# Cryptanalysis of C-3 PEKE Protocol 

R.Padmavathy<br>National Institute of<br>Technology, Warangal,<br>Andhra Pradesh, India


#### Abstract

The key exchange protocol using passwords achieved great attention due to its simplicity and efficiency. Recently, Chang proposed a practical three-party key exchange (C-3 PEKE) protocol with round efficiency. Later, Lee and Chang presented an off-line password guessing attack on C-3 PEKE protocol. In the present paper, an impersonation-of-the initiator attack and impersonation-of-the responder attack are demonstrated on C-3 PEKE protocol using the off-line password guessing attack proposed by Lee and Chang.


.Keywords- C-3 PEKE protocol, off-line password guessing attack, impersonation-of-the-initiator attack, impersonation-of-the-responder attack

## 1. INTRODUCTION

The key exchange protocol is one of the most elegant ways of establishing secure communication between pair of users by using a session key. The session key, which is exchanged between two users, assures the secure communication for later sessions. The first practical key exchange protocol is proposed by Diffie-Hellman [10]. Since the introduction of key ex-change protocol by Diffie-Hellman, various versions and improvements in key exchange protocol have been developed [1,4,6,7,12]. In the line of key exchange protocol development, password based key exchange mechanism achieved great attention due to its simplicity and wide range of applicability, as it requires the users to remember the easily remembrable password. Even though the protocol is simple and efficient, it should not be vulnerable to any type of off line, undetectable or detectable on line password guessing attacks, since the passwords are of lowentropy.

In general the password guessing attacks can be divided into three classes and they are listed below:

- Detectable on-line password guessing attacks: An attacker attempts to use a guessed password in an on-line transaction. $\mathrm{He} /$ She verifies the correctness of his/her guess using the response from server. A failed guess can be detected and logged by the server.
- Undetectable on-line password guessing attacks: Similar to Detectable on-line password guessing attack, an attacker tries to verify a password guess in an on-line transaction. However, a failed guess cannot be detected and logged by server, as server is not able to distinguish an honest request from a malicious one.
- Off-line password guessing attacks: An attacker guesses a password and verifies his/her guess off-line. No participation of server is required, so the server does not notice the attack.

Since the first proposal of Bellovin and Merrit (PAKE) [5], many efficient key exchange protocols based on password have been developed. Recently these two Party key exchange protocols are extended to three party $[2,3,7,11,12,13,14,15$, $16,17,18]$, in which, the two parties initially communicates the passwords with the trusted server securely. Later the server authenticates the clients when they want to agree upon a session key. The 3-party protocol is introduced by Steiner et al [19]. Subsequently Ding and Hoster presented on line and offline guessing attacks on Stener's protocol [9].

Recently, Chang proposed a practical three-party key exchange (C-3 PEKE) protocol with round efficiency [8]. Later, Lee and Chang presented an Off-line password guessing attack on C-3 PEKE protocol [13]. In the present paper, an impersonation -ofthe initiator attack and impersonation-of-the responder attack are demonstrated on C-3 PEKE protocol using the off-line password guessing attack proposed by Lee and Chang.

The rest of the paper is organized as follows: Section2 briefly describes C-3 PEKE (Chang's three-party key exchange protocol) and off-line password guessing attack on C-3 PEKE protocol proposed by Lee and Chang. Section 3 demonstrates impersonation-of-initiator attack and impersonation-of-the responder attack on C-3 PEKE protocol and the concluding remarks are made in section 4.

## 2. REVIEW OF C-3 PEKE PROTOCOL

This section presents C-3 PEKE (Chang's three-party key exchange protocol).

