# Generating Boolean SAT based Test Pattern Generation using Multi-objective Genetic Algorithm

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## ABSTRACT

This paper presents a brief introduction to multi-objective genetic algorithms and FPGAs[5][9]. In this paper we have discussed that how test pattern generation method can be formulated in terms of CNF form [2]and this CNF form can be used to generate test patterns using genetic algorithm. We have proposed that by applying a multi-objective genetic algorithm on this CNF form we can increase number of instances to satisfy boolean equation.

#### **Keywords**

FPGAs, CNF, Multi-objective Algorithm

### **1. INTRODUCTION**

#### 1.1 Multi-objective Genetic Algorithm

In general, a multi-objective optimization is defined by a function f which maps a vector of decision variables, the so-called decision vector, to a vector of objective values, the so-called objective vector:

$$(y_1, y_2, \ldots, y_n) = f(x_1, x_2, \ldots, x_n)$$

#### **Equation No:1**

where  $y_1, y_2, \ldots, y_n$  are decision vector variables,  $x_1, x_2, \ldots, x_n$  are objective values

Without loss of generality, it is assumed here and in the following that each of the n components of the objective vector is to be maximized[9][11]. In this scenario, a solution (defined by the corresponding decision vector) can be better, worse, equal, but also indifferent to another solution with respect to the objective values "Better" means a solution is not worse in any objective and at least better in one objective than another; the superior solution is also said to dominate the inferior one. Using this concept one can define what an optimal solution is: a solution which is not dominated by any other solution in the search space. Such a solution is called Pareto optimal, and the entire set of optimal trade-offs is called the Pareto-optimal set[4]. The concept of Pareto optimality is only the first step in solving a multiobjective optimization problem because at the end, a single solution is sought[5][9][11] Therefore a decision making process is necessary in which preference information is used in order to select an appropriate trade-off. Although there are different ways of integrating this process, in the field of evolutionary multiobjective optimization it is usually assumed that

optimization takes places before decision making. That is the goal to find or approximate the Pareto-optimal set[5].

# 2. Field Programmable Gate Array (FPGA)

Field Programmable Gate Arrays (FPGAs) feature their ability to be configured in the field to implement an arbitrary desired function according to the real-time demands. This ability of FPGAs can help people to achieve a faster design cycle, lower development costs and a reduced time-to market compared to conventional Application-Specific Integrated Circuits (ASICs). FPGAs, therefore, are widely used in many applications such as networking, storage systems, communication, and adaptive computing.

Testing FPGAs requires solutions different from those applicable to ASICs. In literatures, there are several different FPGA testing strategies.

- The first strategy is based on configuring several application vectors developed specifically for each circuit and supplied by an external tester[8]
- The second strategy of external testing techniques exploits regular internal structure and reconfigurability of an FPGA to concurrently examine its individual components configurable logic blocks (CLBs) and interconnects[10]
- The third strategy of testing techniques for FPGA is based on the concept of Built-In Self-Test (BIST)[14][15].

#### 2.1 Types of faults in FPGA

A static RAM based FPGA is composed of a two-dimensional array of configurable logic blocks (CLBs), programmable interconnects, and programmable input/output blocks (IOBs). To realize a specific user-given application on a FPGA chip, a compiler software provided by the FPGA vendor is required to divide the application into several parts with each of them small enough to be fit in a CLB, implement each part in a CLB, and finally connect all used CLBs through a programmed interconnect network[16]. Only if all the programmable resources of the FPGA chip used by the application configuration function correctly, the application can run well on the chip. In order to discuss the application-dependent FPGA testing, it is important to give some detailed information about the fault models widely • used and studied in FPGA testing[14][17].

**Bridging Fault:** The fault represents a short between groups of signals. The logic value of the shorted net may be modeled as

1-dominant (OR bridge), 0-dominant (AND bridge), or indeterminate, depending upon the technology used in circuit. In FPGAs, bridging faults are the most common failure mode in interconnects.

**Stuck-at Fault:** The fault is modeled by assigning a fixed (0 or 1) value to a signal line in the circuit and its most popular form are the single stuck-at faults. It is one of the significant failure modes happened in interconnects [4].

Delay Fault: The fault causes the combinational delay of a circuit to exceed clock period. Because the delays caused by interconnection can account for 70% of the FPGA clock cycle period and the programmable interconnects are the primary source of large variations in propagation delays, testing for delay faults in FPGAs should focus on excessive delays in the interconnect network. The C-exhaustive testing (combinationally-exhaustive testing) proposed, aims at the detection of delay faults in the interconnect network. Because a programmable FPGA chip, to some extent, can be configured in the field to realize an arbitrary function, FPGA testing can be easily performed through a way of functional testing, the functional defects of the programmable resources in a FPGA chip are also well used in FPGA testing.

