

# Performance Evaluation of Voice Traffic of IEEE 802.16e under Femto Cellular Network

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## ABSTRACT

The paper deals with the packet scheduling of voice traffic of IEEE 802.16e under femto cellular network where the length of wireless link is few meters. Instead of distribution of MCS (Modulation and Coding Scheme) levels of previous literature, only availability of traffic channel is considered in packet scheduling since the short wireless link of femto cell is not affected by multipath fading like the link of micro cellular network. The steady probability states of the proposed model is compared with the existing model of WiMAX under Rayleigh fading environment. Finally the performance of the network is measured based on throughput, mean queue length and blocking probability.

## Keywords

Throughput, steady probability states, packet scheduling, transition matrix and mean queue length.

## 1. INTRODUCTION

Initially IEEE 802.16d was developed to support high speed wireless data service of fixed user and its later version IEEE 802.16e supports both fixed and mobile users. In such network sometimes several users are combined on complete sharing mode of traffic channels called subscriber station (SS). To enhance the throughput of broadband wireless network adaptive modulation and channel coding scheme (MCS) is used according to the fading condition of the wireless link. This scheme is widely used in OFDMA based IEEE 802.16e network to support VoIP traffic. IEEE 802.16e is destined for wideband wireless service of Metropolitan Area Network (WMAN). Both WiMAX and 3GPP LTE support VoIP service using IEEE 802.16 where MS sends bandwidth (BW) request and BS allocates it from the central pool of BW. The BS allocates the BW based on availability of BW, possible MCS levels of MSs under fading condition of links between BS and MS. A pictorial presentation of uplink and down link BW scheduling technique is shown in [1]. Three common types of BW allocation algorithms are implemented in [2-3]: Dedicated Resource Allocation (UGS Algorithm) where fixed amount of BW is allocated to each user hence possibility of waste of BW when a user needs to send data at low rate; Polling-Based Resource Allocation (rtPS Algorithm) where BS allocates the BW dynamically therefore incurs some protocol overhead and delay; Hybrid Resource Allocation Algorithm is the combination of above two. IEEE 802.16 deals with five different types of service where the performance of real-time polling service (rtPS) is evaluated in [4]. The down link packet scheduling technique of VoIP traffic is analyzed in [5] based on two states MMPP (Markov Modulated Poisson Process) and probability of using

MCSs level, the similar job is enhanced by the same author for both up and down link in [6].

WiMAX (Worldwide Interoperability for Microwave Access) is the IEEE 802.16 based broadband wireless technology whereas the LTE-Advanced (Long Term Evolution-Advanced) is another 4G wireless service proposed by 3GPP (Third generation Partnership Project). In 2009 4G LTE started its commercial service in Scandinavia. Two important features of LTE are: femtocell deployment and OFDMA-based physical layer access. The architecture of LTE consists of two major parts: the E-UTRAN (Evolved Universal Terrestrial Radio Access Network) and the EPC (Evolved Packet Core) [7-9]. The first part provides air interface between MS or UE to BS and the second part is interconnected switching network called backbone or core network. The core network of LTE is fully IP based packet-switch but the circuit switched network service like voice service is handled by IP multimedia subsystem network. E-UTRAN (Evolved Universal Terrestrial Radio Access Network) deals with two types of Base Stations: Evolved node-B (eNB), which communicates with user equipment like conventional BTS and Home eNode-B (HeNB) of small coverage called femtocell. The very limited service area is covered by femtocell like access points of Wi-Fi. Femto cell is also proposed in 5G mobile cellular network to offload traffic.

The paper is organized like: section 2 provides the traffic model of VoIP of IEEE 802.16e based on Markov chain and MMPP, relation between traffic parameters and fading environment of WiMAX link and LTE; section 3 provides the results bases on analytical model of section 2 and finally section 4 concludes the entire analysis.

## 2. SYSTEM MODEL

Recent literature shows that the most convenient way of evaluating the steady probability states of VoIP traffic is to use combination of two dimensional DTMC (Discrete Time Markov Chain) and MMPP found in [10-12]. To model the burstiness of packet traffic MMPP is preferable compared to ordinary Poisson's model shown in fig.1.