## Notations

A,B: Communication parties
S: the trusted Server
$\mathrm{ID}_{\mathrm{A}} / \mathrm{ID}_{\mathrm{B}} / \mathrm{ID}_{\mathrm{S}}$ : the identities of $\mathrm{A} / \mathrm{B} / \mathrm{S}$
$P_{A} / P_{B}$ : the password securely shared by $A / B$ with $S$
$\mathrm{E}_{3 \mathrm{p}}()$ : a symmetric encryption scheme with a password p
$P$ : a large prime
g : an element of order q with modulus p
G : a finite cyclic group generated by g in $\mathrm{Z}_{\mathrm{P}}$
$R_{A} / R_{B}$ : the random exponents chosen by $A / B$
$\mathrm{R}_{\mathrm{S} 1} / \mathrm{R}_{\mathrm{S} 2}$ : two random exponents chosen by S
$\mathrm{N}_{\mathrm{A}}, \mathrm{N}_{\mathrm{B}}: \mathrm{N}_{\mathrm{A}}=\mathrm{g}^{\mathrm{RS} 1}$ modp, $\mathrm{N}_{\mathrm{B}}=\mathrm{g}^{\mathrm{RS} 2}$ modp
$\mathrm{N}_{\mathrm{S} 1}, \mathrm{~N}_{\mathrm{S} 2}: \mathrm{N}_{\mathrm{S} 1}=\mathrm{g}^{\mathrm{RS} 1} \operatorname{modp}, \mathrm{~N}_{\mathrm{S} 2}=\mathrm{g}^{\mathrm{RS} 2} \operatorname{modp}$
$\mathrm{f}_{\mathrm{K}}($.$) : a pseudo-random function (PRF) indexed by \mathrm{K}$
$\mathrm{K}_{\mathrm{AS}} / \mathrm{K}_{\mathrm{BS}}$ : a one-time key shared key by $\mathrm{A} / \mathrm{B}$ and S
$K_{A B}$ : a session key shared by $A$ and $B$
Step1: A selects a random number $R_{A}$ and computes $N_{A}=g^{R_{A}} \bmod p$ and the sends $I D_{A}, I D_{B}, N_{A}$ to $S$ as request.

Step2: After receiving A's request, S chooses two random numbers $\quad R_{S_{1}}, \quad R_{S_{2}}$ and computes $N_{S_{1}}=g^{R S_{1}} \bmod p$, $N_{S_{2}}=g^{R S_{2}} \bmod p$ then determines $K_{A S}=N_{A}^{R S_{1}} \bmod p=g^{R S_{1} R_{A}} \bmod p$. Then, $S \quad$ sends $\left(I D_{A}, N_{A}, E_{3 P_{A}}\left(N_{S_{1}}\right), E_{3 P_{B}}\left(N_{S_{2}}\right), f_{K_{A S}}\left(I D_{A}, I D_{B}, N_{A}\right)\right)$ to $B$

Step3: Upon receiving $S$ 's message, $B$ first decrypts $E_{3 P_{B}}\left(N_{S_{2}}\right)$ using password $p_{B}$, to get $N_{S_{2}}$. Then $B$ computes $K_{B S}=N_{S_{2}}{ }^{R_{B}} \bmod p=g^{R S_{2} R_{B}} \bmod p$ and
$K_{A B}=N_{A}^{R_{B}} \bmod p=g^{R_{A} R_{B}} \bmod p . \quad$ Next, $B \quad$ sends $\left(I D_{B}, N_{B}, E_{3 P_{A}}\left(N_{S_{1}}\right), f_{K_{A S}}\left(I D_{A}, I D_{B}, N_{A}\right)\right.$, $\left.f_{K_{A B}}\left(I D_{A}, I D_{B}, N_{A}\right), f_{K_{B S}}\left(I D_{A}, I D_{B}, N_{S_{2}}\right)\right)$ to $A$.

Step4: Upon receiving the message, $A$ first decrypts $E_{3 P_{A}}\left(N_{S_{1}}\right)$ using $P_{A}$ to get $N_{S_{1}}$. Then $A$ computes $K_{A S}=N_{S_{1}}^{R_{A}} \bmod p=g^{R S_{1} R_{A}} \bmod p \quad$ and $K_{A B}=N_{B}{ }^{R_{A}} \bmod p=g^{R_{A} R_{B}} \bmod p$. Firstly, $A$ uses $K_{A S}$ to compute $f_{K_{A S}}\left(I D_{A}, I D_{B}, N_{A}\right)$ and verifies if the computation result is equal to the received one. If it is correct, $A$ believes that he/she is communicating with a legitimate $S$; otherwise, $A$ regards $S$ illegal and terminates the protocol. Secondly, $A$ uses $K_{A B}$ to compute $f_{K_{A B}}\left(I D_{A}, I D_{B}, N_{A}\right)$ and verifies if the computation result is equal to the received one. If it is correct, $A$ believes that he/she is communicating with a legitimate $B$; otherwise, $A$ regards $B$ illegal and terminates the protocol. After authenticating $S$ and $B, A$ sends $\left(I D_{A}, I D_{B}, N_{B}, f_{K_{A S}}\left(I D_{A}, I D_{B}, N_{S_{1}}\right)\right.$,
$f_{K_{B S}}\left(I D_{A}, I D_{B}, N_{S_{2}}\right), f_{K_{A B}}\left(I D_{A}, I D_{B}, N_{B}\right)$ ) to $S$.
Step 5: Upon receiving the message, $S$ computes $K_{B S}=N_{B}^{R S_{2}} \bmod p=g^{R S_{2} R_{B}} \bmod p$. Firstly, $S$ uses $K_{A S}$ to
compute $f_{K_{A S}}\left(I D_{A}, I D_{B}, N_{S_{1}}\right)$ and verifies if the computation result is equal to the received one. If it is correct, $S$ believes that he/she is communicating with a legitimate $A$; otherwise, S regards $A$ illegal and terminates the protocol. Secondly, $S$ uses $K_{B S}$ to compute $f_{K_{B S}}\left(I D_{A}, I D_{B}, N_{S_{2}}\right)$ and verifies if the computation result is equal to the received one. If it is correct, $S$ believes that he/she is communicating with a legitimate $B$; otherwise, $S$ regards $B$ illegal and terminates the protocol. After authenticating $A \quad$ and $\quad B, \quad S \quad$ sends $\left(I D_{A}, f_{K_{A B}}\left(I D_{A}, I D_{B}, N_{B}\right), f_{K_{B S}}\left(I D_{A}, I D_{B}, N_{B}\right)\right)$ to $B$. After receiving the message, $B$ uses $K_{B S}$ to compute $f_{K_{B S}}\left(I D_{A}, I D_{B}, N_{B}\right)$ and verifies if the computation result is equal to the received one. If it is correct, $B$ believes that he/she is communicating with a legitimate $S$; otherwise, $B$ regards $S$ illegal and terminates the protocol. Next, $B$ uses $K_{A B}$ to compute $f_{K_{A B}}\left(I D_{A}, I D_{B}, N_{B}\right)$ and verifies if the computation result is equal to the received one. If it is correct, $B$ believes that he/she is communicating with a legitimate $A$; otherwise, $B$ regards $A$ illegal and terminates the protocol.

