# 3D Reconstruction using Interactive Shape from Shading 

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#### Abstract

The Shape-From-Shading (SFS) problem is a fundamental and classical problem in computer vision. It is the process of computing three dimensional shape of a surface using its shading information from single image. In this paper, a new method for interactive shape from shading for reconstruction of a 3D shape is presented. Experimental results on several synthetic and real object images show that the proposed method reconstructs the 3D surface of objects very efficiently.


## General Terms

Shape from Shading (SfS), Fast Marching Algorithm (FMA).

## Keywords

3D Lambertian, user interactive, module.

## 1. INTRODUCTION

The 3D modeling is an interesting subject in computer graphics and image processing because of its wide applications in various fields such as model based compression coding, and computer assisted medical diagnosis and treatment. A single or more images can be used to obtain 3Dmodel of an object, taken simultaneously from different points of view (Stereo) or over a period of time (Video). Single image techniques rely on shading information, while multiple image techniques tend to use corresponding points and the parameters of the camera projection. To calculate depth information, most systems using a single image never use explicit 3D information to assist the modeling. Little work has been done to deal with the problem of 3Dmodeling of an object from a single image. The fine areas of these surfaces appear on the image as a variation of shading (depending on the object's material). The methods that recover these features from the shading are called Shape-from-Shading (SfS), which is one of the attractive research fields in computer vision [1, 2, 3].
SfS deals with the recovery of surface orientation and surface shape (highlight) from the gradual variation of shading in images. SfS is implemented by first modeling the image brightness as a function of surface geometry and then reconstructing a surface which, under the given imaging model, generates an image close to the input image. This field was formally introduced by Horn [4] and there have been many significant improvements in both theoretical and practical aspects of the problem. However, it has been shown that this is an ill-posed problem [5, 6].

In this paper, we present an interactive shape from shading algorithm and show how it can be used for different materials. The aim is to retain the robustness and flexibility of using a user
interactive model for constructing a 3D surface from a single image. Furthermore the proposed approach supports computer graphics applications, such as:

- medical applications,
- gaming,
- image-based crime investigation, and
- recognition applications.

In this paper, we introduce an interactive shape from shading method for estimating the surface of 3D shapes. The remaining of this paper is organized as follows. Section 2 discusses some of the works related to our algorithm and lists the main advantages and limitations of each work. In section 3 we reveal our proposed interactive algorithm for shape from shading and the main steps of implementing it in computer graphics. Section 4 is dedicated for testing and validating our proposed algorithm of various 3D objects. The last section concludes this paper.

## 2. RELATED WORKS

There are two ways to recover shape from a single image namely shape from shading and user interactive modeling [7]. The non-interactive methods compute depth based on the work proposed by Horn and Brook. This is done by minimizing the Eikonal equation and presenting the solution as computed depth. In the interactive method, the depth map obtained is interactively modified by the user in order to get more accurate results. Zhang et al. [1] classified shape from shading methods into four groups viz. minimization, propagation, local and linear methods. Zhang et al. implemented 6 -well known algorithms and compared them objectively based on COP time and error. Although each algorithm works well with specific image, but produces poor results with others. In another work Durou et al. [2] classified shape from shading methods into three classes: minimization approaches, approximation approaches and partial differential equation based approaches. Patel and Smith [8] used a morphable model for shape from shading of non-Lambertian surfaces. Sheta et al. [9] proposed the use of genetic algorithm for solving shape from shading as minimization problem. Genetic algorithm provides efficient minimization compared to the traditional minimization approaches. Shlizerman and Basri [10] used the similarity between faces for 3D reconstruction. Common face features such as location of eyes, aspect ratio and the location of nose can vary between different races, gender or because of facial expressions. Using previously stored features their proposed algorithm guides the reconstruction of the face using information about the subject race, gender and facial expressions.