A two state MMPP is represented by:

$$\mathbf{R} = \begin{bmatrix} -r_1 & r_1 \\ r_2 & -r_2 \end{bmatrix} \text{ and } \mathbf{\Lambda} = \begin{bmatrix} \lambda_1 & 0 \\ 0 & \lambda_2 \end{bmatrix}$$

where  $\mathbf{R}$  is transition rate matrix and  $\mathbf{\Lambda}$  is arrival rate matrix.

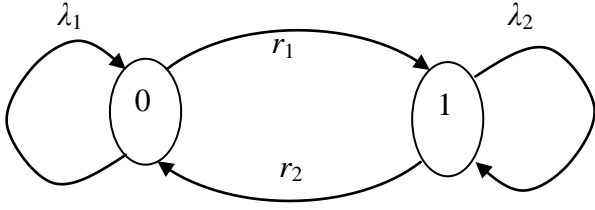


Fig.1 Two state MMPP

The transition matrix,

$$\mathbf{C} = \mathbf{A} - \mathbf{R} = \begin{bmatrix} \lambda_1 + r_1 & -r_1 \\ -r_2 & \lambda_2 + r_2 \end{bmatrix} \quad (1)$$

The state transition probability matrix,

$$\mathbf{U} = \mathbf{C}^{-1} \cdot \mathbf{A} = \begin{bmatrix} \frac{-(\lambda_2 + r_2)\lambda_1}{Y} & \frac{-r_1\lambda_2}{Y} \\ \frac{-r_2\lambda_1}{Y} & \frac{-(\lambda_1 + r_1)\lambda_2}{Y} \end{bmatrix}; \quad (2)$$

where  $Y = \lambda_1\lambda_2 + \lambda_1r_2 + r_1\lambda_2$

Let  $M$  is the number of MCS levels of the wireless link. If  $b$  packets are scheduled in the network then it is represented as an  $M$ -tuple as discussed in [13]:

$$X_b = (x_1, x_2, x_3, \dots, x_M); \text{ where } \sum_{i=1}^M x_i = X_b.$$

A number of  $X_b$  is possible under different combinations of  $x_i$ s with the constraints,

$$\sum_{i=1}^M x_i l_i \leq N_{slot,u} \quad (3)$$

;Where  $x_i$  is the number of packets under MCS level  $i$  and  $l_i$  is the number of slots occupied per  $i$ th MCS level.

If there are  $S$  possible  $X_b$  satisfying above constrain then let us indicate  $j$ th  $X_b$  as  $X_b^j$ . All possible  $X_b^j$  are placed under a set  $\Psi_b$  as [13-14]:

$$\Psi_b = \{X_b^1, X_b^2, X_b^3, \dots, X_b^S\} \quad (4)$$

If a particular  $X_b^j \in \Psi_b$  and after one increment of  $x_n$  satisfies the constraints (3) with  $X_{b+1}^j \in \Psi_{b+1}$  then index probability[14-15],

$$I_n(X_b) = \begin{cases} 1; & \text{if } X_b^j \in \Psi_b \text{ and } X_{b+1}^j \in \Psi_{b+1} \\ 0; & \text{otherwise} \end{cases} \quad (5)$$

Under the constraint (3) we have several  $\Psi_b$ s under the set,  $\Psi = \{\Psi_{b_1+1}, \Psi_{b_1+2}, \Psi_{b_1+3}, \dots, \Psi_{b_2}\}$ ; where the minimum value of  $b$  is  $b_1$  and its maximum value is  $b_2$ .

If a BS is scheduling  $b$  VoIP packets from uplink queue then its probability is expressed as [13-15],

$$P_S^u(b) = P_r \{X_b \in \Psi_b \text{ and } X_{b+1} \notin \Psi_{b+1}\} = \sum_{\forall X_b \in \Psi_b} \left[ \left( b! \prod_{m=1}^M \frac{P_m^{x_m}}{x_m!} \right) \left( 1 - \sum_{m=1}^M P_m \cdot I_m(X_b) \right) \right] \quad (6)$$

Where  $P_m$  is the probability that a packet being modulated by  $m$ th MCS level in uplink.