Finally, $A$ and $B$ can share the session key $K_{A B}$ to encrypt and decrypt their communicated messages. Fig 1 illustrates the C-3 PEKE protocol

## 3. OFF-LINE PASSWORD GUESSING ATTACK ON C-3 PEKE PROTOCOL

An attacker $C$ can intercept transmitted messages from public channel and then break password by playing off-line guessing attacks. $C$ can guess a password $P^{\prime}$ until the guessing $P^{\prime}$ is equal to the correct password $P$. Otherwise, $C$ repeatedly guesses a new $P^{\prime}$ off-line. Suppose that $C$ tends to get $A$ 's password $P_{A}$, then the procedure followed is:

Step1: $C$ wiretaps that $A$ and $B$ communicate with $S . C$ can intercept $I D_{A}$ and $I D_{B}$.

Step2: $C$ forges $A$ communicate with $S$. $\mathrm{He} /$ She chooses a new random number $R_{A}^{\prime}$ and computes $N_{A}^{\prime}=g^{R_{A}^{\prime}} \bmod p$. Then $C$ forges $A$ to send $\left(I D_{A}, I D_{B}, N_{A}^{\prime}\right)$ to $S$.

Step3: After receiving $C_{S}^{\prime}$ request, $S$ computes $K_{A S}=N_{A}^{\prime}{ }^{R S_{1}} \bmod p=g^{R S_{1} R_{A}^{\prime}} \bmod p$. Then, $\quad S$ sends $I D_{A}, N_{A}^{\prime}, E_{3 P_{A}}\left(N_{S_{1}}\right), E_{3 P_{B}}\left(N_{S_{2}}\right), f_{K_{A S}}\left(I D_{A}, I D_{B}, N_{A}^{\prime}\right)$ to $B$. Since $C$ wiretaps their communications, he/she can intercept $E_{3 P_{A}}\left(N_{S_{1}}\right)$ and $f_{K_{A S}}\left(I D_{A}, I D_{B}, N_{A}^{\prime}\right)$.

Step4: Once C intercepts $E_{3 P_{A}}\left(N_{S_{1}}\right)$ and $f_{K_{A S}}\left(I D_{A}, I D_{B}, N_{A}^{\prime}\right)$, he/she can play off-line guessing attacks.

Now $C$ guesses a password $P^{\prime}$. He/She first decrypts $E_{3 P_{A}}\left(N_{S_{1}}\right)$ using $P^{\prime}$. If $P^{\prime}=P_{A}$, he/she can get $N_{S_{1}}$. Then $C$ can compute $K_{A S}=N_{S_{1}}^{R_{A}^{\prime}} \bmod p=g^{R S_{1} R_{A}{ }^{\prime}} \bmod p$. Next, $C$ computes $f_{K_{A S}}\left(I D_{A}, I D_{B}, N_{A}^{\prime}\right)$ and verifies if the computation result is equal to the intercepted one. If it is correct, $C$ believes that he/she had guessed a correct password $P_{A}^{\prime}$; otherwise, $C$ repeatedly guesses a new $P^{\prime}$ off-line till $C$ can guess a correct password $P_{A}$. In the same way, $C$ can get $B$ 's password $P_{B}$.