# **3.** Automatic Test Pattern Generation Using SAT :

Boolean Satisfiability (SAT) solvers have been the subject of remarkable improvements since the mid 90s [3]. One of the main reasons for these improvements has been the wide range of practical applications of SAT. Indeed, examples of modern applications of SAT range from termination analysis in term rewrite systems to circuit-level prediction of crosstalk noise. The success of SAT solvers motivated many practical applications, but many practical applications have also provided the examples and the challenges that allowed the development of more efficient SAT solvers. This paper provides an overview of some of the most well known applications of SAT and outlines several other successful applications of SAT[3][4]. Moreover, the improvements in SAT solvers motivated the development of new algorithms for strategic extensions of SAT. To produce reliable computer systems, defect free components must be available. Automatic test pattern generation (ATPG) systems distinguish defective components from defect-free components by generating input sets that cause the outputs of a component under test to be different if the component is defective than if it is defect free[2][17].Existing algorithmic ATPG systems for single Stuck at faults in combinational circuits fall into two classes[8]:

- The structural methods, which perform a topological search of the circuit under test.
- The algebraic methods, which generate test patterns by manipulating algebraic formulas.

The Boolean satisfiability method for test pattern generation is used for single stuck-at faults in combinational circuits that is neither a purely structural method nor an algebraic one. The most successful ATPG systems use structural search methods[15]. Of these, the most notable are

The D-algorithm, PODEM, FAN, and SOCRATE[7]. To generate a test pattern for a single fault, first extract a formula that defines the set of test patterns that detect the fault and then use a Boolean satisfiability algorithm to satisfy the formula.

# 4. Structure-based Algorithms and ATPGs

A principle common to all structure-based test generation approaches is constructed of a combinational model of the circuit. The feedback signals are regenerated from the previous-time copies of the circuit. Algorithms based on deterministic approach generate tests by activating faults and sensitizing paths for fault propagation though the multiple copies of the combinational circuit. With the exception of a few algorithms, normally, forward time processing (FTP) is used to propagate the effect of fault and reverse time processing (RTP) is used for initialization. In FTP step, a sequence of vectors is generated in the order in which the test will be applied. The RTP test vectors are generated in the reverse order in which they are to be applied.

## 4.1 Structure-based Algorithms[7]

### 4.1.1 D-algorithm

The D-algorithm has been widely used in ATPG. It has two basic operations, namely D and J-operations. D-operation performs forward fault sensitization by selecting a single or multiple paths such that a D or D at the fault site can be driven forward until it reaches a PO. The J-operation, also called the backward line justification, is employed to a PI pattern (test pattern) that will realize all the necessary gate input values on sensitized paths. D algorithm has been used to generate tests for single stuck-at faults in combinational and sequential circuits. The algorithm uses either the 5-valued model or the 9-valued model. Five values for 5valued model are 1 (1/1), 0 (0/0), X (X/X), D (0/1), and D (1/0). The nine values for the 9-valued model are 1 (1/1), 0 (0/0), U (X/X), S0 (0/1, same as D), S1 (1/0, same as D),G0 (0/X, Good Zero), G1 (1/X, Good One), F0 (X/0, Faulty Zero) and F1 (X/1, Faulty One).

In sequential circuits, a single fault behaves like multiple faults for its repeated fault effects through time. Use of 9-valued model overcomes this deficiency while using D-algorithm for sequential test generation.

### 4.1.2 PODEM

Unlike D-algorithm that assigns values to internal lines, the PODEM (Path Oriented Decision Making) algorithm [1] assigns values only to PIs. The assignments are determined by an objective of either activating the fault or propagating the fault towards a PO. First objective of PODEM is to generate D or D on the targeted line, then the next objective is to propagate the D or D one level closer to a PO. The circuit is traced toward PIs, known as back trace, to determine the PIs required to the meet the objective. A logic value is assigned to a PI, and then the effect on the circuit is determined by the forward implication. If the objective is not satisfied, the process repeats from the unsatisfied objective. If there is a conflict, it will backtrack and change the PI(s) to untried value(s). Assignments made to PIs and the information about backtracks is maintained in a

binary In the worst case, PODEM will examine all possible input patterns exhaustively. Since backtracks in PODEM can occur only at PIs, and not on the internal lines, the total number of backtracks is expected to be fewer than those in D-algorithm.

#### 4.1.3 FAN

J-operation. Chang claims that the following three problems are solved when the values of two machines are split. First, justification at the output of an n-input gate in one machine requires at most n choices as in the 5-value model. Second, since each J-drive is for one machine only, the selections can be based on the testability of each machine as in the 5-valued model. Third, since each J-drive involves 3 values only, the tables used to store the functions of gates will have the same size as the tables used for the 5-valued model. In the split model, the relation information (UN: unknown, DI: difference and EQ: equivalence) is included in the circuit status to dynamically identify the area affected by the fault-site. initialization has completed. The memory element inputs are selected for both the current and previous time frames to extend the backtrack across time. If a PPI line needs to be set to a certain value in the current time frame, the back trace procedure selects PI and PPI values in the previous time frame too. When the previous time frame becomes the current time frame, subsequent assignments of values to PPI lines do not require any forward processing since all necessary assignments have been made. This simplifies the test generation algorithm and improves its performance.

