# On Intuitionistic Fuzzy Weakly π Generalized Continuous Mapping

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### ABSTRACT

The purpose of this paper is to introduce and study the concepts of intuitionistic fuzzy weakly  $\pi$  generalized continuous mappings defined on intuitionistic fuzzy topological space. Some of its properties are derived.

#### Keywords

Intuitionistic fuzzy topology, intuitionistic fuzzy weakly  $\pi$  generalized closed set and open set, intuitionistic fuzzy weakly  $\pi$  generalized continuous mappings, intuitionistic fuzzy w $\pi T_{1/2}$  space and intuitionistic fuzzy w $\pi gT_{q}$  space.

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#### **1. INTRODUCTION**

The concept of fuzzy sets was introduced by Zadeh [16] in 1965. Then this concept was generalized into intuitionistic fuzzy (IF) by Atanassov [1] in 1986. After the introduction of IF sets, many research articles have been published in the study of examining and exploring, how far the basic concepts and theorems, defined in crisp sets and in fuzzy sets remain true in the new environment. The concept of fuzzy topology was introduced by Chang [3] in 1968. In 1997, Coker [4] initiated the concept of generalization of fuzzy topology into IF topology. The apprehension of semi closed,  $\alpha$  closed, semi pre-closed, weakly closed had been introduced in his paper. Further their properties are derived.

In this paper, the concept of IF weakly  $\pi$  generalized continuous mappings is introduced and studied with examples. The derivations of some of its properties are done. Illustrations are given to testify the derived results.

This paper is organized into five sections. In the first section historical development of the concepts were discussed. Second section is devoted for basic definitions and results, needed for this work. Section three discusses the IF weakly  $\pi$  generalized continuous mappings. Suitable examples are given in each section. Application of the concepts introduced in section three is studied on IFw $\pi$ T<sub>1/2</sub> space and IFw $\pi$ gr<sub>q</sub> space into section four. Conclusion of this study is in section five.

## 2. PRELIMINARIES

**Definition 2.1:** Let *X* be a non-empty crisp set. An intuitionistic fuzzy (IF) set A in X is defined as an object of the form [1]

 $A = \{ < x, \mu_A(x), \nu_A(x) > | x \in X \},\$ 

where the functions  $\mu_A(x) : X \rightarrow [0, 1]$  and

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 $\nu_A(x): X \to [0, 1]$  denote the degree of membership (namely  $\mu_A$ ) and the degree of non-membership (namely  $\nu_A$ ) of each element  $x \in X$  to the set A, respectively, and  $0 \le \mu_A(x) + \nu_A(x) \le 1$  for each  $x \in X$ . The set of all intuitionistic fuzzy sets in X is denoted by IFS(X).

**Definition 2.2**: Let A and B be IFSs of the form [1],

A = { <  $x, \mu_A(x), \nu_A(x) > | x \in X$  }, B = { <  $x, \mu_B(x), \nu_B(x) > | x \in X$  }.

The operations  $\land$  and  $\lor$  are defined on  $\mu_A(x), \mu_B(x), \nu_A(x)$ , and  $\nu_B(x)$  as follows,

 $\mu_{A}(x) \wedge \mu_{B}(x) = \min \{ \mu_{A}(x), \mu_{B}(x) \},\$ 

 $\nu_{A}(x) \lor \nu_{B}(x) = \max \{ \nu_{A}(x), \nu_{B}(x) \},\$ 

 $\mu_A(x) \lor \mu_B(x) = \max \{ \mu_A(x), \mu_B(x) \}$  and

 $\nu_A(x) \wedge \nu_B(x) = \min \{ \nu_A(x), \nu_B(x) \}.$  Then,

i)  $A \subseteq B$  if and only if  $\mu_A(x) \le \mu_B(x)$  and  $\nu_A(x) \ge \nu_B(x)$  for all  $x \in X$ , similarly  $A \supseteq B$ 

can be defined,

ii) A = B if and only if A  $\subseteq$  B and B  $\subseteq$  A,

iii) 
$$A^{C} = \{ < x, v_{A}(x), \mu_{A}(x) > | x \in X \}$$
, here the

membership grade of x in A is the

non-membership grade of x in A<sup>C</sup> and vice versa,

iv) 
$$A \cap B = \{ \langle x, \mu_A(x) \land \mu_B(x), \nu_A(x) \lor \nu_B(x) \rangle | x \in X \}$$
, and

v)  $A \cup B = \{ < x, \mu_A(x) \lor \mu_B(x), \nu_A(x) \land \nu_B(x) > | x \in X \}.$ 