## 4. IMPERSONATION- OF- THEINITIATOR ATTACK

This section presents an impersonation-of-initiator attack on Chang's three-party key exchange protocol C-3PEKE. Fig 2 illustrates the impersonation-of-initiator attack.

Step1: C selects a random number $R_{C}$ and computes $N_{C}=g^{R_{C}} \bmod p$ and sends $\left(I D_{A}, I D_{B}, N_{C}\right)$ to $S($ as $A)$ as request.

Step2: After receiving $A$ 's request, $S$ chooses two random numbers $\quad R_{S_{1}}, R_{S_{2}} \quad$ and $\quad$ computes $\quad N_{S_{1}}=g^{R S_{1}} \bmod p$, $N_{S_{2}}=g^{R S_{2}} \bmod p$ then determines $K_{C S}=N_{C}{ }^{R S_{1}} \bmod p=g^{R S_{1} R_{C}} \bmod p . \quad$ Then, $\quad S \quad$ sends $\left(I D_{A}, N_{C}, E_{3 P_{A}}\left(N_{S_{1}}\right), E_{3 P_{B}}\left(N_{S_{2}}\right), f_{K_{C S}}\left(I D_{A} \cdot I D_{B}, N_{C}\right)\right)$ to B.

Step3: $\quad B$ selects a random number $R_{B}$ and computes $N_{B}=g^{R_{B}} \bmod p$. Upon receiving $S$ 's message, $B$ first decrypts $E_{3 P_{B}}\left(N_{S_{2}}\right)$ using password $P_{B}$, to get $N_{S_{2}}$. Then $B \quad$ computes $\quad K_{B S}=N_{S_{2}}^{R_{B}} \bmod p=g^{R S_{2} R_{B}} \bmod p \quad$ and $K_{C B}=N_{C}^{R_{B}} \bmod p=g^{R_{C} R_{B}} \bmod p . \quad$ Next, $B \quad$ sends $\left(I D_{B}, N_{B}, E_{3 P_{A}}\left(N_{S_{1}}\right), f_{K_{C S}}\left(I D_{A} \cdot I D_{B}, N_{C}\right), f_{K_{C B}}\left(I D_{A} \cdot I D_{B}, N_{C}\right)\right.$, $f_{K_{B S}}\left(I D_{A} \cdot I D_{B}, N_{S_{2}}\right)$ to A.

Step4: $C$ intercepts this message, upon receiving the message, $C$ first decrypts $E_{3 P_{A}}\left(N_{S_{1}}\right)$ using $P_{A} \quad\left(P_{A}\right.$ is already determined as shown in section $2(A))$ to get $N_{S_{1}}$. Then $C$ computes $\quad K_{C S}=N_{S_{1}}^{R_{C}} \bmod p=g^{R S_{1} R_{C}} \bmod p \quad$ and $K_{C B}=N_{B}{ }^{R_{C}} \bmod p=g^{R_{B} R_{C}} \bmod p$ Firstly, $A$ uses $K_{C S}$ to compute $f_{K_{C S}}\left(I D_{A}, I D_{B}, N_{C}\right)$ and verifies if the computed result is equal to the received one. If it is correct, $C$ believes that he/she is communicating with a legitimate $S$; otherwise, $C$ regards $S$ illegal and terminates the protocol. Secondly, $C$ uses $K_{C B}$ to compute $f_{K_{C B}}\left(I D_{A}, I D_{B}, N_{C}\right)$ and verifies if the computation result is equal to the received one. If it is correct, $C$ believes that he/she is communicating with a legitimate $B$; otherwise, $C$ regards $B$ illegal and terminates the protocol. After authenticating $S$ and $B, \quad C$ sends $\left(I D_{A}, I D_{B}, N_{B}, f_{K_{C S}}\left(I D_{A}, I D_{B}, N_{S_{1}}\right)\right.$, $\left.f_{K_{B S}}\left(I D_{A}, I D_{B}, N_{S_{2}}\right), f_{K_{C B}}\left(I D_{A}, I D_{B}, N_{B}\right)\right)$ to $S$.

