT is to store, transmit, index and manage image data effectively to make easy access to the image databases of humongous size being generated due to large numbers of

images generated from diverse sources like digital camera, digital video, scanner, the internet etc. The storage and transmission is taken care of by image compression [4,7,8]. The image indexing is studied in the perspective of image database [5,9,10,13,14] as one of the promising and important research area for researchers from disciplines like computer vision, image processing and database areas. The thirst for better and quicker image retrieval techniques is increasing day by day. The significant applications for CBIR technology could be listed as art galleries [15,17], museums, archaeology [6], architecture design [11,16], geographic information systems [8], weather forecast [8,25], medical imaging [8,21], trademark databases [24,26], criminal investigations [27,28], image search on the Internet [12,22,23]. The paper attempts to provide better and faster image retrieval techniques.

1.1 Content Based Image Retrieval

For the first time Kato et.al. [7] described the experiments of automatic retrieval of images from a database by colour and shape feature using the terminology content based image retrieval (CBIR). The typical CBIR system performs two major tasks [19,20] as feature extraction (FE), where a set of features called feature vector is generated to accurately represent the content of each image in the database and similarity measurement (SM), where a distance between the query image and each image in the database using their feature vectors is used to retrieve the top "closest" images [19,20,29].

For feature extraction in CBIR there are mainly two approaches [8] feature extraction in spatial domain and feature extraction in transform domain. The feature extraction in spatial domain includes the CBIR techniques based on histograms [8], BTC [4,5,19], VQ [24,28,29]. The transform domain methods are widely used in image compression, as they give high energy compaction in transformed image [20,27]. So it is obvious to use images in transformed domain for feature extraction in CBIR [26]. But taking transform of image is time consuming. Reducing the size of feature vector using pure image pixel data in spatial domain and getting the improvement in performance of image retrieval is shown in [1,2,3]. But the problem of feature vector size still being dependent on image size persists in [1,2,3]. Here the query execution time is further reduced by decreasing the feature vector size further and making it independent of image size. Many current CBIR systems use the Euclidean distance [4-

6,11-17] on the extracted feature set as a similarity measure. The direct Euclidian Distance between image P and query image Q can be given as equation 1, where V_{pi} and V_{qi} are the feature vectors of image P and Query image Q respectively with size 'n'.

$$ED = \sqrt{\sum_{i=1}^n (V_{pi} - V_{qi})^2} \quad (1)$$

2. HAAR TRANSFORM

This sequence was proposed in 1909 by Alfréd Haar [21]. Haar used these functions to give an example of a countable orthonormal system for the space of square-integrable functions on the real line [9,22]. For full 2-Dimensional Haar Transform for an NxN image the number of additions required are 2N²log₂(N) and no multiplications needed. The Haar transform can be generated using the function ψ(t) can be described as:

$$\psi(t) = \begin{cases} 1, & 0 \leq t < \frac{1}{2} \\ -1, & \frac{1}{2} \leq t < 1 \\ 0, & \text{otherwise} \end{cases} \quad (2)$$

and its scaling function φ(t) can be described as:

$$\varphi(t) = \begin{cases} 1, & 0 \leq t < 1 \\ 0, & \text{otherwise} \end{cases} \quad (3)$$

Using the Haar transform matrix assorted texture patterns namely 4-pattern, 16-pattern, 64-pattern, 256-pattern and 1024-pattern are generated. To generate N² texture patterns, each row of the Haar matrix of size NxN is multiplied with every element of all possible rows of the same matrix (one row at a time to get one pattern). The texture patterns obtained are orthogonal in nature.

$$\begin{bmatrix} 1 & 1 \\ 1 & -1 \end{bmatrix}$$

1(a). 2x2 Haar transform matrix

$$\begin{matrix} 1 & \begin{bmatrix} 1 & 1 \\ 1 & 1 \end{bmatrix} & \begin{bmatrix} 1 & 1 \\ -1 & -1 \end{bmatrix} & 1 \\ 1 & \begin{bmatrix} 1 & 1 \\ 1 & 1 \end{bmatrix} & \begin{bmatrix} 1 & 1 \\ -1 & -1 \end{bmatrix} & -1 \\ 1 & \begin{bmatrix} 1 & -1 \\ 1 & -1 \end{bmatrix} & \begin{bmatrix} 1 & 1 \\ -1 & 1 \end{bmatrix} & 1 \\ 1 & \begin{bmatrix} 1 & -1 \\ 1 & -1 \end{bmatrix} & \begin{bmatrix} 1 & 1 \\ -1 & 1 \end{bmatrix} & -1 \end{matrix}$$