In [3] the probability of scheduling  $k$  packets by a BS is expressed as,

$$Pr(N(\Psi_{on}) = k) = P_s(k) \quad (7)$$

Where  $P_s(k)$  is the number of cases  $k$  packets can be scheduled.

In a femto cell of LTE a user anywhere inside the cell experiences approximately exponential path loss model since the path length between transmitter and receiver is only of few meters. In microcellular network the link between transmitter and receiver experiences small and large scale fading hence packet scheduling depends on the condition of link of individual users which requires MCS level distribution. The femocellular links are immune of huge fading therefore instead of MCS level distribution we can consider only one type of modulation and coding scheme for voice traffic. In this case we can only change  $P_S^u(b)$  of (6) where the number of uplink packet scheduling depends on availability of traffic channel can be expressed as:

$$P_S^u(b) = 1 - \sum_{x=1}^b P_{n-b+x} \quad (8)$$

;where  $P_x$  is the probability state of occupying  $x$ th traffic channel.

To evaluate  $P_x$  let us use the Markov chain of  $M/M/n/n+K$  shown in fig.2.

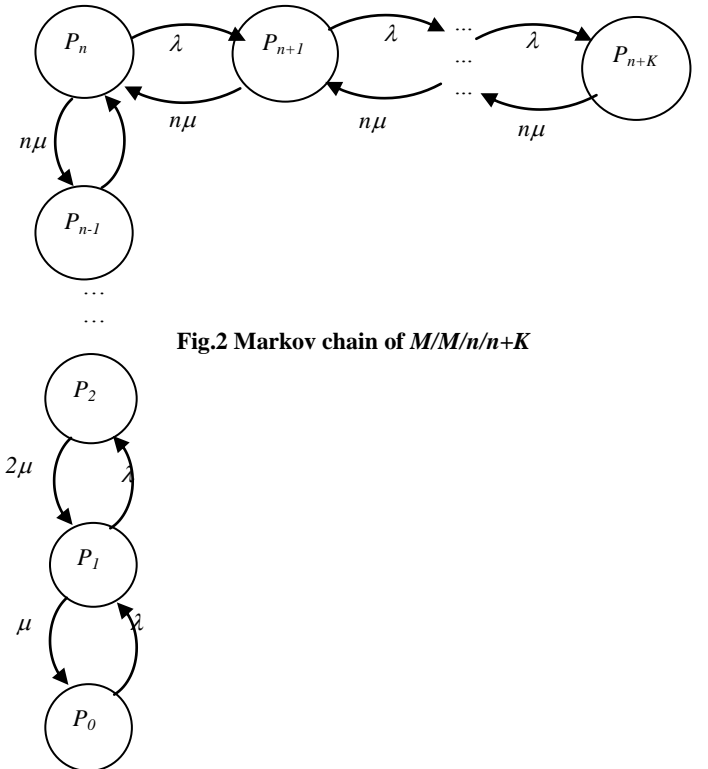


Fig.2 Markov chain of M/M/n/n+K

Solving above chain any probability state in generalized form is derived as,

$$P_x = \begin{cases} \frac{A^x}{x!} & ; x < n \\ \frac{\sum_{i=0}^{n-1} \frac{A^i}{i!} + \frac{A^n}{n!} \sum_{j=0}^K \left(\frac{A}{n}\right)^j}{\sum_{i=0}^{n-1} \frac{A^i}{i!} + \frac{A^n}{n!} \sum_{j=0}^K \left(\frac{A}{n}\right)^j} & ; x \geq n \end{cases} \quad (9)$$

Now the transition matrix of the uplink queue is,

$$\mathbf{P} = \begin{bmatrix} \mathbf{P}_{0,0} & \mathbf{P}_{0,1} & \cdots & \mathbf{P}_{0,K} \\ \mathbf{P}_{1,0} & \mathbf{P}_{1,1} & \cdots & \mathbf{P}_{1,K} \\ \cdots & \cdots & \cdots & \cdots \\ \mathbf{P}_{K,0} & \mathbf{P}_{K,1} & \cdots & \mathbf{P}_{K,K} \end{bmatrix} \quad (10)$$