Step 5: Upon receiving the message, $S$ computes $K_{B S}=N_{B}{ }^{R S_{2}} \bmod p=g^{R S_{2} R_{B}} \bmod p$. Firstly, $S$ uses $K_{C S}$ to compute $f_{K_{C S}}\left(I D_{A}, I D_{B}, N_{S_{1}}\right)$ and verifies if the computation result is equal to the received one. If it is correct, $S$ believes that he/she is communicating with a legitimate A (But $S$ is actually communicating with $C$ ); otherwise, $S$ regards $A$ illegal and terminates the protocol. Secondly, $S$ uses $K_{B S}$ to compute $f_{K_{B S}}\left(I D_{A}, I D_{B}, N_{S_{2}}\right)$ and verifies if the computation result is equal to the received one. If it is correct, $S$ believes that he/she is communicating with a legitimate $B$; otherwise, $S$ regards $B$ illegal and terminates the protocol. After authenticating $A$ and $B, \quad S$ sends $\left(I D_{A}, f_{K_{C B}}\left(I D_{A}, I D_{B}, N_{B}\right), f_{K_{B S}}\left(I D_{A}, I D_{B}, N_{B}\right)\right)$ to $B$. After receiving the message, $B$ uses $K_{B S}$ to compute $f_{K_{B S}}\left(I D_{A}, I D_{B}, N_{B}\right)$ and verifies if the computation result is equal to the received one. If it is correct, $B$ believes that he/she is communicating with a legitimate $S$; otherwise, $B$ regards $S$ illegal and terminates the protocol. Next, $B$ uses $K_{C B}$ to compute $f_{K_{C B}}\left(I D_{A}, I D_{B}, N_{B}\right)$ and verifies if the computation result is equal to the received one. If it is correct, $B$ believes that he/she is communicating with a legitimate $A$ (But $B$ is communicating with $C$ ); otherwise, $B$ regards $A$ illegal and terminates the protocol.

Finally, $C$ and $B$ can share the session key $K_{C B}$ to encrypt and decrypt their communicated messages. $B$ is thinking that it is communicating with $A$ but actually it is communicating with $C$.

## 5. IMPERSONATION- OF- THE RESPONDER ATTACK

This section presents an impersonation-of-the responder attack on C-3PEKE (Chang's three-party key exchange protocol). Fig 3 illustrates the above attack.

Step1: A selects a random number $R_{A}$ and computes $N_{A}=g^{R_{A}} \bmod p$ and the sends $\left(I D_{A}, I D_{B}, N_{A}\right)$ to $S$ as request.

Step2: After receiving $A$ 's request, $S$ chooses two random numbers $\quad R_{S_{1}}, R_{S_{2}} \quad$ and $\quad$ computes $N_{S_{1}}=g^{R S_{1}} \bmod p$, $N_{S_{2}}=g^{R S_{2}} \bmod p$
then
determines $K_{A S}=N_{A}^{R S_{1}} \bmod p=g^{R S_{1} R_{A}} \bmod p$. Then, S sends $\left(I D_{A}, N_{A}, E_{3 P_{A}}\left(N_{S_{1}}\right), E_{3 P_{B}}\left(N_{S_{2}}\right), f_{K_{A S}}\left(I D_{A} \cdot I D_{B}, N_{A}\right)\right)$ to B.

Step3: $C$ selects a random number $R_{C}$ and computes $N_{C}=g^{R_{C}} \bmod p$. Upon receiving $S$ 's message, $C$ first decrypts $E_{3 P_{B}}\left(N_{S_{2}}\right)$ using password $P_{B}$, (password of $B$ is obtained by $C$ as shown in section $2(A)$ ) to get $N_{S_{2}}$. Then $C$ computes $\quad K_{C S}=N_{S_{2}}^{R_{C}} \bmod p=g^{R S_{2} R_{C}} \bmod p \quad$ and $K_{A C}=N_{A}^{R_{C}} \bmod p=g^{R_{A} R_{C}} \bmod p . \quad$ Next, $C \quad$ sends $\left(I D_{B}, N_{C}, E_{3 P_{A}}\left(N_{S_{1}}\right), f_{K_{A S}}\left(I D_{A} \cdot I D_{B}, N_{A}\right)\right.$, $f_{K_{A C}}\left(I D_{A} \cdot I D_{B}, N_{A}\right), f_{K_{C S}}\left(I D_{A} \cdot I D_{B}, N_{S_{2}}\right)$ ) to A.