All the previous works are examples for non-interactive shape from shading. However, non-interactive method does not always produce satisfactory results especially in severe lighting condition. Because of this, interactive methods are used instead. Zeng et al. [7] proposed an interactive face reconstruction using shape from shading. They divided the face into smaller patches and estimated the surface of each patch by minimizing the patch energy function after smoothing it using fast marching method. The user interactively selects different points as new patch and the Voronoi method is used for segmenting each patch. Then the standard shape from shading method is processed for each patch. Meryer et al. [4] used an interactive model for shape from shading. Firstly the algorithm detects flat regions in the image which are the regions with highlights. Then the user interactively select whether these regions represent peaks or valleys. The depth of other points between peaks and valley is computed using mass-spring interpolation. This process is repeated until the user is satisfied with the resultant image.

## 3. PROPOSED METHOD

Figure 1 shows our proposed interactive shape from shading framework. It starts with extracting the luminance from the image. Next, the depth gradient is computed from the luminance. Then, fast marching algorithm is used to smooth the computed depth map. The user interactive module interactively selects the regions with wrong depth estimation and helps in correcting it.


Fig 1: Interactive shape from shading framework.

### 3.1 Luminance Extraction Module

The purpose of this module is to extract the luminance value by computing the shading image from the RGB colored image. The luminance represents the lighting component of the image. From an RGB image, the luminance is computed using the following equation [11, 12]:

Luminance_value $=0.3 R+0.59 G+0.11 B$

### 3.2 Depth Gradient Formulation Module

The first step in depth gradient computation module is to solve the Eikonal equation which represents the luminance value as the inner product between surface normal and light source direction. In this work, we assume a vertical light source whose direction is the same as the viewing direction. This means, we only need to compute the surface normal that represents the image luminance. The surface normal is proportional to the depth gradient of the surface. Therefore the Eikonal equation (Eq. 2) [7] gives the relationship between light source direction and depth gradient in luminance value.

$$
\begin{equation*}
\left\|\nabla Z_{(x, y)}\right\|=\sqrt{I_{(x, y)}^{-2}-1} \tag{2}
\end{equation*}
$$

### 3.3 Fast Marching Algorithm Module

The Eikonal equation can be solved by the numerical algorithm called fast marching algorithm [4, 7]. The fast marching algorithm can be summarized in the following steps:

- At initialization, all pixel altitudes $\mathrm{Z}_{(\mathrm{X}, \mathrm{Y})}$ are set to infinity beside few pixels whose altitude are known.
- All known pixels are put into a priority queue ordered by their altitude, smaller altitude first.
- The algorithm extracts pixels from the priority queue until it is empty.
- Starting from a known pixel, the altitude of its four connected neighbors is updated and added to the queue.
The altitude $\mathrm{Z}_{(\mathrm{X}, \mathrm{Y})}$ of pixel $\mathrm{p}_{(\mathrm{x}, \mathrm{y})}$ is updated as follows [4]:

$$
\left.\begin{array}{lc}
\text { Let } z_{1}=\min \left(z_{(x-1, y)}, z_{(x+1, y)}\right) \\
\text { and } & z_{2}=\min \left(z_{(x, y-1)}, z_{(x, y+1)}\right) \\
\text { if } & \left|z_{1}-z_{2}\right|<\left\|\nabla z_{(x, y)}\right\|  \tag{3}\\
\text { then } & z_{(x, y)}=\frac{z_{1}+z_{2}+\sqrt{2 \times \nabla z_{(x, y)}^{2}-\left(z_{1}-z_{2}\right)^{2}}}{2} \\
\text { else } \quad z_{(x, y)}=\min \left(z_{1}, z_{2}\right)+\left\|\nabla z_{(x, y)}\right\|
\end{array}\right\}
$$

### 3.4 User Interactive Module

After displaying the results obtained by the fast marching method, regions that have wrong depth map are selected by the user. It has been found that these are regions that have very bright or very dark colors. These regions are segmented based on the mean intensity value. Bright and dark regions are naturally peaks or valleys on the surface of the shape. Therefore, a suitable depth will be assigned to these regions based on the status of its neighboring regions. Figure 2 shows a flow diagram of the user interactive module. Firstly the user identifies a polygonal region to represent the region of problem. Then the threshold is computed using Otsu's method and the region is
threshoded accordingly. The threshoding process creates a mask for the region of interest. Finally the depth of the region is corrected using information from neighboring regions. For example, if the depth of the neighboring regions exhibits a decaying pattern, then this region will be considered as a valley. Thus it has a depth less than the neighbors. And if the neighboring regions exhibit an increasing depth pattern, then the region will be considered as a peak. Thus, it will have depth value larger than it neighbors. It has to be noted that the selected region should be small enough so that it can have a constant depth value.