For the sake of simplicity, the notation

 $A = \langle x, \mu_A, \nu_A \rangle$  is used instead of

 $A = \{ < x, \mu_A(x), \nu_A(x) > | x \in X \}.$ 

The intuitionistic fuzzy sets  $0_{\sim}$  and  $1_{\sim}$  are defined respectively as,  $0_{\sim} = \{ < x, 0, 1 > | x \in X \}$  and

 $1_{\sim} = \{ \langle x, 1, 0 \rangle | x \in X \}$ . The sets  $0_{\sim}$  and  $1_{\sim}$  are known as the empty set and the whole set of X respectively.

**Definition 2.3**: An intuitionistic fuzzy topology (IFT) is a family  $\tau$  of IFS defined on X satisfying the following axioms [4],

 $i) \quad 0_{\sim} \ , \ 1_{\sim} \ \varepsilon \ \tau \ ,$ 

ii)  $G_1\cap G_2\in\tau$  , for any  $G_1,G_2\in\tau,$ 

iii)  $\cup$  G<sub>i</sub>  $\in \tau$  for any arbitrary family { G<sub>i</sub> | i  $\in$  J }  $\subseteq \tau$ .

Then the pair  $(X, \tau)$  is called an intuitionistic fuzzy topological space (IFTS) and any IFS in  $\tau$  is known as an intuitionistic fuzzy open set (IFOS) in X.

The complement A  $^{C}$  of an IFOS, A in an IFTS (X,  $\tau$ ) is called an intuitionistic fuzzy closed set (IFCS) in X.

**Definition 2.4**: Let  $(X, \tau)$  be an IFTS and

A =  $\langle x, \mu_A, \nu_A \rangle$  be an IFS in X. Then the intuitionistic fuzzy closure and an intuitionistic fuzzy interior are defined by [4],

 $cl(A) = \cap \{ G | G \text{ is an IFCS in X and } A \subseteq G \}$ , and

int (A) =  $\cup$  { K | K is an IFOS in X and K  $\subseteq$  A}.

Note that for any IFS, A in  $(X, \tau)$ ,  $cl(A^{C}) = (int(A))^{c}$  and int  $(A^{c}) = (cl(A))^{c}$ .

**Definition 2.5:** An IFS,  $A = \langle x, \mu_A, \nu_A \rangle$  in an IFTS(X,  $\tau$ ) is said to be an

- i) intuitionistic fuzzy closed set [4] (IFCS) in  $X \Leftrightarrow cl(A) = A$ , and
- ii) intuitionistic fuzzy open set [4] (IFOS) in  $X \Leftrightarrow int(A) = A$ .

**Definition 2.6**: A subset A of a space  $(X, \tau)$  is called

i) regular open [11] if A = int(cl(A)), and

ii)  $\pi$  open [11] if A is the union of regular open sets,

symbolically A is an IF $\pi$ OS in X.

**Definition 2.7:** An IFS,  $A = \langle x, \mu_A, \nu_A \rangle$  in an IFTS(X,  $\tau$ ) is said to be an

i) intuitionistic fuzzy semi closed set [5] (IFSCS) if  $int(cl(A)) \subseteq A$ , and

ii) intuitionistic fuzzy semi open set [5] (IFSOS) if  $A \subseteq cl(int(A))$ .