Step4: Upon receiving the message, $A$ first decrypts $E_{3 P_{A}}\left(N_{S_{1}}\right)$ using $\quad P_{A}$ to get $N_{S_{1}}$. Then $A$ computes $K_{A S}=N_{S_{1}}^{R_{A}} \bmod p=g^{R S_{2} R_{A}} \bmod p \quad$ and $K_{A C}=N_{C}{ }^{R_{A}} \bmod p=g^{R_{A} R_{C}} \bmod p$ Firstly, $A$ uses $K_{A S}$ to compute $f_{K_{A S}}\left(I D_{A}, I D_{B}, N_{A}\right)$ and verifies if the computation result is equal to the received one. If it is correct, $A$ believes that he/she is communicating with a legitimate $S$; otherwise, $A$ regards $S$ illegal and terminates the protocol. Secondly, $A$ uses $K_{A C}$ to compute $f_{K_{A C}}\left(I D_{A}, I D_{B}, N_{A}\right)$ and verifies if the computation result is equal to the received one. If
it is correct, $A$ believes that he/she is communicating with a legitimate $B$ (But actually $A$ is communicating with $C$ ); otherwise, $A$ regards $B$ illegal and terminates the protocol. After authenticating $\quad S \quad$ and $\quad B$, $A \quad$ sends $\left(I D_{A}, I D_{B}, N_{C}, f_{K_{A S}}\left(I D_{A}, I D_{B}, N_{S_{1}}\right)\right.$, $\left.f_{K_{C S}}\left(I D_{A}, I D_{B}, N_{S_{2}}\right), f_{K_{A C}}\left(I D_{A}, I D_{B}, N_{C}\right)\right)$ to S.

Step 5: Upon receiving the message, $S$ computes $K_{C S}=N_{C}{ }^{R S_{2}} \bmod p=g^{R S_{2} R_{C}} \bmod p$. Firstly, $S$ uses $K_{A S}$ to compute $f_{K_{A S}}\left(I D_{A}, I D_{B}, N_{S_{1}}\right)$ and verifies if the computation result is equal to the received one. If it is correct, S believes that he/she is communicating with a legitimate $A$; otherwise, $S$ regards $A$ illegal and terminates the protocol. Secondly, $S$ uses $K_{C S}$ to compute $f_{K_{C S}}\left(I D_{A}, I D_{B}, N_{S_{2}}\right)$ and verifies if the computation result is equal to the received one. If it is correct, $S$ believes that he/she is communicating with a legitimate $B$ (But S is actually communicating with $C$ ); otherwise, $S$ regards $B$ illegal and terminates the protocol. After authenticating $A$ and $B, \quad S \quad$ sends $\left(I D_{A}, f_{K_{A B}}\left(I D_{A}, I D_{B}, N_{B}\right), f_{K_{B S}}\left(I D_{A}, I D_{B}, N_{B}\right)\right)$ to B. C intercepts this message. After receiving the message, $C$ uses $K_{C S}$ to compute $f_{K_{C S}}\left(I D_{A}, I D_{B}, N_{C}\right)$ and verifies if the computation result is equal to the received one. If it is correct, $C$ believes that he/she is communicating with a legitimate $S$; otherwise, $C$ regards S illegal and terminates the protocol. Next, $C$ uses $K_{A C}$ to compute $f_{K_{A C}}\left(I D_{A}, I D_{B}, N_{C}\right)$ and verifies if the computation result is equal to the received one. If it is correct, $C$ believes that he/she is communicating with a legitimate $A$; otherwise, $C$ regards $A$ illegal and terminates the protocol.

Finally, $A$ and $C$ can share the session key $K_{A C}$ to encrypt and decrypt their communicated messages. $A$ believes that it is communicating with B but actually it is communicating with $C$.

## 6. CONCLUSION

The key exchange protocol using passwords achieved great attention due to its simplicity and efficiency. Recently, Chang proposed a practical three-party key exchange (C-3 PEKE) protocol with round efficiency. Later, Lee and Chang presented an
off-line password guessing attack on C-3 PEKE protocol. In the present paper, an impersonation-of-the initiator attack and impersonation-of-the responder attack are demonstrated on C-3 PEKE protocol using the off-line password guessing attack proposed by Lee and Chang.

Fig 1: C-3 PEKE protocol
A
S
B

Choose $R_{A}$
Choose $R_{S_{1}}, R_{S_{2}}$
Compute $N_{A}=g^{R_{A}} \bmod p$
Compute $N_{S_{1}}=g^{R S_{1}} \bmod p$
Choose $R_{B}$

Compute $N_{S_{2}}=g^{R S_{2}} \bmod p$
$\xrightarrow{I D_{A}, I D_{B}, N_{A}}$

$$
K_{A S}=N_{A}^{R S_{1}} \bmod p=g^{R S_{1} R_{A}} \bmod p
$$

$$
\xrightarrow{\left(I D_{A}, N_{A}, E_{3 P_{A}}\left(N_{S_{1}}\right), E_{3} P_{B}\left(N_{S_{2}}\right), f_{K_{A S}}\left(I D_{A}, I D_{B}, N_{A}\right)\right)}
$$