1(b). '4-pattern' texture patterns

Figure 1. Generation of '4-pattern' Haar texture patterns

$$\begin{bmatrix} 1 & 1 & 1 & 1 \\ 1 & 1 & -1 & -1 \\ 1 & -1 & 0 & 0 \\ 0 & 0 & 1 & -1 \end{bmatrix}$$

2(a). 4x4 Haar transform matrix

$$\begin{matrix} 1 & \begin{bmatrix} 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 \end{bmatrix} & \begin{bmatrix} 1 & -1 & 0 & 0 \\ 1 & -1 & 0 & 0 \\ 1 & -1 & 0 & 0 \\ 1 & -1 & 0 & 0 \end{bmatrix} & 1 \\ 1 & \begin{bmatrix} 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 \end{bmatrix} & \begin{bmatrix} 1 & -1 & 0 & 0 \\ 1 & -1 & 0 & 0 \\ 1 & -1 & 0 & 0 \\ 1 & -1 & 0 & 0 \end{bmatrix} & 1 \\ 1 & \begin{bmatrix} 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 \end{bmatrix} & \begin{bmatrix} 1 & -1 & 0 & 0 \\ 1 & -1 & 0 & 0 \\ 1 & -1 & 0 & 0 \\ 1 & -1 & 0 & 0 \end{bmatrix} & 1 \\ 1 & \begin{bmatrix} 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 \end{bmatrix} & \begin{bmatrix} 1 & -1 & 0 & 0 \\ 1 & -1 & 0 & 0 \\ 1 & -1 & 0 & 0 \\ 1 & -1 & 0 & 0 \end{bmatrix} & 1 \\ 1 & \begin{bmatrix} 1 & 1 & -1 & -1 \\ 1 & 1 & -1 & -1 \\ 1 & 1 & -1 & -1 \\ 1 & 1 & -1 & -1 \end{bmatrix} & \begin{bmatrix} 0 & 0 & 1 & -1 \\ 0 & 0 & 1 & -1 \\ 0 & 0 & 1 & -1 \\ 0 & 0 & 1 & -1 \end{bmatrix} & 1 \\ 1 & \begin{bmatrix} 1 & 1 & -1 & -1 \\ 1 & 1 & -1 & -1 \\ 1 & 1 & -1 & -1 \\ 1 & 1 & -1 & -1 \end{bmatrix} & \begin{bmatrix} 0 & 0 & 1 & -1 \\ 0 & 0 & 1 & -1 \\ 0 & 0 & 1 & -1 \\ 0 & 0 & 1 & -1 \end{bmatrix} & 1 \\ 1 & \begin{bmatrix} 1 & 1 & -1 & -1 \\ 1 & 1 & -1 & -1 \\ 1 & 1 & -1 & -1 \\ 1 & 1 & -1 & -1 \end{bmatrix} & \begin{bmatrix} 0 & 0 & 1 & -1 \\ 0 & 0 & 1 & -1 \\ 0 & 0 & 1 & -1 \\ 0 & 0 & 1 & -1 \end{bmatrix} & 1 \end{matrix}$$

2(b). First four of the '16-pattern' texture patterns

Figure 2. First four of the '16-pattern' Haar texture patterns

Figure 1(a) shows a 2X2 Haar transform matrix. The four texture patterns generated using this matrix are shown in figure 1(b). Similarly figure 2(b) shows first four texture patterns (out of total 16) generated using 4X4 Haar transform matrix shown in figure 2(a).

3. GENERATION OF IMAGE MAPS

Image bitmaps of colour image are generated using three independent red (R), green (G) and blue (B) components of image to calculate three different thresholds and one overall luminance threshold. Let $X = \{R(i,j), G(i,j), B(i,j)\}$ where $i=1,2,\dots,m$ and $j=1,2,\dots,n$; be an $m \times n$ color image in RGB space. Let the individual colour thresholds be TR, TG and TB, which could be computed as per the equations 4, 5 & 6. Let the luminance threshold T be as given by equation 7

$$TR = \frac{1}{m * n} \sum_{i=1}^m \sum_{j=1}^n R(i, j) \quad (4)$$

$$TG = \frac{1}{m * n} \sum_{i=1}^m \sum_{j=1}^n G(i, j) \quad (5)$$

$$TB = \frac{1}{m * n} \sum_{i=1}^m \sum_{j=1}^n B(i, j) \quad (6)$$

$$T = \frac{TR + TG + TB}{3} \quad (7)$$

3.1 Binary Image Maps

Here three bitmaps will be computed as BMr, BMg and BMb. If a pixel in each component (R, G, and B) is greater than or equal to the respective threshold, the corresponding pixel position of the bitmap will have a value of 1 otherwise it will have a value of -1.