**Definition 2.8**: Let A be an IFS of an IFTS  $(X, \tau)$ . Then the semi closure of A (scl (A)) and semi interior of A (sint (A)) are defined as [14],

 $scl(A) = \cap \{ G \mid G \text{ is an IFSCS in X and } A \subseteq G \}$ , and

 $sint(A) = \bigcup \{ K \mid K \text{ is an IFSOS in X and } K \subseteq A \}.$ 

**Result 2.1:** Let A be an IFS in  $(X, \tau)$ , then [12]

i)  $scl(A) = A \cup int(cl(A))$ , and

ii)  $sint(A) = A \cap cl(int(A)).$ 

**Definition 2.9:** An IFS  $A = \langle x, \mu_A, \nu_A \rangle$  in an IFTS(X,  $\tau$ ) is said to be an

i) intuitionistic fuzzy  $\alpha$  closed set [5] (IF $\alpha$ CS) if  $cl(int(cl(A))) \subseteq A$ , and

ii) intuitionistic fuzzy  $\alpha$  open set [5] (IF $\alpha$ OS) if  $A \subseteq int(cl(int(A)))$ .

**Definition 2.10**: Let  $A = \langle x, \mu_A, \nu_A \rangle$  be an IFS of an IFTS  $(X, \tau)$ . Then the  $\alpha$  closure of A ( $\alpha$  cl(A)) and  $\alpha$  interior of A ( $\alpha$  int(A)) are defined as [9],  $\alpha$  cl(A) =  $\cap$  { G | G is an IF $\alpha$ CS in X and A  $\subseteq$  G},

 $\alpha$  int (A) =  $\cup \{ K | K \text{ is an IF} \alpha OS \text{ in } X \text{ and } K \subseteq A \}.$ 

**Result 2.2:** Let A be an IFS in  $(X, \tau)$ , then [9]

i)  $\alpha \operatorname{cl}(A) = A \cup \operatorname{cl}(\operatorname{int}(\operatorname{cl}(A)))$ , and

ii)  $\alpha$  int(A) = A  $\cap$  int(cl(int(A))).

**Definition 2.11:** An IFS,  $A = \langle x, \mu_A, \nu_A \rangle$  in an IFTS (X,  $\tau$ ) is said to be an

- i) intuitionistic fuzzy pre-closed set [5] (IFPCS) if,  $cl(int(A)) \subseteq A$ ,
- ii) intuitionistic fuzzy regular closed set [5] (IFRCS) if, cl(int(A)) = A,

iii)intuitionistic fuzzy generalized closed set [13]

(IFGCS) if,  $cl(A) \subseteq U$  whenever  $A \subseteq U$ , U is an

IFOS in X,

iv)intuitionistic fuzzy generalized semi closed set [10]

(IFGSCS) if,  $scl(A) \subseteq U$  whenever  $A \subseteq U$ , U is

an IFOS in X,

v) intuitionistic fuzzy a generalized closed set [9]

(IF $\alpha$ GCS) if,  $\alpha$  cl(A)  $\subseteq$  U whenever A  $\subseteq$  U,U is

an IFOS in X.

**Definition 2.12:** An IFS, A is said to be an intuitionistic fuzzy weakly  $\pi$  generalized closed set [7] (IFW $\pi$ GCS) in (X,  $\tau$ ), if cl(int(A))  $\subseteq$  U whenever A  $\subseteq$  U and U is an IF $\pi$ OS in X.

The family of all IFW $\pi$ GCS of an IFTS (X,  $\tau$ ) is denoted by IFW $\pi$ GCS(X).

**Result 2.3:** Every IFCS, IF $\alpha$ CS, IFGCS, IFRCS, IFPCS, IF $\alpha$ GCS are IFW $\pi$ GCS [7] but the converse need not be true.

**Definition 2.13:** An IFS, A is said to be an intuitionistic fuzzy weakly  $\pi$  generalized open set [7] (IFW $\pi$ GOS) in (X,  $\tau$ ) if, the complement A<sup>c</sup> is an IFW $\pi$ GOS in X.

The family of all IFW $\pi$ GOS of an IFTS (X,  $\tau$ ) is denoted by IFW $\pi$ GOS (X).

**Definition 2.14:** An IFTS  $(X, \tau)$  is called an intuitionistic fuzzy w $\pi T_{1/2}$  space (IF w $\pi T_{1/2}$ ) [7], if every IFW $\pi$ GCS in X is an IFCS in X.