Elements of the matrix  $\mathbf{P}$  is expressed as [16-17],

$$p_{i,j} = \sum_{b=b_1}^{b_2} \mathbf{U} \mathbf{D}(j - \max(i-b, 0)) P_S^u(b) \quad (11)$$

;where  $\mathbf{U} = (\mathbf{A} - \mathbf{R})^{-1} \mathbf{A}$  and diagonal probability matrix,

$$\mathbf{D}(k) = \begin{bmatrix} \frac{(\lambda_1 T_f)^k}{k!} e^{-\lambda_1 T_f} & 0 \\ 0 & \frac{(\lambda_2 T_f)^k}{k!} e^{-\lambda_2 T_f} \end{bmatrix}$$

Here,  $T_f$  is the duration of a frame,  $\mathbf{R}$  and  $\mathbf{A}$  are the transition rate matrix and arrival rate matrix of MMPP.

The steady probability vector  $\boldsymbol{\pi}$  can be found from [18-20],

$$\boldsymbol{\Pi} \cdot \mathbf{P} = \boldsymbol{\Pi} \text{ and } \boldsymbol{\Pi} \cdot \mathbf{1} = 1 \quad (12)$$

If  $\boldsymbol{\Pi} = [\pi_1 \ \pi_2 \ \pi_3 \ \cdots \ \pi_{2K_u+2}]$  then

$$\pi(i) = \pi_{2i-1} + \pi_{2i}$$

The mean queue length,

$$\bar{L} = \sum_{i=1}^{K_u} i \cdot \pi(i) \quad (13)$$

Finally the throughput or the carried traffic is:

$$Th = 1 - \boldsymbol{\pi}(K_u) \text{ *(offered traffic)} \quad (14)$$

Next section provides the results based on analysis of this section.

### 3. RESULTS

Let us consider a system with 3 MCS levels shown in table -1. Considering  $N_s = 50$  TS as the available resources the BS can schedule. The number of packets under  $m$ th MCS level is  $x_m$ , here  $m = 1, 2$  and  $3$  since the case of 3 MCS levels. We have to check whether,  $36x_1 + 24x_2 + 12x_3 \leq N_s$  or not.

Table-1

MCS levels	Modulation	Slot/PDU
1	BPSK	36
2	QPSK	24
3	16-QAM	12

Now,  $X_1 = (x_1, x_2, x_3) = (1, 0, 0)$ ; slots =  $1 \times 36 = 36 < N_s$ ,

$$X_1 = \{(0, 1, 0)\}; \text{ slots} = 1 \times 24 = 24 < N_s$$

$$X_1 = \{(0, 0, 1)\}; \text{ slots} = 1 \times 12 = 12 < N_s$$

The possible set of  $X_1$ ,

$$\Psi_1 = \{(1, 0, 0), (0, 1, 0), (0, 0, 1)\};$$

Similarly

$$\Psi_2 = \{(1, 0, 1), (0, 2, 0), (0, 1, 1), (0, 0, 2)\};$$

$$\Psi_3 = \{(0, 1, 2), (0, 0, 3)\};$$

$$\Psi_4 = \{(0, 0, 4)\};$$

Now,

$$\boldsymbol{\Psi} = \{\Psi_1, \Psi_2, \Psi_3, \Psi_4\};$$

The minimum number of PDU from  $\Psi_1$  is 1 i.e.  $b_1 = 1$  and the maximum number of PDU from  $\Psi_4$  is 4 i.e.  $b_2 = 4$ .

Now the index probability  $I_m(X_b)$  can be found for  $m = 1, 2$  and  $3$  and  $b = 1, 2, 3$  and  $4$ .