$$BMr(i, j) = \begin{cases} 1, & \text{if } .R(i, j) \geq TR \\ -1, & \text{if } .R(i, j) < TR \end{cases} \quad (8)$$

$$BMg(i, j) = \begin{cases} 1, & \text{if } .G(i, j) \geq TG \\ -1, & \text{if } .G(i, j) < TG \end{cases} \quad (9)$$

$$BMb(i, j) = \begin{cases} 1, & \text{if } .B(i, j) \geq TB \\ -1, & \text{if } .B(i, j) < TB \end{cases} \quad (10)$$

3.2 Ternary Image Maps

Here first for each component (R, G, and B), the individual colour threshold intervals (lower-Tshl, and higher-Tshh) are calculated as shown in equations 11, 12 and 13.

$$Tshrl = TR - |TR - T|, \quad Tshrh = TR + |TR - T| \quad (11)$$

$$Tshgl = TG - |TG - T|, \quad Tshgh = TG + |TG - T| \quad (12)$$

$$Tshbl = TB - |TB - T|, \quad Tshbh = TB + |TB - T| \quad (13)$$

Then the individual colour plane global ternary image maps are computed (TMr, TMg and TMb) as given in equations 14, 15 and 16. If a pixel value of respective colour component is greater than the respective higher threshold interval (Tshh), the corresponding pixel position of the image map gets a value 'one'; else if the pixel value is lesser than the respective lower threshold interval (Tshl), the corresponding pixel position of the image map gets a value of 'minus one'; otherwise it gets a value 'zero'.

$$TMr(i, j) = \begin{cases} 1, & \text{if } .R(i, j) > Tshrh \\ 0, & \text{if } .Tshrl \leq R(i, j) \leq Tshrh \\ -1, & \text{if } .R(i, j) < Tshrl \end{cases} \quad (14)$$

$$TMg(i, j) = \begin{cases} 1, & \text{if } .G(i, j) > Tshgh \\ 0, & \text{if } .Tshgl \leq G(i, j) \leq Tshgh \\ -1, & \text{if } .G(i, j) < Tshgl \end{cases} \quad (15)$$

$$TMb(i, j) = \begin{cases} 1, & \text{if } .B(i, j) > Tshbh \\ 0, & \text{if } .Tshbl \leq B(i, j) \leq Tshbh \\ -1, & \text{if } .B(i, j) < Tshbl \end{cases} \quad (16)$$

4. PROPOSED CBIR METHODS

The feature vector of the image is generated by comparing the image maps with the Haar texture patterns for matching number of ones & minus ones (in case of binary image maps) and ones, zeros and minus ones (in case of ternary image maps). The size of the feature vector of the image is given by equation 17.

$$\text{Feature vector size} = 2 * 3 * (\text{no. of considered texture-pattern}) \quad (17)$$

Five assorted texture pattern sets are used along with original and original-even image to unfold twenty novel feature vector generation methods giving rise to twenty new image retrieval techniques. In the proposed CBIR techniques the combination of original and even part of images gives better results than the original image alone [1,2]. The main advantage of proposed CBIR methods is reduced time complexity for query execution due to reduced size of feature vector resulting into faster image retrieval with better performance. Also the feature vector size is independent of image size in proposed CBIR methods.

Table 1. Feature vector size of discussed image retrieval techniques

CBIR Technique	Feature vector size for Binary Image Maps	Feature vector size for Ternary Image Maps
4-Pattern	8	12
16-Pattern	32	48
64-Pattern	128	192
256-Pattern	512	768
1024-Pattern	2048	3072

5. IMPLEMENTATION

The implementation of the discussed CBIR techniques is done in MATLAB 7.0 using a computer with Intel Core 2 Duo Processor T8100 (2.1GHz) and 2 GB RAM.

The CBIR techniques are tested on the augmented Wang image database [18] of 1000 variable size images spread across 11 categories of human being, animals, natural scenery and manmade things. The categories and distribution of the images is shown in table 2.