**Definition 2.15:** An IFTS  $(X, \tau)$  is called an intuitionistic fuzzy w $\pi$ gT<sub>q</sub> space (IF w $\pi$ gT<sub>q</sub>) [7], where

0 < q < 1, if every IFW $\pi$ GCS in X is an IFPCS in X.

**Definition 2.16**: Let f be a mapping from an IFTS  $(X, \tau)$  into IFTS  $(Y, \sigma)$ . Then f is said to be intuitionistic fuzzy continuous [5] (IF cts) if,  $f^{-1}(B) \in IFOS(X)$  for every  $B \in \sigma$ .

**Definition 2.17**: Let f be a mapping from an IFTS  $(X, \tau)$  into IFTS $(Y, \sigma)$ . Then f is said to be

- i) intuitionistic fuzzy semi continuous [15] (IFS cts) if,  $f^{-1}(B) \in IFSO(X)$  for every  $B \in \sigma$ ,
- ii) intuitionistic fuzzy  $\alpha$  continuous [15] (IF $\alpha$  cts) if,  $f^{-1}(B) \in IF\alpha O(X)$  for every  $B \in \sigma$ ,
- iii)intuitionistic fuzzy pre continuous [15] (IFP cts) if,  $f^{-1}(B) \in IFPO(X)$  for every  $B \in \sigma$ ,

iv)intuitionistic fuzzy regular continuous [15] (IFR cts)

if,  $f^{-1}(B) \in IFRO(X)$  for every  $B \in \sigma$ .

**Definition 2.18**: Let f be a mapping from an IFTS  $(X, \tau)$  into IFTS  $(Y, \sigma)$ . Then f is said to be intuitionistic fuzzy generalized continuous [10]

(IFG cts) if,  $f^{-1}(B) \in IFGCS$  (X) for every IFCS, B in Y.

**Definition 2.19**: A mapping f:  $(X, \tau) \rightarrow (Y, \sigma)$  is called intuitionistic fuzzy generalized semi continuous [9] (IFGS cts) if, f<sup>-1</sup>(B) is an IFGSCS in  $(X, \tau)$  for every IFCS, B of  $(Y, \sigma)$ .

**Definition 2.20**: A mapping f:  $(X, \tau) \rightarrow (Y, \sigma)$  is called intuitionistic fuzzy  $\alpha$  generalized continuous [9]

(IFaGS cts) if,  $f^{-1}(B)$  is an IFaGCS in  $(X, \tau)$  for every IFCS, B of  $(Y, \sigma)$ .

## 3. INTUITIONISTIC FUZZY WEAKLY π GENERALIZED CONTINUOUS MAPPINGS

In this section, intuitionistic fuzzy weakly  $\pi$  generalized continuous mappings is defined. Some of its properties are derived.

**Definition 3.1:** A mapping  $f: (X, \tau) \rightarrow (Y, \sigma)$  is called an intuitionistic fuzzy weakly  $\pi$  generalized continuous mapping (IFW $\pi$ G cts) if,  $f^{-1}(B)$  is an IFW $\pi$ GCS in  $(X, \tau)$  for every IFCS, B of  $(Y, \sigma)$ .

**Example 3.1**: Let  $X = \{a, b\}, Y = \{u, v\}$  and

 $G_1 = \langle x, (0.2, 0.2), (0.6, 0.7) \rangle$ 

 $G_2 = \langle y, (0.6, 0.7), (0.4, 0.2) \rangle$ . Then

 $\tau=\{\ 0_{\sim}\,,G_1,1_{\sim}\,\}$  and  $\sigma=\{\ 0_{\sim}\,,G_2,1_{\sim}\,\}$  are IFTs on X and Y respectively. Define a mapping

f:  $(X, \tau) \rightarrow (Y, \sigma)$  by f(a) = u and f(b) = v. Then f is an IFW $\pi$ G continuous mapping.

**Proposition 3.1**: Every IF continuous mapping is an IFW $\pi$ G continuous mapping but not conversely.

**Proof:** Let  $f: (X, \tau) \rightarrow (Y, \sigma)$  be an IF continuous mapping. Let B be an IFCS in Y. Since f is IF continuous mapping,  $f^{-1}(B)$  is an IFCS in X. Since every IFCS is an IFW $\pi$ GCS,  $f^{-1}(B)$  is an IFW $\pi$ GCS in X. Therefore f is an IFW $\pi$ G continuous mapping.