$\operatorname{Decrypt} E_{3 P_{B}}\left(N_{S_{2}}\right)$, get $N_{S_{2}}$
Compute $K_{B S}=N_{S_{2}}{ }^{R_{B}} \bmod p=g^{R S_{2} R_{B}} \bmod p$

$$
K_{A B}=N_{A}^{R_{B}} \bmod p=g^{R_{A} R_{B}} \bmod p
$$

$$
\stackrel{I D_{B}, N_{B}, E_{3 P_{A}}\left(N_{S_{1}}\right), f_{K_{A S}}\left(I D_{A}, I D_{B}, N_{A}\right), f_{K_{A B}}\left(I D_{A}, I D_{B}, N_{A}\right), f_{K_{B S}}\left(I D_{A}, I D_{B}, N_{S_{2}}\right)}{\leftarrow}
$$

Decrypt $E_{3 P_{B}}\left(N_{S_{1}}\right)$, get $N_{S_{1}}$
$K_{A S}=N_{S_{1}}{ }^{R_{A}} \bmod p=g^{R S R_{A}} \bmod p$
$K_{A B}=N_{B}{ }^{R_{A}} \bmod p=g^{R_{A} R_{B}} \bmod p$
verify $f_{K_{A S}}\left(I D_{A}, I D_{B}, N_{A}\right)$,

## (A authenticates $S$ )

verify $f_{K_{A B}}\left(I D_{A}, I D_{B}, N_{A}\right)$,
( $A$ authenticates $B$ )

$$
\xrightarrow{I D_{A}, I D_{B}, N_{B}, f_{K_{A S}}\left(I D_{A}, I D_{B}, N_{S_{1}}\right), f_{K_{B S}}\left(I D_{A}, I D_{B}, N_{S_{2}}\right), f_{K_{A B}}\left(I D_{A}, I D_{B}, N_{B}\right)}
$$

$$
K_{B S}=N_{B}^{R S_{2}} \bmod p=g^{R S_{2} R_{B}} \bmod p
$$

$$
\text { Verify } f_{K_{A S}}\left(I D_{A}, I D_{B}, N_{S_{1}}\right)
$$

( $S$ authenticates $A$ )
Verify $f_{K_{B S}}\left(I D_{A}, I D_{B}, N_{S_{2}}\right)$,
(S authenticates B)
$\xrightarrow[I D_{A}, f_{K_{A B}}\left(I D_{A}, I D_{B}, N_{B}\right), f_{K_{B S}}\left(I D_{A}, I D_{B}, N_{B}\right)]{ }$
Verify $f_{K_{B S}}\left(I D_{A}, I D_{B}, N_{B}\right)$
( $B$ authenticates $S$ )
Verify $f_{K_{A B}}\left(I D_{A}, I D_{B}, N_{B}\right)$
( $B$ authenticates $A$ )
$K_{A B}$ is the final key through which $A$ and $B$ communicates

Fig 2: Impersonation of the initiator attack on C-3PEKE protocol
Attacker(C)
S
B

Choose $R_{C}$
Compute $N_{C}=g^{R_{C}} \bmod p$

Choose $R_{S_{1}}, R_{S_{2}}$
Compute $N_{S_{1}}=g^{R S_{1}} \bmod p$ Compute $N_{S_{2}}=g^{R S_{2}} \bmod p$

$$
\xrightarrow{\left(I D_{A}, I D_{B}, N_{C}\right)}
$$

$$
\begin{gathered}
K_{C S}=N_{C}{ }^{R S_{1}} \bmod p=g^{R S_{1} R_{C}} \bmod p \\
\xrightarrow{\left(I D_{A}, N_{C}, E_{3 P_{A}}\left(N_{S_{1}}\right), E_{3} P_{B}\left(N_{S_{2}}\right), f_{K_{C S}}\left(I D_{A} \cdot I D_{B}, N_{C}\right)\right)} \\
\text { Decrypt } E_{3 P_{B}}\left(N_{S_{2}}\right) \text {, get } N_{S_{S_{2}}} \\
\text { Compute } K_{B S}=N_{S_{2}}{ }^{R_{B}} \bmod p=g^{R S_{2} R_{B}} \bmod p \\
K_{C B}=N_{C}^{R_{B}} \bmod p=g^{R_{C} R_{B}} \bmod p \\
\stackrel{I D_{B}, N_{B}, E_{3 P_{A}}\left(N_{S_{1}}\right), f_{K_{C S}}\left(I D_{A} \cdot I I_{B}, N_{C}\right), f_{K_{C B}}\left(I D_{A} \cdot I D_{B}, N_{C}\right), f_{K_{B S}}\left(I D_{A} \cdot I D_{B}, N_{S_{2}}\right)}{\longrightarrow}
\end{gathered}
$$