To analyse the effectiveness of proposed CBIR techniques, the average precision and recall values of the 55 queries (randomly selected 5 from each image category) have been used as statistical comparison parameters [4,5]. These two parameters have been defined in the equations 11 and 12.

$$\text{Precision} = \frac{\text{Number_of_relevant_images_retrieved}}{\text{Total_number_of_images_retrieved}} \quad (11)$$

$$Recall = \frac{Number_of_relevant_images_retrieved}{Total_number_of_relevant_images_in_database} \quad (12)$$

Table 2. Image Database: Category-wise Distribution

Category	Tribes	Buses	Beaches
No. of Images	85	99	99
Category	Horses	Mountains	Airplanes
No. of Images	99	61	100
Category	Dinosaurs	Elephants	Roses
No. of Images	99	99	99
Category	Monuments	Sunrise	
No. of Images	99	61	

6. RESULTS AND DISCUSSIONS

The performance of the proposed CBIR methods is tested by firing 55 queries (randomly selected 5 from each image category) on the image database. The feature vector of query image and database image are matched using the Euclidian distance. The average precision and recall values are found for all the proposed CBIR methods. The intersection of precision and recall values gives the crossover point. The crossover point of precision and recall is computed for all the proposed CBIR methods. The CBIR technique with higher value of crossover point indicates better performance.

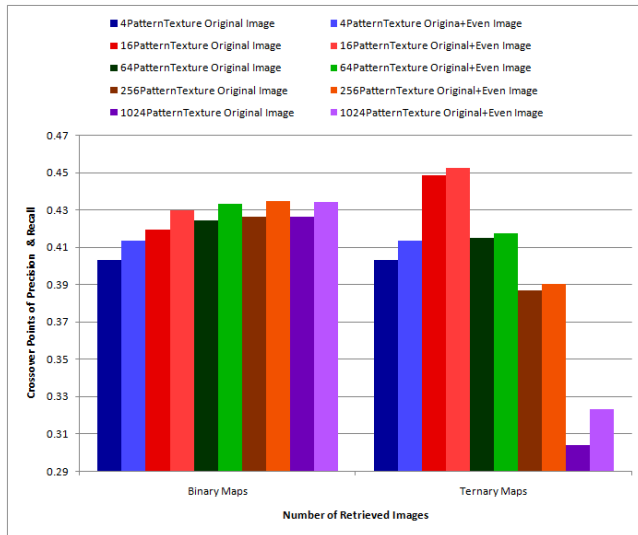


Figure 3. Performance comparison of proposed CBIR methods with binary and ternary image maps

Figure 3 shows the performance comparison of proposed CBIR methods with the binary and ternary image maps. It is observed that in case of binary image maps the performance of the texture pattern based image retrieval increases with increase in number of texture patterns generated. The crossover points of the ‘256-pattern’ texture and ‘1024-pattern’ texture based image retrieval are almost same indicating that the texture based image retrieval gives improved performance up to a certain level only. Moreover as the number of texture patterns generated is increased the size of the feature vector also increases thus increasing the time complexity for query execution. In case of ternary image maps

‘16-pattern’ texture based image retrieval with combination of original and even image gives the highest precision-recall crossover point indicating better performance. Beyond this, on increasing the number of texture patterns, the results start deteriorating.

From the comparison of proposed texture based image retrieval techniques using binary and ternary image maps, it is observed that ‘16-pattern’ texture based image retrieval using ternary image maps with the combination of original and even image gives the highest precision-recall crossover point indicating better performance. The size of the feature vector in ‘16-pattern’ texture based method is around ten times smaller than that of ‘256-pattern’ texture based image retrieval method using binary image maps [30]. Since the size of the feature vector is reduced so is the time complexity in query execution. Feature extraction using the combination of original image with even part of image further improves the performance of the proposed texture pattern based CBIR. Increasing the number of texture patterns helps in performance amelioration up to certain extent only beyond which the performance is degraded and the size of feature vector is also increased.

7. CONCLUSION

As compared to the texture pattern based image retrieval using Haar transform with binary image maps [30], the performance of image retrieval can be ameliorated using the ternary image maps. Among the various texture patterns used for content based image retrieval, “16-pattern” texture patterns using ternary image maps give the best result with the combination of original image and even image part. The precision-recall crossover point of this texture pattern is higher than that of texture patterns with binary image maps [30]. Moreover, it is observed that the performance of proposed CBIR method improves with increasing number of texture patterns up to a certain level. The combination of original image with even image part gives ameliorated performance than the original image alone.

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