**Example 3.2**: Let  $X = \{a, b\}, Y = \{u, v\}$  and

 $G_1 = \langle x, (0.1, 0.2), (0.8, 0.7) \rangle$ 

 $G_2 = \langle y, (0.8, 0.7), (0.1, 0.3) \rangle$ . Then

 $\tau = \{ 0_{\sim}, G_1, 1_{\sim} \}$  and  $\sigma = \{ 0_{\sim}, G_2, 1_{\sim} \}$  are IFTs on X and Y respectively. Define a mapping

f:  $(X, \tau) \rightarrow (Y, \sigma)$  by f(a) = u and f(b) = v. The IFS,  $B = \langle y, (0.1, 0.3), (0.8, 0.7) \rangle$  is IFCS in Y. Then  $f^{-1}(B)$  is IFW $\pi$ GCS in X, but not IFCS in X. Therefore f is an IFW $\pi$ G continuous mapping but not an IF continuous mapping.

**Proposition 3.2**: Every IF $\alpha$  continuous mapping is an IFW $\pi$ G continuous mapping but not conversely.

**Proof:** Let  $f: (X, \tau) \rightarrow (Y, \sigma)$  be an IF $\alpha$  continuous mapping. Let B be an IFCS in Y. Then by definition  $f^{-1}(B)$  is an IF $\alpha$ CS in X. Since every IF $\alpha$ CS is an IFW $\pi$ GCS,  $f^{-1}(B)$  is an IFW $\pi$ GCS in X. Thus f is an IFW $\pi$ G continuous mapping.

**Example 3.3**: Let  $X = \{a, b\}, Y = \{u, v\}$  and

 $G_1 = \langle x, (0.4, 0.3), (0.6, 0.5) \rangle$ ,

 $G_2 = \langle y, (0.2, 0.3), (0.5, 0.4) \rangle$ . Then

 $\tau$  = {  $0_{\sim}$  ,  $G_1,1_{\sim}$  } and  $\sigma$  = {  $0_{\sim}$  ,  $G_2,1_{\sim}$  } are IFTs on X and Y respectively. Define a mapping

f:  $(X, \tau) \rightarrow (Y, \sigma)$  by f(a) = u and f(b) = v. The IFS,  $B = \langle y, (0.5, 0.4), (0.2, 0.3) \rangle$  is IFCS in Y. Then  $f^{-1}(B)$  is IFW $\pi$ GCS in X, but not IF $\alpha$ CS in X. Then f is an IFW $\pi$ G continuous mapping but not an IF $\alpha$  continuous mapping.

**Proposition 3.3**: Every IFR continuous mapping is an IFW $\pi$ G continuous mapping but not conversely.

**Proof:** Let  $f: (X, \tau) \rightarrow (Y, \sigma)$  be an IFR continuous mapping. Let B be an IFCS in Y. Then by definition  $f^{-1}(B)$  is an IFRCS in X. Since every IFRCS is an IFW $\pi$ GCS,  $f^{-1}(B)$  is an IFW $\pi$ GCS in X. So, f is an IFW $\pi$ G continuous mapping.

**Example 3.4**: Let  $X = \{a, b\}, Y = \{u, v\}$  and

 $G_1 = \langle x, (0.5, 0.4), (0.4, 0.5) \rangle$ 

 $G_2 = \langle y, (0.5, 0.5), (0.4, 0.3) \rangle$ . Then

 $\tau = \{ 0_{\sim}, G_1, 1_{\sim} \}$  and  $\sigma = \{ 0_{\sim}, G_2, 1_{\sim} \}$  are IFTs on X and Y respectively. Define a mapping

f:  $(X, \tau) \rightarrow (Y, \sigma)$  by f(a) = u and f(b) = v. The IFS,  $B = \langle y, (0.4, 0.3), (0.5, 0.5) \rangle$  is IFCS in Y. Then  $f^{-1}(B)$  is IFW $\pi$ GCS in X, but not IFRCS in X. Therefore f is IFW $\pi$ G continuous mapping but not an IFR continuous mapping.