(Since password of $A$ i.e. $P_{A}$ is already

## determined as shown in section 2(A))

Decrypt $E_{3 P_{A}}\left(N_{S_{1}}\right)$, get $N_{S_{i}}$
$K_{C S}=N_{S_{1}}{ }^{R_{C}} \bmod p=g^{R S S_{C} R_{C}} \bmod p$
$K_{C B}=N_{B}{ }^{R_{C}} \bmod p=g^{R_{C} R_{B}} \bmod p$
verify $f_{K_{C S}}\left(I D_{A}, I D_{B}, N_{C}\right)$,
( $A$ authenticates $S$ )
verify $f_{K_{C B}}\left(I D_{A}, I D_{B}, N_{C}\right)$,
( $C$ authenticates $B$ )
$\xrightarrow{I D_{A}, I D_{B}, N_{B}, f_{K_{C S}}\left(I D_{A}, I D_{B}, N_{S_{1}}\right), f_{K_{B S}}\left(I D_{A}, I D_{B}, N_{S_{2}}\right), f_{K_{C B}}\left(I D_{A}, I D_{B}, N_{B}\right)}$
$K_{B S}=N_{B}{ }^{R S_{2}} \bmod p=g^{R S_{2} R_{B}} \bmod p$
Verify $f_{K_{C S}}\left(I D_{A}, I D_{B}, N_{S_{1}}\right)$,
(S authenticates $A$ (but it is actually $C$ ))
Verify $f_{K_{B S}}\left(I D_{A}, I D_{B}, N_{S_{2}}\right)$,
( $S$ authenticates $B$ )

$$
\xrightarrow{I D_{A}, f_{K C B}\left(I D_{A}, I D_{B}, N_{B}\right), f_{K_{B S}}\left(I D_{A}, I D_{B}, N_{B}\right)}
$$

Verify $f_{K_{B S}}\left(I D_{A}, I D_{B}, N_{B}\right)$

Verify $f_{K_{C B}}\left(I D_{A}, I D_{B}, N_{B}\right)$
$K_{C B}$ is the final key trough which $C$ and $B$ communicates
$B$ thinks that it is communicating with $A$ but it is actually communicating with $C$ (attacker).

Fig 3: Impersonation-of-responder attack on C-3PEKE protocol


Decrypt $E_{3 P_{A}}\left(N_{S_{1}}\right)$, get $N_{S_{1}}$
$K_{A S}=N_{S_{1}}{ }^{R_{A}} \bmod p=g^{R S_{2} R_{A}} \bmod p$
$K_{A C}=N_{C}{ }^{R_{A}} \bmod p=g^{R_{A} R_{C}} \bmod p$
verify $f_{K_{A S}}\left(I D_{A}, I D_{B}, N_{A}\right)$,
( $A$ authenticates $S$ )
verify $f_{K_{A C}}\left(I D_{A}, I D_{B}, N_{A}\right)$,

## ( $A$ authenticates $B$ )

(But it is actually $C$ )

$$
\xrightarrow{I D_{A}, I D_{B}, N_{C}, f_{K_{A S}}\left(I D_{A}, I D_{B}, N_{S_{1}}\right), f_{K_{C S}}\left(I D_{A}, I D_{B}, N_{S_{2}}\right), f_{K_{A C}}\left(I D_{A}, I D_{B}, N_{C}\right)}
$$

$K_{C S}=N_{C}{ }^{R S_{2}} \bmod p=g^{R S_{2} R_{C}} \bmod p$
Verify $f_{K_{A S}}\left(I D_{A}, I D_{B}, N_{S_{1}}\right)$
( $S$ authenticates $A$ )
Verify $f_{K_{C S}}\left(I D_{A}, I D_{B}, N_{S_{2}}\right)$,
( $S$ authenticates $B$ )
(But it is actually $C$ )
$\xrightarrow{I D_{A}, f_{K_{A C}}\left(I D_{A}, I D_{B}, N_{B}\right), f_{K_{C S}}\left(I D_{A}, I D_{B}, N_{B}\right)}$
Verify $f_{K_{C S}}\left(I D_{A}, I D_{B}, N_{C}\right)$
( $C$ authenticates $S$ )
Verify $f_{K_{A C}}\left(I D_{A}, I D_{B}, N_{C}\right)$
( $C$ authenticates $A$ )
$K_{A C}$ is the final key through which $A$ and $B$ communicates

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