$$(1, 0, 0) \in \Psi_1; I_3(X_1) = 1, I_1(X_1) = I_2(X_1) = 0$$

$$(0, 1, 0) \in \Psi_1; I_2(X_1) = I_3(X_1) = 1, I_1(X_1) = 0$$

$$(0, 0, 1) \in \Psi_1; I_1(X_1) = I_2(X_1) = I_3(X_1) = 1$$

$$(1, 0, 1) \in \Psi_2; I_3(X_2) = 1, I_1(X_2) = I_2(X_2) = 0$$

$$(0, 2, 0) \in \Psi_2; I_1(X_2) = I_2(X_2) = I_3(X_2) = 0$$

$$(0, 1, 1) \in \Psi_2; I_1(X_2) = I_2(X_2) = 0, I_3(X_2) = 1$$

$$(0, 0, 2) \in \Psi_2; I_2(X_2) = I_3(X_2) = 0, I_1(X_2) = 0$$

$$(0, 1, 2) \in \Psi_3; I_1(X_3) = I_2(X_3) = 0, I_3(X_3) = 1$$

$$(0, 0, 3) \in \Psi_3; I_1(X_3) = I_2(X_3) = 0, I_3(X_3) = 1$$

$$(0, 0, 4) \in \Psi_4; I_1(X_4) = I_2(X_4) = I_3(X_4) = 0$$

Now the probability that BS schedules  $b$  packets from uplink queue:

$$P(b=1) = 1! \cdot \frac{P_1^1}{1!} \cdot 1.1 \cdot \{1 - P_3\} + 1! \cdot 1! \cdot \frac{P_2^1}{1!} \cdot 1.$$

$$\{1 - P_2 - P_3\} + 1! \cdot 1.1 \cdot \frac{P_3^1}{1!} \cdot \{1 - P_1 - P_2 - P_3\}$$

$$P(b=2) = 2! \cdot \frac{P_1^1}{1!} \cdot 1.1 \cdot \frac{P_2^1}{1!} \cdot \{1 - 0\} + 2! \cdot 1.1 \cdot \frac{P_2^2}{2!} \cdot 1.1 \cdot \{1 - 0\}$$

$$+ 2! \cdot 1.1 \cdot \frac{P_2^1}{1!} \cdot \frac{P_3^1}{1!} \cdot \{1 - P_3\} + 2! \cdot 1.1 \cdot \frac{P_3^2}{2!} \cdot \{1 - P_2 - P_3\}$$

$$P(b=3) = 3! \cdot 1.1 \cdot \frac{P_2^1}{1!} \cdot \frac{P_3^2}{2!} \cdot \{1 - 0\} + 3! \cdot 1.1 \cdot \frac{P_3^3}{3!} \cdot \{1 - P_3\}$$

$$P(b=4) = 4! \cdot 1.1 \cdot \frac{P_3^4}{4!} \cdot \{1 - 0\}$$

$P_m$  is the probability that a packet being modulated by  $m$ th MCS level in uplink. For Rayleigh fading environment,

$$P_1 = \int_0^{\gamma_1} \frac{1}{\gamma_{av}} e^{-\gamma/\gamma_{av}} d\gamma, \quad P_2 = \int_{\gamma_1}^{\gamma_2} \frac{1}{\gamma_{av}} e^{-\gamma/\gamma_{av}} d\gamma \quad \text{and}$$

$$P_3 = \int_{\gamma_2}^{\gamma_3} \frac{1}{\gamma_{av}} e^{-\gamma/\gamma_{av}} d\gamma$$

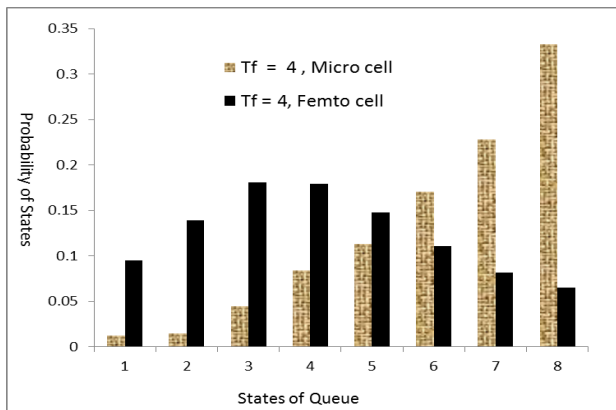
Now,  $P(b) = \sum_{i=b_1}^{b_2} P(i)$ ; where  $b_1 = 1$  and  $b_2 = 4$

We consider the traffic parameters:  $\lambda_1 = 0.656$ ,  $\lambda_2 = 0.842$ ,  $r_1 = 0.41$  and  $r_2 = 0.32$ , the corresponding matrix becomes,