**Proposition 3.4**: Every IFP continuous mapping is an IFW $\pi$ G continuous mapping but not conversely.

**Proof:** Let  $f: (X, \tau) \rightarrow (Y, \sigma)$  be an IFP continuous mapping. Let B be an IFCS in Y. Then  $f^{-1}(B)$  is an IFPCS in X. Since every IFPCS is an IFW $\pi$ GCS,  $f^{-1}(B)$  is an IFW $\pi$ GCS in X. Therefore f is an IFW $\pi$ G continuous mapping.

**Example 3.5**: Let  $X = \{a, b\}, Y = \{u, v\}$  and

 $G_1 = \langle x, (0.4, 0.3), (0.6, 0.7) \rangle,$ 

 $G_2 = \langle y, (0.6, 0.4), (0.4, 0.4) \rangle$ . Then  $\tau = \{ 0_{\sim}, G_1, 1_{\sim} \}$  and  $\sigma = \{ 0_{\sim}, G_2, 1_{\sim} \}$  are IFTs on X and Y respectively. Define a mapping

f:  $(X, \tau) \rightarrow (Y, \sigma)$  by f(a) = u and f(b) = v. The IFS,  $B = \langle y, (0.4, 0.4), (0.6, 0.4) \rangle$  is IFCS in Y. Then  $f^{-1}(B)$  is

IFW $\pi$ GCS in X, but not IFPCS in X. Therefore f is IFW $\pi$ G continuous mapping but not an IFP continuous mapping.

**Proposition 3.5:** Every IFG continuous mapping is an  $IFW\pi G$  continuous mapping but not conversely.

**Proof:** Let f:  $(X, \tau) \rightarrow (Y, \sigma)$  be an IFG continuous mapping. Let B be an IFCS in Y. Since f is an IFG continuous mapping,  $f^{-1}(B)$  is an IFGCS in X. Since every IFGCS is an IFW $\pi$ GCS,  $f^{-1}(B)$  is an IFW $\pi$ GCS in X. Thus f is an IFW $\pi$ G continuous mapping.

**Example 3.6**: Let  $X = \{a, b\}$ ,  $Y = \{u, v\}$  and  $G_1 = \langle x, (0.2, 0.3), (0.7, 0.6) \rangle$ ,

f:  $(X, \tau) \rightarrow (Y, \sigma)$  by f(a) = u and f(b) = v. The IFS,  $B = \langle y, (0.2, 0.2), (0.8, 0.7) \rangle$  is IFCS in Y,  $f^{-1}(B)$  is IFW $\pi$ GCS in X but not IFGCS in X. Therefore f is IFW $\pi$ G continuous mapping but not an IFG continuous mapping.

**Proposition 3.6**: Every IF $\alpha$ G continuous mapping is an IFW $\pi$ G continuous mapping but not conversely.

**Proof:** Let f:  $(X, \tau) \rightarrow (Y, \sigma)$  be an IF $\alpha$ G continuous mapping. Let B be an IFCS in Y. Then by definition, f<sup>-1</sup>(B) is an IF $\alpha$ GCS in X. Since every IF $\alpha$ GCS is an IFW $\pi$ GCS, f<sup>-1</sup>(B) is an IFW $\pi$ GCS in X. So, f is an IFW $\pi$ G continuous mapping.

**Example 3.7**: Let  $X = \{a, b\}, Y = \{u, v\}$  and

 $G_1 = \langle x, (0.4, 0.6), (0.2, 0.2) \rangle$ 

 $G_2 = \langle y, (0.6, 0.2), (0.4, 0.3) \rangle$ . Then  $\tau = \{ 0_{\sim}, G_1, 1_{\sim} \}$  and  $\sigma = \{ 0_{\sim}, G_2, 1_{\sim} \}$  are IFTs on X and Y respectively. Define a mapping

f:  $(X, \tau) \rightarrow (Y, \sigma)$  by f(a) = u and f(b) = v. The IFS,  $B = \langle y, (0.4, 0.3), (0.6, 0.2) \rangle$  is IFCS in Y. Then  $f^{-1}(B)$  is IFW $\pi$ GCS in X, but not IF $\alpha$ GCS in X. Therefore f is IFW $\pi$ G continuous mapping but not an IF $\alpha$ G continuous mapping.