#### 4.1.4 BACK

Chang proposed the BACK algorithm as an improvement of the EBT algorithm and like EBT, it also uses the RTP technique. However, unlike the EBT, instead of pre-selecting a path, the BACK algorithm pre-selects a primary output. It assigns D or D to the selected primary output and justifies the value backward. Without the forward propagation process of the D-algorithm, the BACK algorithm performs backward justification process through topological path (TP) is selected from the fault site to a PO. The TP is processed in reverse order from circuit output back to the site of the fault. The test generation procedure starts with a single time frame in the iterative array model. PI and PPI values are determined

that will propagate the effect of the fault along the TP to the PO in the current time frame. The objective of back trace is to determine the PI or PPI values to achieve a desired value on the target line. After a time frame is processed, all memory elements that are not initialized are selected, and back trace continues in the previous time frame until relevant.

#### 4.1.5 EBT

The previous algorithms were primarily developed for combinational circuits. The Extended Back Track (EBT) algorithm [18] performs sequential test generation using RTP. BACK algorithm performs backward justification process Fujiwara and Shimono proposed the FAN algorithm, which

is a refinement of PODEM with an aim to reduce the number

of backtracks. FAN performs special processing of fan-out points and has been shown to be more efficient and faster than PODEM.

His method splits the values in the 9-valued model into two sets of values, one for the good machine and the other for the faulty machine such that one can treat two difference machines separately in J-operation.

through the circuit and through time thus making it easier to implement while requiring less run time memory. Cheng also proposed a circuit model called SPLIT to implement 9-valued model decision tree.

# **4.** Applying Genetic Algorithm to Test Pattern Generation:

GA can be used in ATPG for exploring the work space. In genetic terms every test vector is considered as a chromosome and set of test vector is called as population. The ATPG performs in 2 phases. To assess every test vector in a population in any generation of evolution. The ATPG algorithm performs in two phases. In the first phase the initial population is being generated with the help of pseudo random process. In the second phase the GA phase the test vectors are evolved based on fitness function[14].The fitness function used is :

```
Fitness = NFi
```

{

```
Where NFi is the number of faults detected.
```

```
FL= {total number of faults}
initial pop=phase I (FL);
if (FL =NULL)
break;
phase II (initial pop, FL);
```

# Figure 1: Pseudo-code of overall GA based test pattern generation

Phase I

In this phase the initial sequences composed of M vectors are generated based on pseudo random process. The generated sequences are fault simulated for the faults in the fault list. If the sequence detects fault that fault is removed from the fault list and the corresponding sequence is added into the solution set. If no faults are detected by the sequence, then the last sequence generated in the corresponding cycle is added to the set. This process is repeated for max\_iter.

Function Phase I

initial pop (FL)
for (i=1; i<max\_iter-1, i++)
{
 initial pop=phase I(FL);</pre>

randomly generate sequences of length L; for (each sequence) { if sequence detects faults in the fault list { add sequence to the test set;

```
drop the faults detected by that sequence;

}

return (initial population);

}
```

#### Figure 2: The Pseudo-code of Phase I

#### Phase II

The initial population of GA is composed of the sequences generated in phase I. To generate a new population from the existing one, two individuals (parents) are selected and crossed to create two entirely individuals (child) and each child is mutated with some small mutation probability. The selection operator is rank based selection. In rank based selection, the solutions are sorted according to their fitness from the worst (rank 1) to the best (rank N).Each member in the sorted list is assigned a fitness equal to the rank of the solution in the list. Thereafter the proportionate selection operator is applied with the ranked fitness value and better solutions are chosen. The two parents are crossed to create two entirely new individuals (i.e.) child and each child is mutated with some small mutation probability. The two new individuals are than placed in the new population and the process continues until the generation is entirely filled. The previous population is discarded. Crossover used is one point crossover. A crossover probability of 2 and mutation probability of 0.03 is used in all circuits. The no\_gen is assumed to be 16, to reduce the execution time. During test generation pop\_size of 25 is used. Function Phase II

{

```
Initial pop from phase1;
for (l=1;l<no_gen-1;l++)
{ for (k=1; k<popsize-1;k++)
        { select two individuals from
            population;
            apply crossover with probability 2;
            apply mutation with probability 0.03;}
            compute fitness of the individuals;
            for (each sequence)
            if (sequence detects the faults in the fault list
            { add sequence to the solution set;
                 drop the faults detected by the sequence;
            }
        }
    }
}
```



### 5. Conclusion

SAT problems produce excellent results on various benchmarks. Multi-objective when applied on Boolean SAT makes it more scalable. It can also be applied to solve multiple SAT instances simultaneously in order to increase the speed of execution.

Multi-objective optimization is that in which we have to optimize multiple objectives. So this field can be applied to various SAT instances to increase the efficiency of test generation.

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