Fig 2: User interactive module.

## 4. Result and Implementation

### 4.1 Input module

In this paper, a single RGB image of three different materials, ceramic (Cup), plastic (Toy), and plants (Apple) have been used as input data (Fig. 3) to validate the proposed method.


Fig 3: Input data, (a) Ceramic, (b) Plastic, (c) Plant.

### 4.2 Luminance extraction module

Eq. 1 was used to convert the input RGB image to shading image and to keep the luminance value. Fig. 4 illustrates the luminance images of the input images.


### 4.3 Depth gradient formulation module

Fig. 5 demonstrates the depth of the highlighted regions computed by using Eq. 2. These highlighted regions are represented by the blue color.


Fig 5: Depth gradient (blue color), (a) Ceramic, (b) Plastic, (c) Plant.

### 4.4 Fast marching algorithm module

Fast marching algorithm is used to smooth the computed depth map by computing new pixel depths of the initial computed pixel depths in the previous step by using Eq. 3. The new pixel depths computed using fast marching algorithm is represented by red color in Fig. 6.


Figure 6: New pixel depth after applying fast marching algorithm, (a) Ceramic, (b) Plastic, (c) Plant.

### 4.5 Display module

This module is used to display the 3 D reconstructed surface. Fig. 7 illustrates the 3D surfaces of the RGB images.

The reconstructed surfaces (Fig 7) of the cup in column (a) and toy in column (b) are satisfactory but not the reconstructed surface of apple in column(c) because it has some problem as shown clearly in the last image.


Fig 9. Reconstructed surface of apple after applying user interactive module.

### 4.7 Comparative study

In order to assess the proposed approach with the other existing approaches of 3D reconstruction using SfS, Table 1 demonstrates a comparison between the proposed approach and existing approaches. Further, Table 1 shows that the proposed approach has achieved acceptable degree of success with less processing time and unlimited image size compared to existing approaches.

Table 1. compertive study

| Approach | $\begin{gathered} \text { Tsai } \\ \text { and } \\ \text { Shah } \\ (1994) \end{gathered}$ | Gang <br> Zeng et <br> al. <br> (1995) | Meyer et al. (2007) | Proposed approach (2011) |
| :---: | :---: | :---: | :---: | :---: |
| Technique | SfS | SfS | SfS | SfS |
| No. of input images | 1 | 1 | 1 | 1 |
| Size of image | $\begin{gathered} 128 \times 12 \\ 8 \end{gathered}$ | $\begin{gathered} 300 \times 30 \\ 0 \end{gathered}$ | 300x200 | $\begin{aligned} & \text { Unlimited } \\ & (1 \times 1) \end{aligned}$ |
| $\begin{gathered} \text { User } \\ \text { interactive } \end{gathered}$ | x | $\checkmark$ | $\checkmark$ | $\checkmark$ |
| $\begin{gathered} \hline \text { Processing } \\ \text { time } \\ \text { (Second) } \end{gathered}$ | 2 | - | 30 | 0.57 |
| Limitation | at the brighte st points and darkne ss points | at the brighte st points | some kinks at the surface junctions during the process | Extremely Shining objects (e.g. Stainless St eel objects) |

## 5. CONCLUSION

In this paper, we have presented a novel approach for reconstructing 3D surfaces of object from a single image through the use of shading information. The aim is to retain the robustness and flexibility of using a user interactive model for constructing 3D surfaces from a single image. Furthermore the proposed approach supports computer graphics applications, such as medical applications, and recognition applications.

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