**Remark 3.1**: IFS continuous mapping and IFW $\pi$ G continuous mapping are independent to each other. **Example 3.8**: Let X = {a, b}, Y = {u, v} and

 $G_1 = \langle x, (0.4, 0.3), (0.6, 0.7) \rangle$ 

 $G_2 = \langle y, (0.6, 0.7), (0.4, 0.3) \rangle$ . Then  $\tau = \{ 0_{\sim}, G_1, 1_{\sim} \}$  and  $\sigma = \{ 0_{\sim}, G_2, 1_{\sim} \}$  are IFTs on X and Y respectively. Define a mapping

f:  $(X, \tau) \rightarrow (Y, \sigma)$  by f(a) = u and f(b) = v. Then f is IFS continuous mapping but not an IFW $\pi$ G continuous mapping, since  $B = \langle y, (0.4, 0.3), (0.6, 0.2) \rangle$  is an IFSCS in Y, but  $f^{-1}(B) = \langle x, (0.4, 0.3), (0.6, 0.2) \rangle$  is not an IFW $\pi$ GCS in X.

**Example 3.9**: Let  $X = \{a, b\}, Y = \{u, v\}$  and

 $G_1 = \langle x, (0.9, 0.7), (0.1, 0.2) \rangle$ 

 $\begin{array}{ll} G_2 = < y, (0.3, 0.4), (0.7, 0.6) >. & \mbox{Then } \tau = \\ \{ \ 0_{\sim}, G_1, 1_{\sim} \} \ \mbox{and } \sigma = \{ \ 0_{\sim}, G_2, 1_{\sim} \} \ \mbox{are IFTs on } X \ \mbox{and } Y \ \mbox{respectively. Define a mapping} \end{array}$ 

f:  $(X, \tau) \rightarrow (Y, \sigma)$  by f(a) = u and f(b) = v. Then f is IFW $\pi$ G continuous mapping, but not an IFS continuous mapping, since  $B = \langle y, (0.7, 0.6), (0.3, 0.4) \rangle$  is an IFW $\pi$ GCS in Y, but  $f^{-1}(B) = \langle x, (0.7, 0.6), (0.3, 0.4) \rangle$  is not an IFSCS in X

**Remark 3.2**: IFGS continuous mapping and IFW $\pi$ G continuous mapping are independent to each other.

**Example 3.10**: Let  $X = \{a, b\}$ ,  $Y = \{u, v\}$  and  $G_1 = \langle x, (0.2, 0.3), (0.5, 0.5) \rangle$ ,

 $G_2 = \langle y, (0.5, 0.5), (0.2, 0.3) \rangle$ . Then

 $\tau = \{ 0_{\sim}, G_1, 1_{\sim} \}$  and  $\sigma = \{ 0_{\sim}, G_2, 1_{\sim} \}$  are IFTs on X and Y respectively. Define a mapping

f:  $(X, \tau) \rightarrow (Y, \sigma)$  by f(a) = u and f(b) = v. Then f is IFGS continuous mapping, but not an IFW $\pi$ G continuous mapping, since  $B = \langle y, (0.2, 0.3), (0.5, 0.5) \rangle$  is an IFGSCS in Y, but  $f^{-1}(B) = \langle x, (0.2, 0.3), (0.5, 0.5) \rangle$  is not an IFW $\pi$ GCS in X.

**Example 3.11**: Let  $X = \{a, b\}$ ,  $Y = \{u, v\}$  and  $G_1 = \langle x, (0.5, 0.6), (0.2, 0.2) \rangle$ ,

 $G_2 = \langle y, (0.6, 0.6), (0.3, 0.2) \rangle$ . Then  $\tau = \{ 0_{\sim}, G_1, 1_{\sim} \}$  and  $\sigma = \{ 0_{\sim}, G_2, 1_{\sim} \}$  are IFTs on X and Y respectively. Define a mapping

f:  $(X, \tau) \rightarrow (Y, \sigma)$  by f(a) = u and f(b) = v. Then f is IFW $\pi$ G continuous mapping, but not an IFGS continuous mapping, since  $B = \langle y, (0.3, 0.2), (0.6, 0.6) \rangle$  is an IFW $\pi$ GCS in Y but  $f^{-1}(B) = \langle x, (0.3, 0.2), (0.6, 0.6) \rangle$  is not an IFGSCS in X.