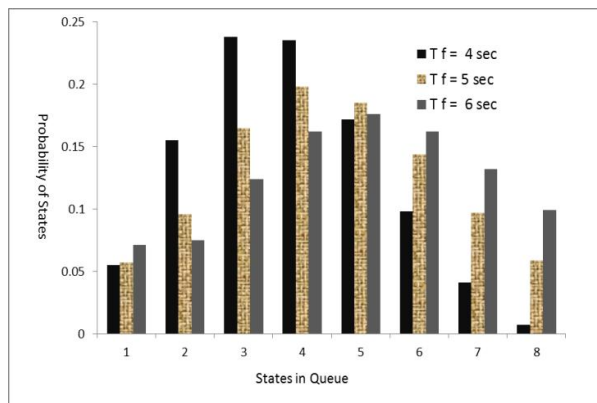
$$\mathbf{U} = \begin{bmatrix} 0.688 & 0.312 \\ 0.19 & 0.81 \end{bmatrix},$$

$$\mathbf{D}(k=1) = \begin{bmatrix} 0.061 & 0 \\ 0 & 0.077 \end{bmatrix}$$

The steady probability states:  $\pi(i)$ ,  $i = 1, 2, 3, \dots, 8$  is shown in fig.3 for both the fading channel of WiMAX and awgn channel of femto cell (using eq. (12)). The distribution of probability state is like Gaussian for femto cell and found exponential for the case of fading channel of WiMAX. The probability of occupancy of whole queue or blocking probability is found higher in WiMAX because of adverse condition of channel in sending the packets.

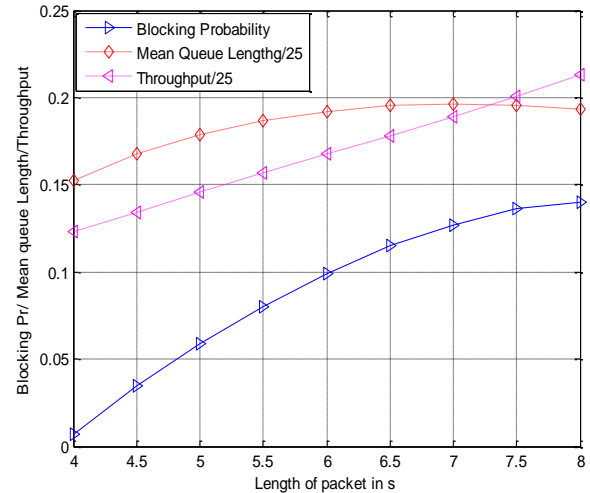


**Fig.3 Comparison of states of queue of WiMAX under Rayleigh fading and that of femto cellular network under AWGN**



**Fig.4 Impact of packet length on steady probability states**

The impact of packet length on probability state is shown in fig.4 where we consider large packets of length: 4, 5 and 6s. At lower packet length the occupancy of lower probability states are found higher i.e. availability of space of buffer but for larger packet the tendency of occupancy of higher states are found higher hence gives the indication of full occupancy of buffer or higher blocking probability.



**Fig.5 Impact of length of packet on performance of femto cellular network**

Finally fig.5 shows the profile of blocking probability, normalized mean queue length and throughput of the network against the length of packets. All the parameters rise with increase in the length of packet since the offered is directly proportional the length of packet. The mean queue length become saturated at some threshold value of  $T_f = 6.5$ s which indicates the fully occupied condition of the queue.

#### 4. CONCLUSIONS

The paper actually compares the steady probability states of voice traffic of WiMAX and that of femto cellular network of LTE. The profile of blocking probability, normalized throughput and mean queue length are shown against the length of packet. The traffic model we consider is  $M/M/n/n+K$  but we can extend the work for traffic of  $M/D/1/K$  of fixed cell or mixed traffic like  $M/G/1/K$ . Traffic shaping algorithm can also be incorporated to observe the improvement of throughputs. Even the concept of the paper in can be applied in cognitive radio network only adding the parameters: probability of correct detection of primary users on a traffic channel and the probability availability of free traffic channels. The concept of the paper is also applicable in ultra dense cellular network of 5G.

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