**Remark 3.3**: The derived relationship among the terms can be schematically presented as follows.

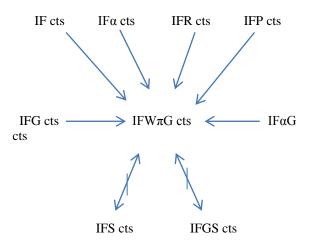


Fig.3.1 Relationships between the intuitionistic fuzzy weakly  $\pi$  generalized continuous mapping, and the other existing continuous mapping on intuitionistic fuzzy closed sets.

# 4. APPLICATIONS OF INTUITIONISTIC FUZZY WEAKLY π GENERALIZED CLOSED MAPPING

**Proposition 4.1**: A mapping f:  $(X, \tau) \rightarrow (Y, \sigma)$  is IFW $\pi$ G continuous, then the inverse image of each IFOS in Y is an IFW $\pi$ GOS in X.

Proof: Let B be an IFOS in Y. This implies  $B^c$  is IFCS in Y. Since f is IFW $\pi$ G continuous,  $f^{-1}(B^c)$  is IFW $\pi$ GCS in X. Since  $f^{-1}(B^c) = (f^{-1}(B))^c$ ,  $f^{-1}(B)$  is an IFW $\pi$ GOS in X.

**Proposition 4.2**: Let  $f: X \to Y$  be an IFW $\pi$ G continuous mapping and X be an IFw $\pi$ T<sub>1/2</sub> space. Then f is an IF continuous mapping.

Proof: Let X be an  $IFw\pi T_{1/2}$  space and B be an IFCS in Y. Then by definition (2.14),  $f^{-1}(B)$  is an  $IFW\pi GCS$  in X. So,  $f^{-1}(B)$  is an IFCS in X. Therefore f is an IF continuous mapping.

**Proposition 4.3**: Let  $f: X \rightarrow Y$  be an IFW $\pi$ G continuous mapping and X be an IFw $\pi$ gT<sub>q</sub> space, where 0 < q < 1. Then f is an IFG continuous mapping.

**Proof:** Let X be an IFw $\pi$ gT<sub>q</sub> space, B be an IFCS in Y. Then by definition (2.15), f<sup>-1</sup>(B) is an IFW $\pi$ GCS in X. So, f<sup>-1</sup>(B) is an IFGCS in X. Thus f is a IFG continuous mapping.

**Proposition 4.4**: A mapping f:  $(X, \tau) \rightarrow (Y, \sigma)$  be an IFW $\pi$ G continuous mapping and g:  $(Y, \sigma) \rightarrow (Z, \delta)$  is

IF continuous, then  $g \circ f : (X, \tau) \to (Z, \delta)$  is an IFW $\pi G$  continuous.

**Proof:** Let D be an IFCS in Z. Then by definition  $g^{-1}(D)$  is an IFCS in Y. Since f is an IFW $\pi$ G continuous mapping, inverse image of a IFCS in Y is a IFW $\pi$ GCS in X. ie.,  $f^{-1} \circ (g^{-1}(D)) = (g \circ f)^{-1}(D)$  is an IFW $\pi$ GCS in X. Therefore  $g \circ f$  is a IFW $\pi$ G continuous mapping.

# 5. CONCLUSION

In this paper, a special type of IF cts mapping , namely IFW $\pi$ G continuous mapping is introduced. Their relationships have been studied. Some of the basic properties of intuitionistic fuzzy weakly  $\pi$  generalized continuous mapping are derived. Also the relationship among the intuitionistic fuzzy weakly  $\pi$  generalized continuous mapping and other existing intuitionistic fuzzy continuous mappings are obtained. It is given, schematically in figure (3.1).

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